

## ORIGINAL ARTICLE

High quality factor microwave dielectric ceramics in the  
(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)O<sub>2</sub>–ZrO<sub>2</sub>–TiO<sub>2</sub> ternary systemWen-Bo Li<sup>1</sup> | Di Zhou<sup>1,2,3</sup>  | Li-Xia Pang<sup>3,4</sup> | Yan-Zhu Dai<sup>1</sup> | Ze-Ming Qi<sup>5</sup> |  
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**Abstract**

Novel high quality factor microwave dielectric ceramics  $(1-x)\text{ZrTiO}_4-x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ( $0.325 \leq x \leq 0.4$ ) and  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  ( $0.2 \leq y \leq 0.5$ ) with the addition of 0.5 wt%  $\text{MnCO}_3$  in the  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_2\text{-ZrO}_2\text{-TiO}_2$  ternary system were prepared, using solid-state reaction method. The relationship between the structure and microwave dielectric properties of the ceramics was studied. The XRD patterns of the sintered samples reveal the main phase belonged to  $\alpha\text{-PbO}_2$ -type structure. Raman spectroscopy and infrared reflectivity (IR) spectra were employed to evaluate phonon modes of ceramics. The  $0.65\text{ZrTiO}_4\text{-}0.35(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4\text{-}0.5$  wt%  $\text{MnCO}_3$  ceramic can be well densified at  $1240^\circ\text{C}$  for 2 hours and exhibits good microwave dielectric properties with a relative permittivity ( $\epsilon_r$ ) of 42.5, a quality factor ( $Q \times f$ ) value of 43 520 GHz (at 5.9 GHz) and temperature coefficient of resonant frequency ( $\tau_f$ ) value of  $-5$  ppm/ $^\circ\text{C}$ . Furthermore, the  $(\text{ZrTi})_{0.7}(\text{Mg}_{1/3}\text{Nb}_{2/3})_{0.3}\text{O}_4\text{-}0.5$  wt%  $\text{MnCO}_3$  ceramic sintered at  $1260^\circ\text{C}$  for 2 hours possesses a  $\epsilon_r$  of 31.8, a  $Q \times f$  value of 35 640 GHz (at 6.3 GHz) and a near zero  $\tau_f$  value of  $-5.9$  ppm/ $^\circ\text{C}$ . The results demonstrated that the  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_2\text{-ZrO}_2\text{-TiO}_2$  ternary system with excellent properties was a promising material for microwave electronic device applications.

**KEYWORDS**

dielectric materials/properties, phase diagrams, solid solutions, sinter/sintering

## 1 | INTRODUCTION

Microwave communication technology has been widely studied and made remarkable progress in the past decades for practical application.<sup>1-5</sup> Microwave dielectric ceramics have been used as components extensively in the filters units of communication systems, such as wireless fidelity (WIFI), global positioning systems (GPS) patch antennas, and mobile telephones, etc.<sup>6-10</sup> In particular, dielectric resonator has a very important position in microwave integrated circuits and microwave filters. Microwave dielectric ceramics with high-dielectric permittivities ( $\epsilon_r$ ), high quality factor ( $Q \times f$ ), small or zero temperature coefficient of resonant frequency ( $\tau_f$ ) and nontoxic constituents are indispensable for microwave devices.<sup>11,12</sup>

The binary system  $ZrO_2$ - $TiO_2$  has been studied as good candidates for microwave dielectric materials in the last two decades. Previous studies show that  $ZrTiO_4$  based solid solutions with  $\alpha$ - $PbO_2$  type structure have been widely used as dielectric resonators because of good microwave dielectric properties.<sup>13-15</sup> The studies conduct that  $Zr^{4+}$  ions or  $Ti^{4+}$  ions substitution by  $M^{4+}$  ions has a significant impact on the microwave dielectric properties of  $ZrO_2$ - $TiO_2$  system. It was found that the  $Zr_xSn_yTi_zO_4$  ( $x+y+z=2$ ) system has superior microwave dielectric properties, near zero  $\tau_f$  value and high  $Q \times f$  value.<sup>16</sup> Due to the difference between the ionic radii of  $Zr^{4+}$  ions (0.72 Å, CN=6) and  $Ti^{4+}$  ions (0.53 Å, CN=6),  $ZrO_2$ - $TiO_2$  binary system substitution by  $(AB)^{4+}$  ions have been investigated.<sup>17</sup> Such as  $Zn_{1/3}Ta_{2/3}O_2$ - $ZrO_2$ - $TiO_2$  ternary system,  $Zn_{1/3}Nb_{2/3}O_2$ - $ZrO_2$ - $TiO_2$  ternary system and  $Zr(Zn_{1/3}Nb_{2/3})_xTi_{2-x}O_6$ .<sup>18-22</sup> It is well known that the microwave dielectric ceramic  $Zn_{1/3}Ta_{2/3}O_2$ - $ZrO_2$ - $TiO_2$  ternary system has been investigated extensively. For example, Kim et al. showed that  $Zr_{1-x}(Zn_{1/3}Ta_{2/3})_xTiO_4$  ( $0.2 \leq x \leq 0.6$ ) with increasing  $Zn_{1/3}Ta_{2/3}O_2$  content, two-phase regions were observed:  $\alpha$ - $PbO_2$  solid solution region below  $x < 0.35$ , rutile type  $Zn_{1/3}Ta_{2/3}TiO_4$ , and the  $\alpha$ - $PbO_2$  solid solution with further substitution of  $Zn_{1/3}Ta_{2/3}O_2$ .  $Zr_{0.65}(Zn_{1/3}Ta_{2/3})_{0.35}TiO_4$  ceramic has good microwave dielectric properties with  $\epsilon_r=42.5$ ,  $Q \times f=40$  200 GHz and  $\tau_f=1.1$  ppm/ $^\circ C$ .<sup>23</sup> As is known to all, the expensive price and high toxicity of Ta-based materials maybe limited by the  $Zn_{1/3}Ta_{2/3}O_2$ - $ZrO_2$ - $TiO_2$  ternary system in practical applications. A series of other  $(AB)^{4+}$  ions such as  $(Zn_{1/3}Nb_{2/3})^{4+}$  and  $(Li_{1/4}Nb_{3/4})^{4+}$  have been attracted by researcher attention. Recently Huang et al. reported that  $Nb^{5+}$  (0.64 Å, CN=6) ion replacing  $Ta^{5+}$  (0.64 Å, CN=6) ion form the  $Zr_x(Zn_{1/3}Nb_{2/3})_{1-x}TiO_4$  ( $x=0.1-0.4$ ) solid solutions with high  $\epsilon_r=51$ ,  $Q \times f=26$  600 GHz and  $\tau_f=70$  ppm/ $^\circ C$ .<sup>24</sup> Our previous work investigated  $(Li_{1/4}Nb_{3/4})^{4+}$ -doped  $ZrO_2$ - $TiO_2$  system and found that crystalline phases and microwave dielectric properties of

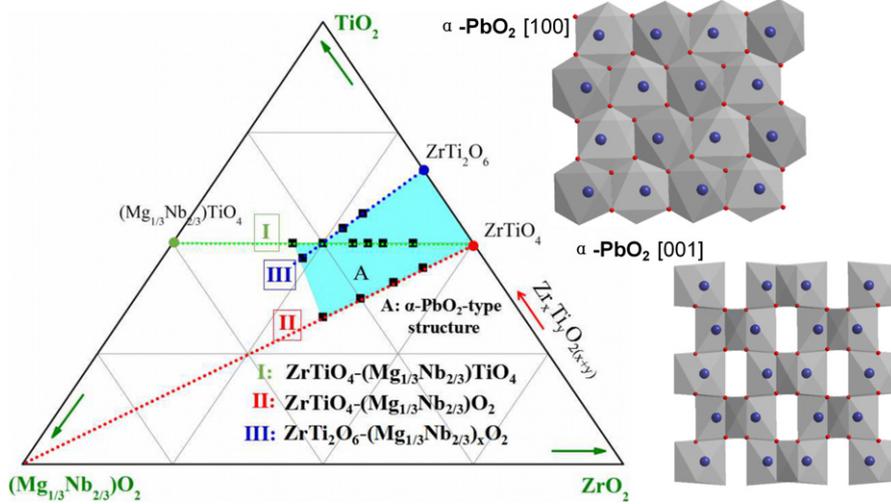
$(Li_{1/4}Nb_{3/4})_{0.4}Zr_xTi_yO_4$  depended greatly on the Zr/Ti ratio.<sup>25,26</sup> In our work, pure  $(Mg_{1/3}Nb_{2/3})TiO_4$  ceramic can be well densified at 1220 $^\circ C$  for 2 hours and exhibits good microwave dielectric properties with a  $\epsilon_r$  of 81.9, a  $Q \times f$  value of 13 380 GHz (at 4.5 GHz) and  $\tau_f$  value of +277.5 ppm/ $^\circ C$ .

In the present work, we investigated the structure and microwave dielectric properties of the  $Mg_{1/3}Nb_{2/3}O_2$ - $ZrO_2$ - $TiO_2$  ternary system. Figure 1 presents phase diagram of the  $Mg_{1/3}Nb_{2/3}O_2$ - $ZrO_2$ - $TiO_2$  ternary system. As seen from Figure 1, the  $ZrTiO_4$ - $(Mg_{1/3}Nb_{2/3})TiO_4$  and  $(ZrTi)_{1-y}(Mg_{1/3}Nb_{2/3})_yO_4$  phases regions were highlighted by the green line and the red line, respectively. In this system, novel solid solution 0.5 wt%  $MnCO_3$ -doped  $(1-x)ZrTiO_4-x(Mg_{1/3}Nb_{2/3})TiO_4$  ( $0.325 \leq x \leq 0.4$ ) and  $(ZrTi)_{1-y}(Mg_{1/3}Nb_{2/3})_yO_4$  ( $0.2 \leq y \leq 0.5$ ) ceramics were prepared, using solid-state reaction method. Sintering behavior, phase composition, microstructures, microwave dielectric properties, and the relation between structure and microwave dielectric properties of the ceramics were studied in detail.

## 2 | EXPERIMENTAL PROCEDURE

The starting materials of  $ZrO_2$  ( $\geq 99\%$ ),  $MgO$  ( $>98\%$ ),  $Nb_2O_5$  ( $>99\%$ ),  $TiO_2$  ( $>99.84\%$ ), and  $MnCO_3$  ( $>98\%$ ) were used according to the stoichiometric formula  $(1-x)ZrTiO_4-x(Mg_{1/3}Nb_{2/3})TiO_4$  ( $0.325 \leq x \leq 0.4$ ) and  $(ZrTi)_{1-y}(Mg_{1/3}Nb_{2/3})_yO_4$  ( $0.2 \leq y \leq 0.5$ ) with 0.5 wt%  $MnCO_3$ . Powders were mixed with the Zirconia balls in ethanol and milled for 4 hours, using a planetary mill operating at a running speed of 150 rpm. After being milled, two kinds of powders were calcined at 1000 $^\circ C$  and 1100 $^\circ C$  for 4 hours, respectively. After being crushed, the powders were remilled for 5 hours to increase reactivity and homogeneity and then dried. The as-dried powders were mixed with 5 wt% polyvinyl alcohol (PVA) binder and granulated, and then these powders were pressed into cylinders (10 mm in diameter and 4~5 mm in height) in a steel die under a uniaxial pressure of 200 MPa. Samples were sintered in the temperature ranges from 1200 $^\circ C$  to 1260 $^\circ C$  for 2 hours in ambient atmosphere, respectively.

The crystalline structures of samples were investigated, using X-ray diffraction (XRD) with  $CuK\alpha$  radiation (Rigaku D/MAX-2400 X-ray diffractometer, Tokyo, Japan,  $\lambda=1.54056$  Å) at a scanning rate of 0.02 $^\circ s^{-1}$  in a  $2\theta$  range of 10 $^\circ$ -70 $^\circ$ . Microstructures of the sintered ceramic were characterized with scanning electron microscopy (SEM) (SEM; Quanta 250 F, FEI). The Raman spectra were recorded at room temperature, using a Raman spectrometer (inVia, Renishaw, England) excited with an Ar<sup>+</sup> laser (514.5 nm). Room temperature infrared reflectivity



**FIGURE 1** Ternary phase diagram for the system  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_2\text{-ZrO}_2\text{-TiO}_2$ . The  $\text{ZrTiO}_4\text{-(Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  and  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  phases region are indicated by the black line and red line, respectively. The  $\alpha\text{-PbO}_2$  phase of region A is indicated by the cyan areas [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com)]

spectra were measured, using a Bruker IFS 66v FT-IR spectrometer on the infrared beamline station (U4) at the National Synchrotron Radiation Lab (NSRL), China. Microwave dielectric behaviors were measured with the  $TE_{018}$  shielded cavity method with a network analyzer (8720ES, Agilent, Palo Alto, CA) and a temperature chamber (Delta 9023, Delta Design, Powa CA) in the temperature range of 25°C-85°C. Temperature coefficient of resonant frequency (TCF or  $\tau_f$  value) was calculated with the following formula:

$$\tau_f = \frac{f_{85} - f_{25}}{f_{25}(85 - 25)} \times 10^6 \text{ ppm}/^\circ\text{C}, \quad (1)$$

where  $f_{85}$  and  $f_{25}$  were the  $TE_{018}$  resonant frequencies at 85°C and 25°C, respectively.

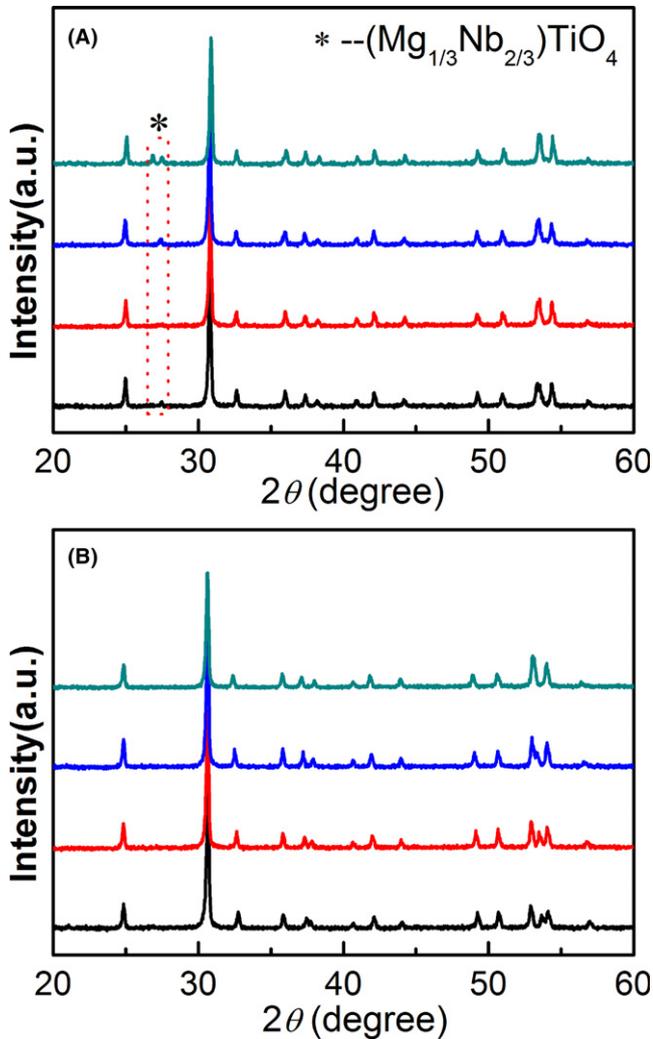
### 3 | RESULTS AND DISCUSSIONS

Figure 2 shows XRD patterns of the  $(1-x)\text{ZrTiO}_4\text{-}x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ( $0.325 \leq x \leq 0.4$ ) and  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  ( $0.2 \leq y \leq 0.5$ ) ceramics sintered at optimal temperatures for 2 hours with 0.5 wt %  $\text{MnCO}_3$  addition. The peaks are indexed, using the standard PDF cards of  $\text{ZrTiO}_4$  (PDF code: 34-0415). It is found that all the diffraction peaks of the  $(1-x)\text{ZrTiO}_4\text{-}x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ( $0.325 \leq x \leq 0.4$ ) and  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  ( $0.2 \leq y \leq 0.5$ ) ceramic sintered at 1240°C could be indexed as  $\alpha\text{-PbO}_2$ -type structure [space group  $Pnab$  (60)], which is shown in Figure 1. However, some tiny peaks corresponding to the  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  phase in Figure 2A. The Pb-site cation is coordinated by 6 oxygen forming  $\text{PbO}_6$  octahedra. Based on the Shannon's data, equivalent ionic radii of  $\text{Zr}^{4+}$  ions with coordination numbers (CN=6) is 0.72 Å. The equivalent ionic radii of  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  ions can be calculated by the

following equation:  $r = 1/3R(\text{Mg}^{2+}) + 2/3R(\text{Nb}^{5+}) = 0.67 \text{ \AA}$  (ionic radii for  $\text{Mg}^{2+}$  and  $\text{Nb}^{5+}$  are 0.72 Å and 0.64 Å, respectively).<sup>27</sup> The result shows that the equivalent ionic radii of  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  is smaller than that of  $\text{Zr}^{4+}$  (0.72 Å), it is understandable that the  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  ion can occupy the  $\text{Zr}^{4+}$  sites. Moreover, the  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  is larger than that of  $\text{Ti}^{4+}$  (0.604 Å). It is believed that  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  ions are more likely to enter  $\text{Zr}^{4+}$  site in the  $(1-x)\text{ZrTiO}_4\text{-}x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ( $0.325 \leq x \leq 0.4$ ) and  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  ( $0.2 \leq y \leq 0.5$ ) ceramics. The XRD results indicates that  $\alpha\text{-PbO}_2$ -type solid solution was formed in the 0.5 wt%  $\text{MnCO}_3$ -doped  $(1-x)\text{ZrTiO}_4\text{-}x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ( $0.325 \leq x \leq 0.4$ ) and  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  ( $0.2 \leq y \leq 0.5$ ) ceramics.

SEM images of cross-section of the 0.5 wt%  $\text{MnCO}_3$ -doped  $(1-x)\text{ZrTiO}_4\text{-}x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ( $x=0.325, 0.35, 0.4$ ) and  $(\text{ZrTi})_{(1-y)}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  ( $y=0.2, 0.3, 0.4$ ) ceramics sintered at optimal temperatures for 2 hours are depicted in Figure 3. From Figure 3A-C, it can be seen that dense microstructures were observed and the average grain size of the  $\text{ZrTiO}_4\text{-(Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4\text{-}0.5 \text{ wt\% MnCO}_3$  ceramic is in the range of 4-5  $\mu\text{m}$ . The  $(\text{ZrTi})\text{(Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4\text{-}0.5 \text{ wt\% MnCO}_3$  ceramics have less porous microstructures in Figure 3C,D. Compared with the  $\text{ZrTiO}_4\text{-(Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4\text{-}0.5 \text{ wt\% MnCO}_3$  ceramic, the average grain sizes of  $(\text{ZrTi})\text{(Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4\text{-}0.5 \text{ wt\% MnCO}_3$  ceramics are much larger.

Figure 4 shows the density and microwave dielectric properties of the  $(1-x)\text{ZrTiO}_4\text{-}x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ( $0.325 \leq x \leq 0.4$ ) ceramics with 0.5 wt%  $\text{MnCO}_3$  sintered at temperatures ranging from 1200°C to 1260°C as a function of  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  addition. From Figure 4A, the density of sample increases with the increase of  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$ . It should be related to the solubilization of  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  ions into the sites of  $\text{Zr}^{4+}$  ions. The densities of the sample sintered at

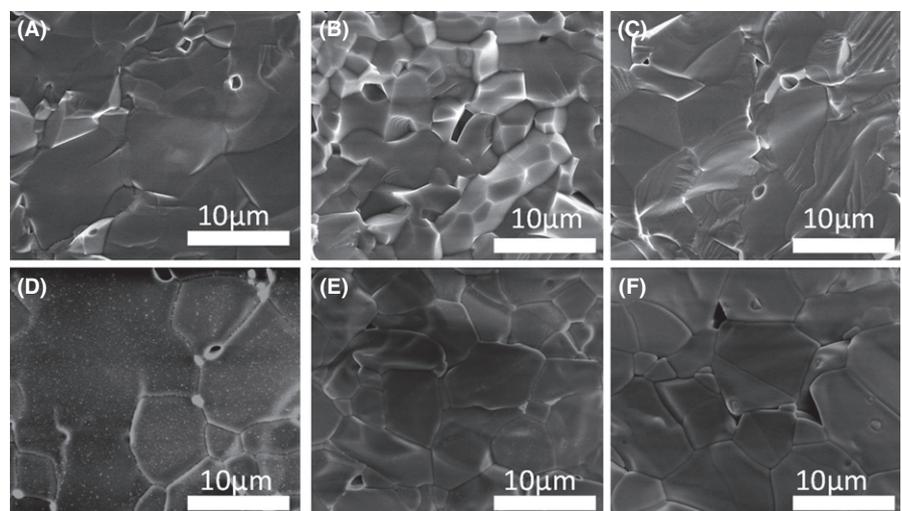


**FIGURE 2** XRD patterns of the sintered 0.5 wt%  $\text{MnCO}_3$ -doped  $(1-x)\text{ZrTiO}_4-x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  (A) and  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  (B) ceramics [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com)]

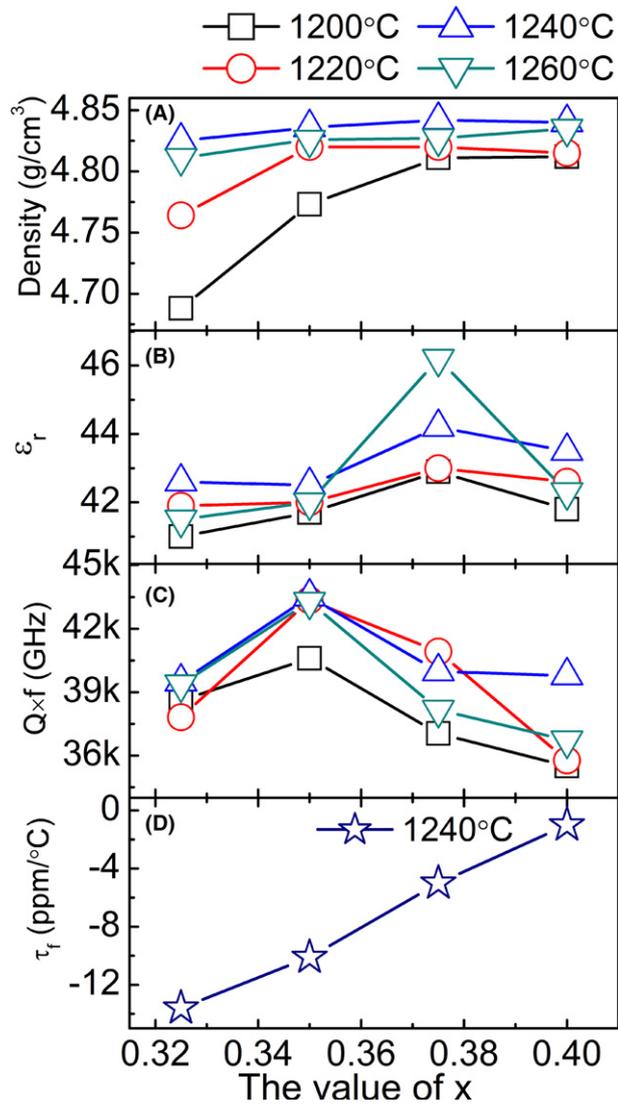
1240°C for 2 hours show the maximum apparent density  $4.85 \text{ g/cm}^3$  at  $x=0.375$ . Permittivity of the sample increased firstly with the  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  addition from  $x=0.325$  to

$0.375$ , and then decreased at  $x=0.4$ . Permittivity of samples sintered at 1240°C increased first from 42.6 to maximum value of 44.2, and then reduced to 43.5. Figure 4C,D shows  $Q \times f$  and  $\tau_f$  values of the  $(1-x)\text{ZrTiO}_4-x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ( $0.325 \leq x \leq 0.4$ ) ceramics with 0.5 wt%  $\text{MnCO}_3$  addition sintered at temperatures ranging from 1200°C to 1260°C as a function of the  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  addition. The variation in  $Q \times f$  value versus sintering temperature presented similar behavior to that of permittivity, the  $Q \times f$  values increased and then decreased rapidly as the  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  addition was increased further. As shown in Figure 4D, the  $\tau_f$  value increased gradually step by step with  $x$  value. High performance of microwave dielectric properties of the  $0.65\text{ZrTiO}_4-0.35(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ceramic can be obtained sintered at 1240°C for 2 hours with  $\epsilon_r \sim 44.2$ ,  $Q \times f \sim 40\,030 \text{ GHz}$  and  $\tau_f \sim -10.1 \text{ ppm/}^\circ\text{C}$ . Table 1 shows the microwave dielectric properties of the  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  ( $0.2 \leq y \leq 0.5$ ) ceramics with 0.5 wt%  $\text{MnCO}_3$  sintered at optimized sintering temperature. The samples can be sintered well at 1200°C–1260°C with  $\epsilon_r$  of 31.5–33.2, the  $Q \times f$  values of 24 100–38 600 GHz, and the  $\tau_f$  values of  $-23 \text{ ppm/}^\circ\text{C}$  to  $6 \text{ ppm/}^\circ\text{C}$ . The  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$  ceramics can be obtained the best microwave dielectric properties with permittivity  $\sim 31.8$ ,  $Q \times f \sim 35\,640 \text{ GHz}$  and  $\tau_f \sim -5.9 \text{ ppm/}^\circ\text{C}$  when  $y=0.3$ .

Raman spectroscopy is a useful tool to study the structures and identify vibrational modes of solid materials.<sup>28–30</sup> Figure 5 shows room-temperature Raman spectrum of the 0.5 wt%  $\text{MnCO}_3$ -doped  $0.65\text{ZrTiO}_4-0.35(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  and  $(\text{ZrTi})_{0.7}(\text{Mg}_{1/3}\text{Nb}_{2/3})_{0.3}\text{O}_4$  ceramics over the range  $150\text{--}900 \text{ cm}^{-1}$ .  $\text{ZrTiO}_4$  with a random distribution of zirconium and titanium ions (taking zirconium and titanium ions as one type of averaged ion) has an orthorhombic  $\alpha\text{-PbO}_2$  structure (space group  $Pbcn$ ). Using the factor group analysis, the phonons of  $\text{ZrTiO}_4$  in the  $\Gamma$ -point of the first Brillouin zone can be described as follows:<sup>31</sup>



**FIGURE 3** SEM images of fractured surface of the sintered 0.5 wt%  $\text{MnCO}_3$ -doped  $(1-x)\text{ZrTiO}_4-x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$ :  $x=0.325$  (A),  $x=0.35$  (B),  $x=0.375$  (C) and  $(\text{ZrTi})_{1-y}(\text{Mg}_{1/3}\text{Nb}_{2/3})_y\text{O}_4$ :  $y=0.2$  (D),  $y=0.3$  (E),  $y=0.4$  (F) ceramics



**FIGURE 4** The density and microwave dielectric properties of 0.5 wt%  $\text{MnCO}_3$ -doped  $(1-x)\text{ZrTiO}_4-x(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  ( $0.325 \leq x \leq 0.4$ ) ceramics as a function of  $x$  value and sintering temperature [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com)]

$$\Gamma = 4A_g + 5B_{1g} + 4B_{2g} + 5B_{3g} + 4A_u + 3B_{2u} + 4B_{3u} \quad (2)$$

According to the literature, 18 Raman active ( $4A_g + 5B_{1g} + 4B_{2g} + 5B_{3g}$ ) and 11 infrared active ( $4A_u + 4B_{1u} + 3B_{2u}$ ) modes are predicted.<sup>32</sup>

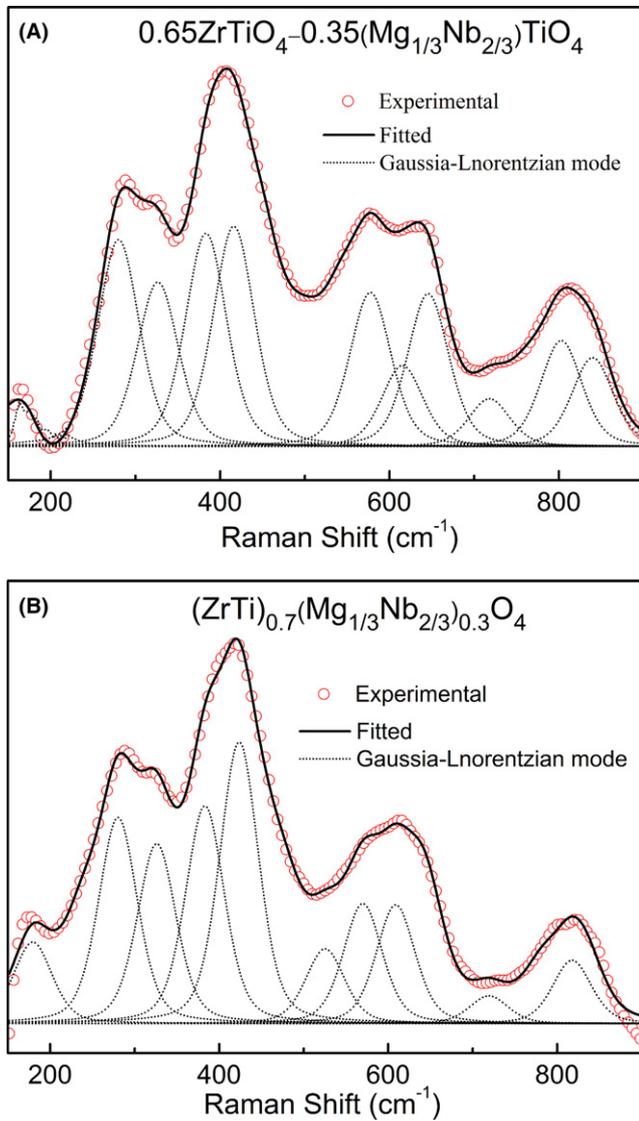
As shown in Figure 5, it is indicated that the substitution of  $\text{Zr}^{4+}$  by  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  influenced the number, intensity and location of the Raman bands. When  $\text{Zr}^{4+}$  ions is replaced by the  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  ions, less Raman bands appear and most of the peaks become broader. Some weak Raman bands of  $\text{ZrTiO}_4$ , such as those centered at  $397 \text{ cm}^{-1}$ , and  $730 \text{ cm}^{-1}$  disappeared with the substitution of  $\text{Zr}^{4+}$  by  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  in Figure 5. The number of visible Raman bands of 0.5 wt%  $\text{MnCO}_3$ -doped  $0.65\text{ZrTiO}_4-0.35(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  and  $(\text{ZrTi})_{0.7}(\text{Mg}_{1/3}\text{Nb}_{2/3})_{0.3}\text{O}_4$  ceramics are 11 and 10 in the range of  $150 \text{ cm}^{-1}$  to  $900 \text{ cm}^{-1}$ , respectively. In order to observe the lattice vibrational modes, the peaks were fitted by the standard Gaussia-Lorentzian model, and the fitted Raman spectra are plotted in Figure 5 as solid lines. In this study, the expected wavenumbers of the characteristic bands of  $\text{TiO}_4$  tetrahedron are  $306 \text{ cm}^{-1}$ ,  $371 \text{ cm}^{-1}$ ,  $761 \text{ cm}^{-1}$ ,  $770 \text{ cm}^{-1}$  and that of  $\text{ZrO}_4$  tetrahedron are  $332 \text{ cm}^{-1}$ ,  $387 \text{ cm}^{-1}$ ,  $792 \text{ cm}^{-1}$ , and  $846 \text{ cm}^{-1}$ . Three bands centered at  $271 \text{ cm}^{-1}$ ,  $406 \text{ cm}^{-1}$ ,  $640 \text{ cm}^{-1}$  are assigned to vibrational modes  $\text{Ti}(\text{Zr})\text{O}_6$  octahedron.<sup>33</sup> Since  $(\text{Mg}_{1/3}\text{Nb}_{2/3})^{4+}$  ions are more likely to enter  $\text{Zr}^{4+}$  site substituting  $\text{Zr}^{4+}$ , a  $(\text{MgNb})-\text{O}$  bond is formed and the length of the  $(\text{MgNb})-\text{O}$  bond is shorter than that of the  $\text{Zr}-\text{O}$  bond in the lattice. Based on Raman data in Figure 5, the spectrum recorded in the studied system is in good agreement with that of the previously reported  $\text{Zr}_{1-x}(\text{Li}_{1/4}\text{Nb}_{3/4})_x\text{TiO}_4$  ( $0 \leq x \leq 0.5$ ) samples.<sup>25,26</sup>

Figure 6 presents IR reflectivity spectra of the  $0.65\text{ZrTiO}_4-0.35(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  and  $(\text{ZrTi})_{0.7}(\text{Mg}_{1/3}$

**TABLE 1** Microwave dielectric properties of 0.5 wt%  $\text{MnCO}_3$ -doped temperature stable ceramics  $(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_2-\text{ZrO}_2-\text{TiO}_2$  ternary system

No.	Composition	S.T. (°C)	$\epsilon_r$	$Q \times f$ (GHz)	$\tau_f$ (ppm/°C)
1	$(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$	1220	81.9	13 380	+277.5
2	$0.675\text{ZrTiO}_4-0.325(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$	1240	42.6	39 490	-13.6
3	$0.65\text{ZrTiO}_4-0.35(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$	1240	42.5	43 510	-10.1
4	$0.625\text{ZrTiO}_4-0.375(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$	1260	44.2	39 980	-5
5	$0.6\text{ZrTiO}_4-0.4(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$	1240	43.5	39 780	-1
6	$(\text{ZrTi})_{0.8}(\text{Mg}_{1/3}\text{Nb}_{2/3})_{0.2}\text{O}_4$	1260	33.0	24 100	+6
7	$(\text{ZrTi})_{0.7}(\text{Mg}_{1/3}\text{Nb}_{2/3})_{0.3}\text{O}_4$	1260	31.8	35 640	-5.9
8	$(\text{ZrTi})_{0.6}(\text{Mg}_{1/3}\text{Nb}_{2/3})_{0.4}\text{O}_4$	1260	31.5	28 000	-12
9	$(\text{ZrTi})_{0.5}(\text{Mg}_{1/3}\text{Nb}_{2/3})_{0.5}\text{O}_4$	1220	33.2	38 600	-23

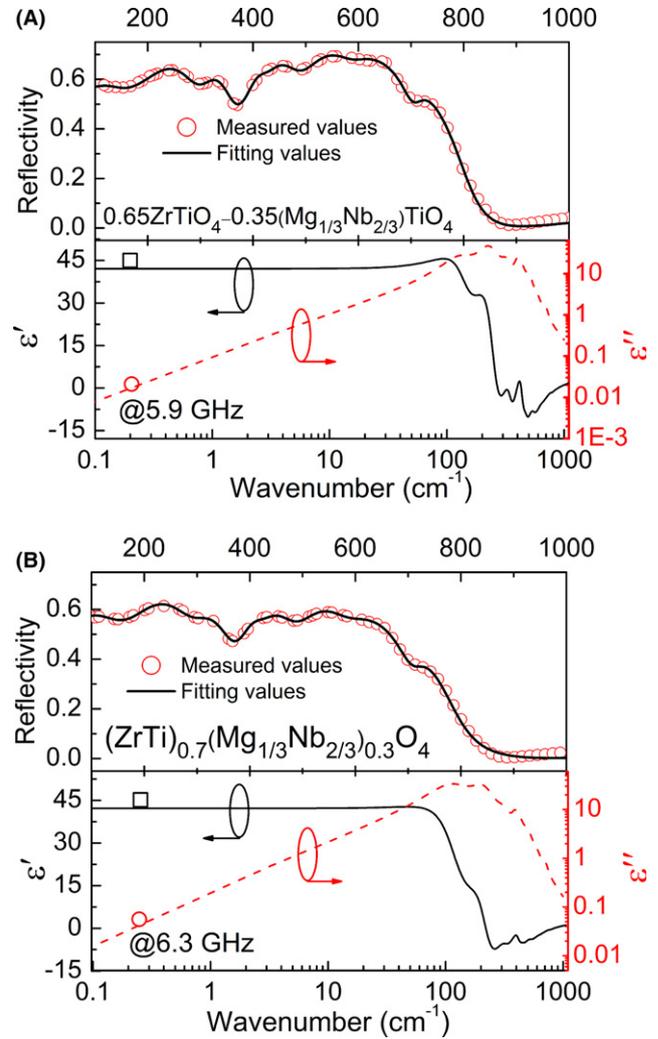
S.T., Sintering Temperature.



**FIGURE 5** Room-temperature Raman spectra of 0.5 wt%  $\text{MnCO}_3$ -doped  $0.65\text{ZrTiO}_4-0.35(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  (A) and  $(\text{ZrTi})_{0.7}(\text{Mg}_{1/3}\text{Nb}_{2/3})_{0.3}\text{O}_4$  (B) ceramics sintered at  $1240^\circ\text{C}$ . (Circles show the observed data, thick black solid line give the model fit and the dashed line indicates the Gaussian-Lorentzian mode fitting) [Color figure can be viewed at [wileyonlinelibrary.com](#)]

$\text{Nb}_{2/3})_{0.3}\text{O}_4$  ceramics with 0.5 wt%  $\text{MnCO}_3$  addition in the range  $100\text{ cm}^{-1}\sim 1000\text{ cm}^{-1}$ . It is seen that the infrared spectra can be well fitted by 8 resonant modes which is less than the predicted value by group theory analysis mentioned above. The measured spectrum was similar to that of the  $\text{ZrTiO}_4$ . These spectra were analyzed, using the classical harmonic oscillator model based on the standard Lorentzian formula [Equation (3)] and the Fresnel formula [Equation (4)]:<sup>34,35</sup>

$$\varepsilon^*(\omega) = \varepsilon_\infty + \sum_{j=1}^n \frac{\omega_{pj}^2}{\omega_{oj}^2 - \omega^2 - i\gamma_j\omega} \quad (3)$$



**FIGURE 6** Measured and calculated infrared reflectivity spectra and complex dielectric spectra of 0.5 wt%  $\text{MnCO}_3$ -doped  $0.65\text{ZrTiO}_4-0.35(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{TiO}_4$  (A) and  $(\text{ZrTi})_{0.7}(\text{Mg}_{1/3}\text{Nb}_{2/3})_{0.3}\text{O}_4$  (B) ceramic (solid line for fitting values and hollow symbol for measured values, circles are experimental at microwave region, and solid lines represent the fit of IR spectra) [Color figure can be viewed at [wileyonlinelibrary.com](#)]

$$R(\omega) = \left| \frac{1 - \sqrt{\varepsilon^*(\omega)}}{1 + \sqrt{\varepsilon^*(\omega)}} \right|^2, \quad (4)$$

where  $\varepsilon^*(\omega)$  is complex dielectric function;  $\varepsilon_\infty$  is the dielectric constant caused by the electronic polarization at high frequencies;  $\omega_{pj}$ ,  $\omega_{oj}$ , and  $\gamma_j$  are the plasma frequency, the transverse frequency, and damping factor of the  $j$ -th Lorentz oscillator, respectively;  $n$  is the number of transverse phonon modes;  $R(\omega)$  is the IR reflectivity.

Figure 6 is also shown the calculated permittivity  $\varepsilon'(\omega)$  and loss  $\varepsilon''(\omega)$  obtained from the fits of the infrared reflectivity together with the experimental microwave data. The fitting of the infrared reflectivity spectra of the 0.5 wt%  $\text{MnCO}_3$ -doped  $0.65\text{ZrTiO}_4-0.35(\text{Mg}_{1/3}\text{Nb}_{2/3})$

TiO<sub>4</sub> and (ZrTi)<sub>0.7</sub>(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)<sub>0.3</sub>O<sub>4</sub> ceramics. It is observed that the calculated  $\epsilon_r$  is a little smaller than the measured ones in the microwave range. Meanwhile, all the calculated dielectric permittivity and dielectric loss values are nearly equal to the measured ones, using  $TE_{01\delta}$  method. Therefore, it can be concluded that majority of the dielectric contribution for (Mg<sub>1/3</sub>Nb<sub>2/3</sub>)O<sub>2</sub>-ZrO<sub>2</sub>-TiO<sub>2</sub> system at the microwave region was attributed to the absorptions of phonon oscillation at infrared region and very little contribution from defect phonon scattering.

## 4 | CONCLUSION

In the present work, the 0.5 wt% MnCO<sub>3</sub>-doped (1-x)ZrTiO<sub>4</sub>-x(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)TiO<sub>4</sub> (0.325 ≤ x ≤ 0.4) and (ZrTi)<sub>1-y</sub>(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)<sub>y</sub>O<sub>4</sub> (0.2 ≤ y ≤ 0.5) ceramics were obtained at low sintering temperatures. High performance of microwave dielectric properties can be obtained in the 0.65ZrTiO<sub>4</sub>-0.35(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)TiO<sub>4</sub> ceramics with  $\epsilon_r$  of 42.5,  $Q \times f$  values of 43 520 GHz (at 5.9 GHz), and near zero  $\tau_f$  values of -5 ppm/°C. Meanwhile, the (ZrTi)<sub>0.7</sub>(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)<sub>0.3</sub>O<sub>4</sub> ceramic sintered at 1260°C for 2 hours with a  $\epsilon_r$  of 31.8, a  $Q \times f$  value of 35 640 GHz and a near zero  $\tau_f$  value of -5.9 ppm/°C. The Raman spectrum and infrared spectra analysis indicated that the majority of the dielectric polarization at microwave frequency was contributed by the phonon oscillation.

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