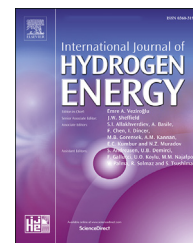




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Kinetic modeling investigation on the coupling effects of H₂ and CO₂ addition on the laminar flame speed of hydrogen enriched biogas mixture

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HIGHLIGHTS

- Coupling effects of H₂ and CO₂ on S_L were isolated and analyzed.
- H₂ chemical effects result in the reduced dropping trend of S_L via R84 and R3.
- CO₂ chemical effects dominate the more evident decrease of S_L at the rich condition.
- R3, R46, R52, R84, R99 and R158 have major contributions on the chemistry transition.
- H₂/CO₂-related chemistry can be monitored directly by R84 and R99.

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ABSTRACT

The numerical simulation was conducted to investigate the coupling effects of H₂ and CO₂ on the laminar flame speed and reaction pathways of the biogas-hydrogen mixtures. The same proportions of H₂ and CO₂ were considered in the study. The dilution effects, chemical effects and thermal effects of H₂ and CO₂ were isolated, while the contributions of different effects were also calculated to identify the dominating factor. The results show that H radical pool plays the important role in the variation of laminar flame speed of biogas-hydrogen mixture. The coupling dilution effects of H₂ and CO₂ lead to the considerable decrease of H radical and dominate the decreased laminar flame speed. The H₂ chemical effects improve R84 (OH + H₂ = H₂O + H) and R3 (O + H₂ = H + OH) quite effectively, which results in the reduced dropping trends of H radical and laminar flame speed from BG60H40 to BG40H60. The CO₂ chemical effects suppress the major H radical production reactions of R84, R3, R99 (OH + CO = H + CO₂) and R10 (O + CH₃ = H + CH₂O) more apparently at the fuel-rich condition, while importance of major consumption reactions (R53: H + CH₄ = CH₃+H₂, R52: H + CH₃(+M) = CH₄(+M) and R58: H + CH₂-O = HCO + H₂) are higher at the fuel-rich condition. This dominates the more evident decrease of H radical and laminar flame speed at the fuel-rich condition. Based on the ROP analysis, R3, R46 (H + HO₂ = 2OH), R52, R84, R99 and R158 (2CH₃(+M) = C₂H₆(+M)) have the major contributions on the chemistry transition caused by the coupling effects of H₂ and CO₂. The decreased contribution of R158 and R99 indicate the weakened CH₄-related chemistry while the increased contributions of R3, R46, R52 and R84 indicate the improved H₂-related chemistry in the biogas-hydrogen flame. Furthermore, coupling effects of H₂

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and CO₂ or H₂/CO₂-related chemistry can be monitored by the contribution variations of R84 and R99 on the OH radical concentration.

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Introduction

The serious environmental challenges and the increasing world consumption of fossil energy have prompted much more efforts to be made so as to develop sustainable and renewable fuels in recent decades. Biogas (BG) is considered as a promising renewable clean fuel due to its short carbon cycle and its easy productivity. Since biogas is the product of the fermentation of agriculture wastes, animal wastes and other sources of biomass, it consists of methane (CH₄), carbon dioxide (CO₂) and a small amount of oxygen, nitrogen and other organic compounds. Thanks to the various sources, the CO₂ content in the biogas varies between 40% and 80% generally. The considerable amount of inert CO₂ in the biogas leads to its lower heating value, decreased laminar flame speed and worse combustion stability. The real utilization of biogas is thus restricted considerably in industrial facilities [1,2]. Hydrogen (H₂), as a carbon-free gaseous fuel, has been widely accepted as an almost perfect clean energy and has a promising prospect in combustion engineering. Thanks to its high reactivity and diffusivity, hydrogen has the excellent mass-basis calorific value, the low minimum ignition energy, extensive flammability and the quite high flame propagation speed [3–6]. This makes the hydrogen to be an excellent addition to improve combustion characteristics of other hydrocarbon fuels, such as methane, propane and LPG [7–12]. Therefore, the hydrogen addition can also be adopted to improve the fuel characteristics of biogas and improve its practical applications.

To better utilize the biogas-hydrogen blends, effects of H₂ and CO₂ on the combustion features of biogas-hydrogen blends need to be studied thoroughly. In the past few decades, several researches have been conducted to improve the understandings of fuel characteristics of biogas-hydrogen blends. Leung et al. [13] reported that the stability range of the biogas diffusion flame can be improved effectively with a small amount of hydrogen addition. Chen and Zheng [14] performed the numerical simulations to study the mild combustion characteristics of biogas-hydrogen mixture and suggested that the lower preheated temperature is preferred for obtaining the stable mild combustion of biogas-hydrogen mixture. Zhang et al. [15] conducted an experiment to investigate the effects of hydrogen addition on the biogas combustion stability in a spark ignited engine and found that the hydrogen addition can enhance the heat release rate and improve the combustion stability of the biogas fuel. Hu et al. [16] reported that the increased hydrogen addition can increase the hydrodynamic and thermal mass diffusion instability in the biogas-hydrogen spherical flame. Zhang et al. [16] evaluated the fuel variability effects on the biogas-hydrogen combustion and suggested that the flame speed fluctuation

is caused by the hydrogen variability primarily. Wei et al. [17] conducted the experiment to analyze the effects of H₂ and CO₂ on the impingement heat transfer of the biogas-hydrogen flame and proposed an optimum hydrogen addition to improve the heat transfer of biogas-hydrogen impinging flame. Zhen et al. [18] investigated heat transfer and flame configurations of the hydrogen enriched biogas flame systematically. Zhen et al. [19] also performed an experimental study on the stability of biogas-hydrogen diffusion flame and reported that the hydrogen addition accelerates the fuel mass diffusion and improves the stability of biogas diffusion flame.

Besides, the heat release features [20], emission formations [21–23], explosion characteristics [24] and self-acceleration [25] of biogas-hydrogen combustion are studied by some researchers, while the combustion performance of biogas-hydrogen blends in the real combustors are investigated in plenty of studies [26–29]. The above mentioned studies provide quite a lot valuable information of the combustion features of biogas-hydrogen blends. Whereas, it is general that H₂ effects and CO₂ effects are investigated separately in the previous studies. Considering the simultaneous existence of H₂ and CO₂ in the biogas-hydrogen blend and their extremely different features to affect the combustion process, it is quite critical to identify the coupling effects of H₂ and CO₂ on the combustion characteristics of the biogas-hydrogen blend. This can help to obtain a deeper understanding on the combustion characteristics of biogas-hydrogen blends and further improve its practical applications. Hence, more studies need to be conducted to investigate the coupling effects of H₂ and CO₂ on the combustion features of biogas-hydrogen blend.

As one of most significant global combustion parameters, the laminar flame speed is not only quite pivotal for the development of the chemical mechanism and determination of turbulent burning velocity but also helpful for the design and optimization of combustion facilities. However, the laminar flame speed of biogas-hydrogen-air mixture are reported by few studies and the limited range of conditions are considered in these studies [30–34]. Furthermore, the coupling effects of H₂ and CO₂ on the laminar flame speed of biogas-hydrogen blends are rarely investigated. Considering the promising prospect of biogas-hydrogen blends and the significance of laminar flame speed on its real applications, there exists an urgent need to carry out the investigation on the coupling effects of H₂ and CO₂ on the laminar flame speed of the biogas-hydrogen blend. Based on our previous experimental work [33], the coupling effects of H₂ and CO₂ on the laminar flame speed will be further analyzed quantitatively with the numerical simulation in this study.

The objective of this research is to investigate the coupling effects of H₂ and CO₂ on the laminar flame speed of biogas-hydrogen blend. To better complete this objective, the

proportion of H₂ will keep the same with the CO₂ proportion and the proportions of H₂ and CO₂ will be varied simultaneously. Furthermore, dilution, thermal and chemical effects of H₂ and CO₂ will be isolated simultaneously to identify the dominating factor in the coupling effects of H₂ and CO₂. In addition, the change of reaction pathway will be investigated based on the rate of production (ROP) analysis, which can improve the understanding on the chemistry transition process from methane to the biogas-hydrogen blend when H₂ and CO₂ are added simultaneously.

Numerical methods

In this study, the biogas was emulated by mixing CH₄ and CO₂ according to the volumetric ratios of 80%: 20%, 60%: 40% and 40%: 60%, which are denoted as BG80, BG60 and BG40, respectively. In addition, the hydrogen addition is defined as $\alpha_{H_2} = V_{H_2}/(V_{CH_4} + V_{CO_2})$, where V_{H_2} , V_{CH_4} and V_{CO_2} are the mole fractions of hydrogen, methane and carbon dioxide, respectively. To better analyze the coupling effects of H₂ and CO₂, $\alpha_{H_2} = 20\%$, 40% and 60%, which are the same as the volumetric ratios of CO₂, were added into BG80, BG60 and BG40 respectively in the study, and the obtained biogas-hydrogen mixtures are denoted as BG80H20, BG60H40 and BG40H60, respectively. The details of the compositions of biogas-hydrogen mixtures used in this study are given in Table 1.

By using the PREMIX code [35] of CHEMKIN-II and the GRI 3.0 mechanism [36], the laminar flame speeds of CH₄ and biogas-hydrogen mixtures were calculated at 298 K and 1 atm under three equivalence ratios ($\phi = 0.9, 1.0$ and 1.1), and the multicomponent transport and Soret effect were both included in the model. The adaptive grid control on solution gradient (GRAD) and adaptive grid control on solution curvature (CURV) were set to 0.05 and 0.05, respectively. GRI 3.0, which consists of 53 species and 325 elementary chemical reactions, has been demonstrated to be an accurate detailed mechanism to describe the methane combustion by a few of experimental data. To confirm the accuracy of GRI 3.0 on the biogas-hydrogen mixture, the laminar flame speed measured by the cylindrical combustion bomb [33] are adopted here to compare the calculated results. The measured and calculated laminar flame speeds of biogas-hydrogen mixture are illustrated in Fig. 1. It is seen that the calculated results can agree well with the measured data, which indicates that GRI 3.0 can be used for the further investigation of combustion characteristics of biogas-hydrogen mixture.

In order to investigate the coupling effects of H₂ and CO₂ thoroughly, the dilution, thermal and chemical effects of H₂

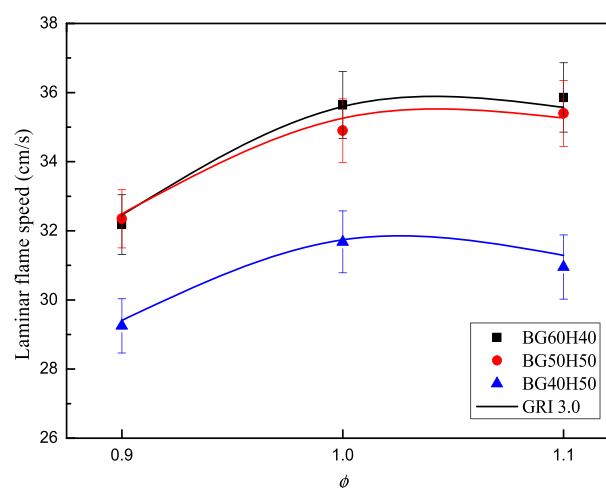


Fig. 1 – The comparison of calculated results and measured data of biogas-hydrogen flames.

and CO₂ were separated in the study by introducing the fictitious H₂ and CO₂, referred to FH₂ and FCO₂, respectively. FH₂ and FCO₂ have the same thermodynamic properties, transport properties and third-body collision efficiencies as the normal H₂ and CO₂, but they are not allowed to participate in any chemical reactions. To isolate the dilution, thermal and chemical effects of H₂ and CO₂, the CH₄, CH₄/N₂/N₂, CH₄/N₂/FH₂, CH₄/FCO₂/FH₂, CH₄/FCO₂/H₂ and CH₄/CO₂/H₂ were calculated successively at a condition. Based on these calculations, the difference between CH₄ and CH₄/N₂/N₂ is attributed to the coupling dilution effects of H₂ and CO₂ (Coupling D). The difference between CH₄/N₂/N₂ and CH₄/N₂/FH₂ is resulted from the thermal effects of H₂ (H2 T) while difference between CH₄/N₂/FH₂ and CH₄/FCO₂/FH₂ is ascribed to the thermal effects of CO₂ (CO2 T). Furthermore, the chemical effects of H₂ (H2 C) can be obtained by the difference between CH₄/FCO₂/FH₂ and CH₄/FCO₂/H₂ while the chemical effects of CO₂ (CO2 C) can be calculated by the difference between CH₄/FCO₂/H₂ and CH₄/CO₂/H₂. With these results, different effects of H₂ and CO₂ on the laminar flame speed can be investigated clearly, while the importance of different effects of H₂ and CO₂ can be also identified.

Results and discussions

Coupling effects on the laminar flame speed

The laminar flame speeds of biogas-hydrogen mixtures are compared with that of methane at $\phi = 0.9, 1.0$ and 1.1 as illustrated in Fig. 2. It is seen that, with the increased proportions of H₂ and CO₂, the laminar flame speeds of biogas-hydrogen mixture are decreased steadily from the methane to the BG60H40 mixture. However, with the further increased percentages of H₂ and CO₂, the laminar flame speed of BG40H60 mixture is increased considerably at the fuel-lean condition but still decreased slightly at the fuel-rich condition compared with that of BG60H40 mixture. Considering the variation of laminar flame speed, it seems that the increased CO₂ content contributes to the dropping trend of the laminar

Table 1 – The details of fuel compositions considered in this study.

	Mole fraction		
	CH ₄	CO ₂	H ₂
CH ₄	1	0	0
BG80H20	0.666	0.167	0.167
BG60H40	0.428	0.286	0.286
BG40H60	0.25	0.375	0.375

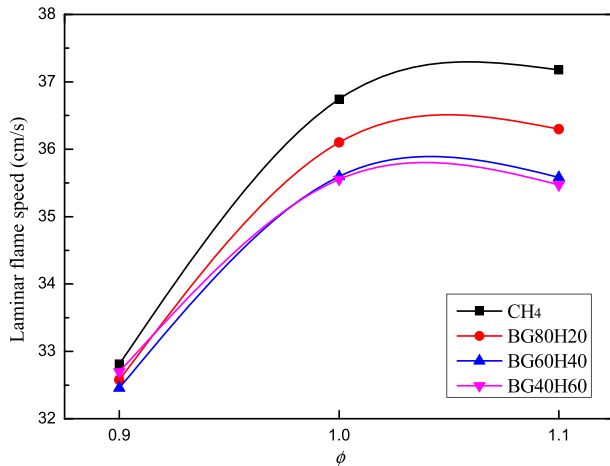


Fig. 2 – The laminar flame speeds of methane and biogas-hydrogen mixtures at $\phi = 0.9, 1.0$ and 1.1 .

flame speed firstly while the effects of H_2 will overcome the effects of CO_2 and reduce the dropping trend of laminar flame speed of the BG40H60 mixture.

To better investigate the coupling effects of H_2 and CO_2 , the variations of laminar flame speed caused by the coupling dilution effects of H_2 and CO_2 , and the respective thermal and chemical effects of H_2 and CO_2 are isolated and given in Fig. 3. As shown in Fig. 3, there is no surprise that the chemical effects of CO_2 decrease the laminar flame speed while the chemical effects of H_2 can increase the laminar flame speed quite efficiently. In addition, it is seen that the thermal effects of CO_2 can affect the laminar flame speed more evidently than that of H_2 owing to its much larger specific heat capacity which decreases the flame temperature. Thus the H_2 reactivity dominates the coupling chemical effects while the thermal properties of CO_2 give rise to its more significant role in the coupling thermal effects. In addition, the coupling dilution effects of H_2 and CO_2 play the most important role in the decrease of laminar flame speed of biogas-hydrogen mixture. Besides, it is seen that the dilution, thermal and

chemical effects of H_2 and CO_2 are increased considerably with their increased proportions, while H_2 and CO_2 can exert more evident influences on the laminar flame speed at the fuel-rich condition than that at the fuel-lean condition thanks to their higher proportions in the unburned gases mixture. Overall, it is known that the coupling dilution effects of H_2 and CO_2 dominate the decrease of laminar flame speed with the increased proportions of H_2 and CO_2 , while the chemical effects of H_2 play the critical role in the increase of laminar flame speed.

The laminar flame speed variation is normalized by the sum of the absolute values of laminar flame speed variations caused by different effects at a condition, which can compare the relative importance of dilution, thermal and chemical effects of H_2 and CO_2 at different conditions clearly. The obtained results are shown in Fig. 4. With the increased H_2 and CO_2 contents, the contribution of CO_2 chemical effect is decreased while that of H_2 chemical effect is increased at either the fuel-lean or the fuel-rich condition. In addition, the thermal effects of H_2 and CO_2 both become less important in the variation of laminar flame speed while the significance of coupling dilution effects of H_2 and CO_2 is enhanced from CH_4 to BG40H60. Besides, it is noted that the contributions of CO_2 chemical effects are increased by around 30% at the fuel-rich condition compared with that at the fuel-lean condition while the contributions of other factors are decreased slightly at the fuel-rich condition. Hence, compared with that at $\phi = 0.9$, CO_2 chemical effects play the more significant role in the laminar flame speed at $\phi = 1.1$ as shown in Fig. 4.

The total contributions of positive (thermal and chemical effects of H_2) and negative (thermal and chemical effects of CO_2 and coupling dilution effects) effects on the laminar flame speed are shown in Fig. 5. It is seen that the negative effects account for more than 50% of coupling effects of H_2 and CO_2 on the laminar flame speed, which means that the negative effects of H_2 and CO_2 dominate the variation of laminar flame speed of the biogas-hydrogen mixture and result in the dropping trend of laminar flame speed from CH_4 to biogas-hydrogen mixture as shown in Fig. 2. In addition, it is noted that the contribution of positive effects of H_2 and CO_2 suffer

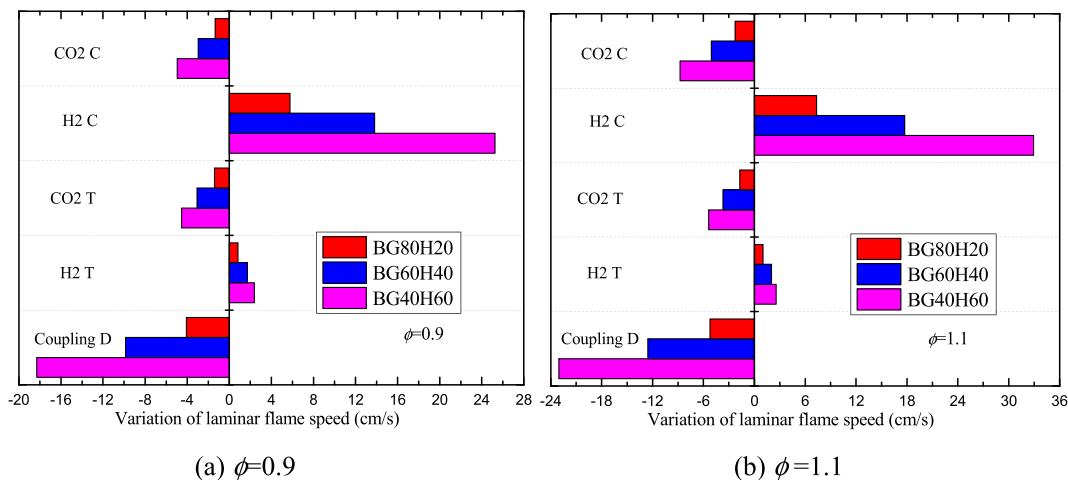


Fig. 3 – The coupling dilution effect and respective thermal/chemical effects of H_2 and CO_2 on laminar flame speeds of biogas-hydrogen mixtures at $\phi = 0.9$ and 1.1 .

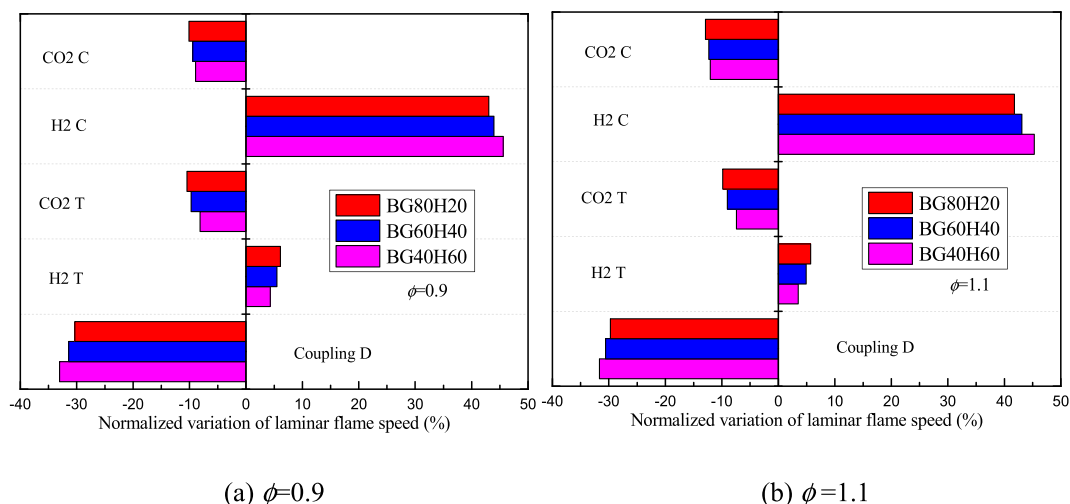


Fig. 4 – The contributions of different effects of H₂ and CO₂ on laminar flame speeds of biogas-hydrogen mixtures at $\phi = 0.9$ and 1.1.

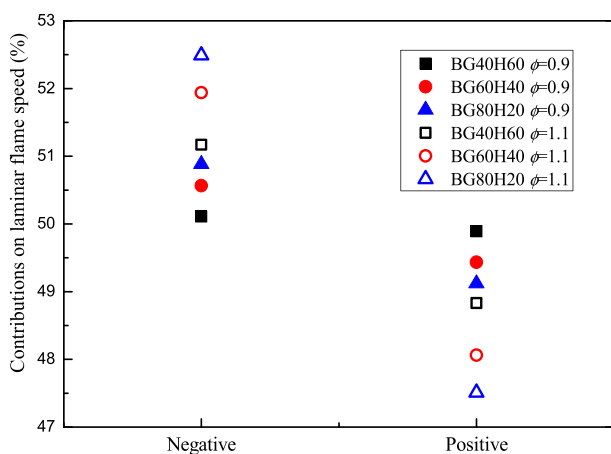


Fig. 5 – The total negative and positive effects of H₂ and CO₂ on laminar flame speeds of biogas-hydrogen mixtures at $\phi = 0.9$ and 1.1.

the more evident increase from BG60H40 to BG40H60 compared with that from BG80H20 to BG60H40 at $\phi = 0.9$ and 1.1 as shown in Fig. 5. This indicates that the positive effects of H₂ and CO₂ are improved more effectively than the negative effects in the BG40H60 mixture. Furthermore, the contribution of H₂ thermal effects is decreased with the increased H₂ and CO₂ as shown in Fig. 4, the more efficient improvements of positive effects in the BG40H60 flame are thus resulted from the more effectively increased contribution of H₂ chemical effects. This finally leads to the considerably reduced dropping rate of laminar flame speed from BG60H40 to BG40H60.

Besides, it is apparent that, as shown in Fig. 5, the negative effects of H₂ and CO₂ at the fuel-rich condition can be approximately 1%–1.5% higher than that at the fuel-lean condition. Considering the contributions of thermal/chemical effects of CO₂ and coupling dilution effects shown in Fig. 4, it is known that the higher contributions of CO₂ chemical effects bring about the increased negative effects at the fuel-rich condition. Consequently, compared with that at the fuel-lean

condition, the much stronger CO₂ chemical effects at the fuel-rich condition give rise to the more evident decrease of laminar flame speed at $\phi = 1.1$ than that at $\phi = 0.9$ as shown in Fig. 2. In addition, combined with the more obvious improvements on the positive effects from BG60H40 to BG40H60, the stronger negative effects at the fuel-rich condition contribute to the slight decrease of laminar flame speed from BG60H40 to BG40H60 at $\phi = 1.1$ but the moderate increase at $\phi = 0.9$ as shown in Fig. 2.

Overall, it is concluded that the lower laminar flame speed of biogas-hydrogen mixture is dominated by the increased contribution of coupling dilution effects of H₂ and CO₂, while the more evident dropping trend of laminar flame speed at $\phi = 1.1$ is ascribed to the stronger suppressions caused by CO₂ chemical effects. From BG60H40 to BG40H60, the reduced dropping trend of laminar flame speed is attributed to the more evidently increased contribution of H₂ chemical effect, while the lower contribution of CO₂ chemical effects at the fuel-lean condition further result in the increased laminar flame speed at $\phi = 0.9$ as shown in Fig. 2.

Coupling effects on the radical pool

The radical pool has the close relationship with the laminar flame speed that can be used to further clarify the reasons of the laminar flame speed variation. The radical pool of the methane flames and biogas-hydrogen flames are plotted in Fig. 6. As shown in Fig. 6, OH radical is the most abundant radical in the radical pool at the fuel-lean condition while H radical is more significant at the fuel-rich condition. In addition, the peak mole fractions of H, O, OH and CH₃ are decreased generally from CH₄ to BG40H60. It is noted that the H radical can be an indicator of the laminar flame speed of the biogas-hydrogen mixture because its peak mole fraction can reflect the variation of laminar flame speed reasonably. Specifically, the peak mole fraction of H radical shows a quite moderate dropping trend at the fuel-lean condition compared with that at the fuel-rich condition as shown in Fig. 6. Furthermore, the peak mole fraction of H radical is increased

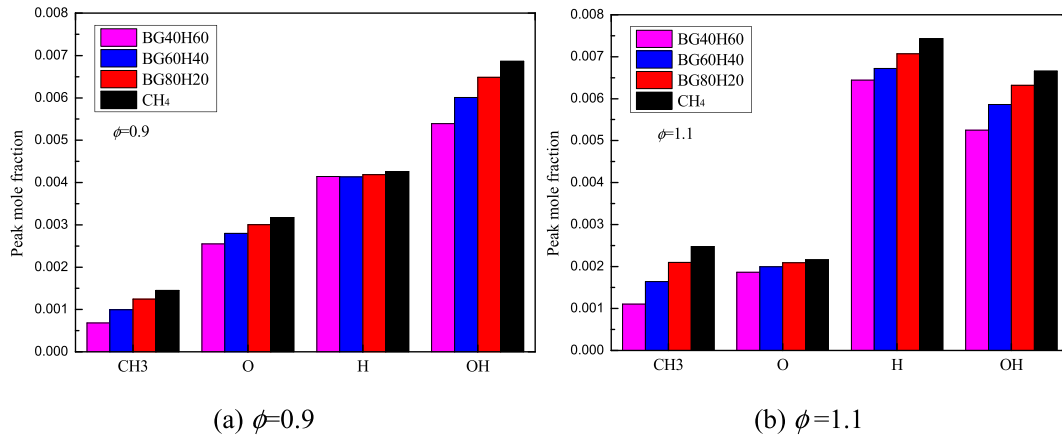


Fig. 6 – The radical pool (H, O, OH and CH₃) in the methane flames and biogas-hydrogen flames at $\phi = 0.9$ and 1.1.

slightly from 4.13×10^{-3} in the BG60H40 flame to 4.14×10^{-3} in the BG40H60 flame at $\phi = 0.9$ while its dropping trend becomes comparatively moderate from BG60H40 to BG40H60 at $\phi = 1.1$. Hence, the variations of H radical are consistent with the variations of laminar flame speed at $\phi = 0.9$ and 1.1 as shown in Fig. 2, which indicates that H radical should play the dominated role in the laminar flame speed of biogas-hydrogen flame. In addition, the considerably decreased CH₃ mole fraction indicates the weakened CH₄ chemistry [37].

To identify the different effects of H₂ and CO₂ on the H radical in the biogas-hydrogen flame, the peak mole fraction variations of H radical caused by the different effects of H₂ and CO₂ in the biogas-hydrogen mixture are illustrated in Fig. 7, while the contributions of different effects of H₂ and CO₂ on the H radical variation are shown in Fig. 8. As shown in Fig. 7, the peak mole fraction variation of H radical can be increased effectively with the increased percentages of H₂ and CO₂. However, the contributions of H₂ chemical effects and coupling dilution effects are increased from BG80H20 to BG40H60 while the contributions of other effects are decreased as shown in Fig. 8. In addition, it is seen that the contributions of CO₂ chemical effects on the H radical variation are higher at $\phi = 1.1$ than that at $\phi = 0.9$. It is thus

confirmed that the slightly increased peak mole fraction of H radical from BG60H40 to BG40H60 at $\phi = 0.9$ can be attributed to the enhanced contribution of H₂ chemical effects while the steady decrease of peak mole fraction of H radical at $\phi = 1.1$ is dominated by the higher importance of CO₂ chemical effects at the fuel-rich condition.

The primary reactions to produce and consume the H radical in the CH₄ and BG40H60 flames are illustrated in Fig. 9 in order to further clarify the roles of H₂ and CO₂ in the variation of the H radical. In the methane and biogas-hydrogen flames, the primary reactions to produce the H radical are R84: OH + H₂ = H₂O + H, R3: O + H₂ = H + OH, R99: OH + CO = H + CO₂ and R10: O + CH₃ = H + CH₂O, while the major reactions to consume the H radical are R38: H + O₂ = OH + O, R52: H + CH₃(+M) = CH₄(+M), R53: H + CH₄ = CH₃ + H₂ and R58: H + CH₂O = HCO + H₂. Furthermore, R84 and R38 are the most important reactions to produce and consume the H radical respectively at both fuel-lean and fuel-rich conditions. In addition, as shown in Fig. 9, the difference between the ROPs of CH₄ and CH₄/FCO₂/FH₂ is ascribed to the thermal and dilution effects of H₂ and CO₂. The difference between the ROPs of CH₄/FCO₂/FH₂ and CH₄/FCO₂/H₂ is resulted from the H₂ chemical effects while the difference between the ROPs of

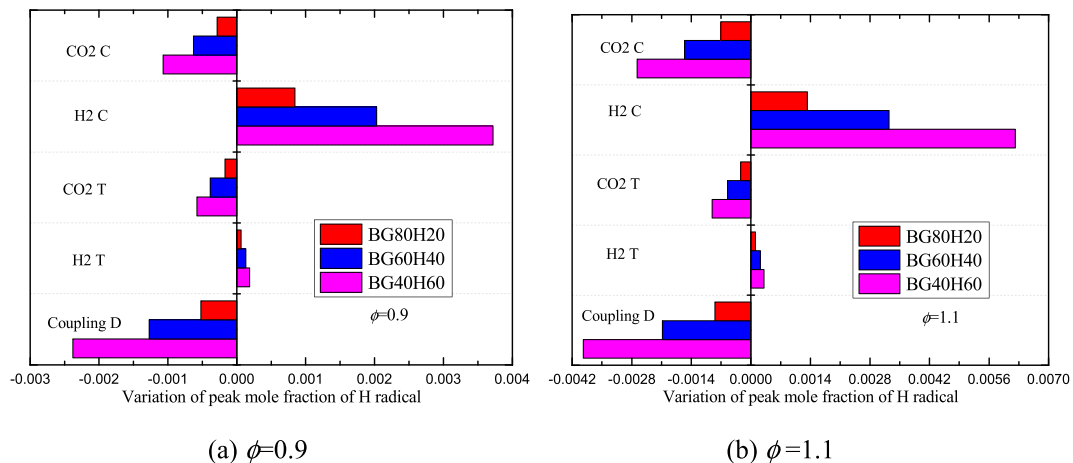


Fig. 7 – The coupling dilution effect and respective thermal/chemical effects of H₂ and CO₂ on the H radical of biogas-hydrogen mixtures at $\phi = 0.9$ and 1.1.

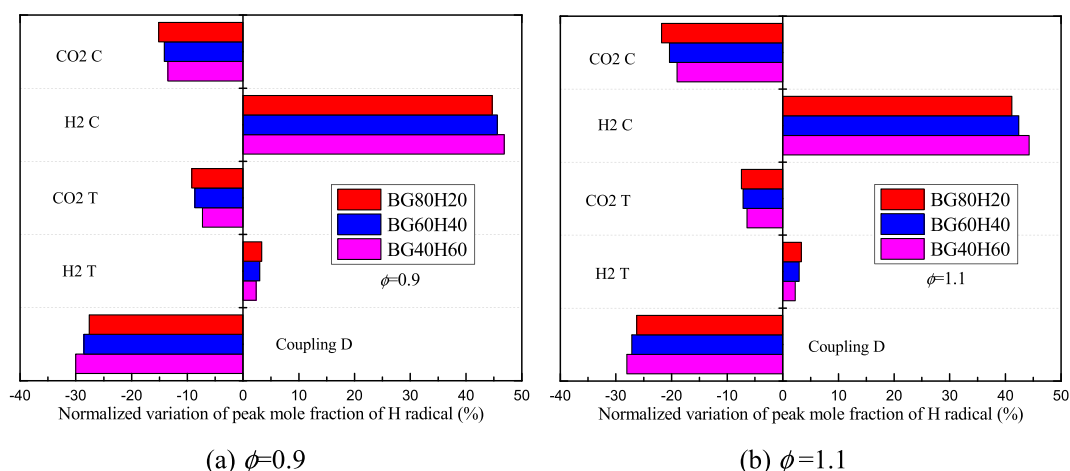


Fig. 8 – The contributions of different effects of H₂ and CO₂ on the H radical of biogas-hydrogen mixtures at $\phi = 0.9$ and 1.1.

CH₄/FCO₂/H₂ and BG40H60 is attributed to the CO₂ chemical effects. It is thus known that, as shown in Fig. 9, the coupling dilution and thermal effects of H₂ and CO₂ lead to the considerable decrease in ROPs of H radical for all major reactions thanks to the considerably decreased temperature and reduced active radicals. The coupling dilution effects of H₂ and CO₂ consequently contribute to the considerably decreased H radical in the radical pool and then suppress the flame propagation effectively.

As the H₂ chemical effects are introduced, the ROPs of H radical via these reactions are all improved effectively. Whereas, it is noted that the ROPs of R84, R3 and R52 are enhanced drastically in the CH₄/FCO₂/H₂ flame which are even higher than that in the CH₄ flame, while ROPs of R10, R53, R58 and R99 are still lower than that in the CH₄ flame as shown in Fig. 9. Besides, it is seen that, compared with that in the CH₄ flame, the H₂ chemical effects lead to the slightly lower ROP of R38 in the CH₄/FCO₂/H₂ flame at the fuel-lean condition but the higher ROP at the fuel-rich condition. With the introduced H₂ chemical effects, R84 and R38 can be improved considerably by the high reactivity of H₂ which can increase the amount of H, O and OH radicals considerably. This can then accelerate other reactions effectively and enhance the heat release rate of biogas-hydrogen combustion [20], which gives rise to the enhancements of ROPs of these reactions as shown in Fig. 9. Additionally, the quite evident improvements on the ROP of R84 and R3 are caused by the obviously increased amount of H₂ in the mixture and its direct participations in these two reactions. For R52, it is a three-body reaction which can be affected drastically by the concentrations of H, CH₃ and the third-body amount in the flame. The considerably increased H radical and the large amounts of the third-body (H₂, CO₂, H₂O, etc.) in the CH₄/FCO₂/H₂ flame can thus accelerate the R52 efficiently by the enhanced collision efficiency, which then brings about its higher ROP of H radical than that of CH₄ flame. Besides, the ROP of R38 in the CH₄/FCO₂/H₂ flame is slightly lower than that in the CH₄ flame at fuel-lean condition thanks to the abundant O₂ in the mixture while its ROP becomes moderately higher at the fuel-rich condition which can be ascribed to the quite higher concentration of H radical. Considering the more improvements on R84, R3 and R52, it is

known that these three reactions play the more important roles in the H radical pool variation caused by the H₂ chemical effects. Although the higher ROP of R52 can accelerate the consumption of H radical in the flame, its consumption rate is much lower than the production rate of R84 and cannot overcome the improvements of R84 on the H radical production. As a result, the considerably improved R84 and R3 dominate the increased H radical with the H₂ chemical effects.

As the CO₂ chemical effects are further introduced, the ROPs of these reactions are decreased effectively in the BG40H60 flame at both the fuel-lean and the fuel-rich condition as shown Fig. 9. It is known that the CO₂ chemical effects can accelerate the reverse reaction of R99 directly, which can compete for the H radical with R38 significantly and then suppress this most significant chain-branching reaction in the biogas-hydrogen combustion [38,39]. In addition, R99 is an important exothermic reaction in the biogas-hydrogen mixture [20]. The CO₂ chemical effects can suppress the forward reaction of R99 and then decrease the heat release rate of the biogas-hydrogen combustion, which leads to the declined temperature in the reaction zone [40]. Hence, the suppressed chain-branching reaction and declined temperature caused by the CO₂ chemical effects can suppress the H radical production considerably. Furthermore, the importance of R52 on the H radical pool is increased in the biogas-hydrogen flame considering that its ROP is higher than that in the CH₄ flame while ROPs of other major H radical consumption reactions are lower than that in the CH₄ flame. The increased importance of R52 can be ascribed to the obvious improvements of H₂ chemical effects. As a result, with the CO₂ chemical effects, the suppressed H radical production and the increased contribution of R52 contribute to the decreased H radical with the CO₂ chemical effects.

Besides, thanks to the coupling chemical effects of H₂ and CO₂, the ROPs of R84 and R52 in the BG40H60 flame become higher than that in the CH₄ flame while the ROP of R3 in the BG40H60 flame is higher at the fuel-lean condition but slightly lower at the fuel-rich condition than that in the CH₄ flame as shown Fig. 9. For other reactions, their ROPs in the BG40H60 flame are quite lower than that in the CH₄ flame due to the coupling effects of H₂ and CO₂. It is thus known that the

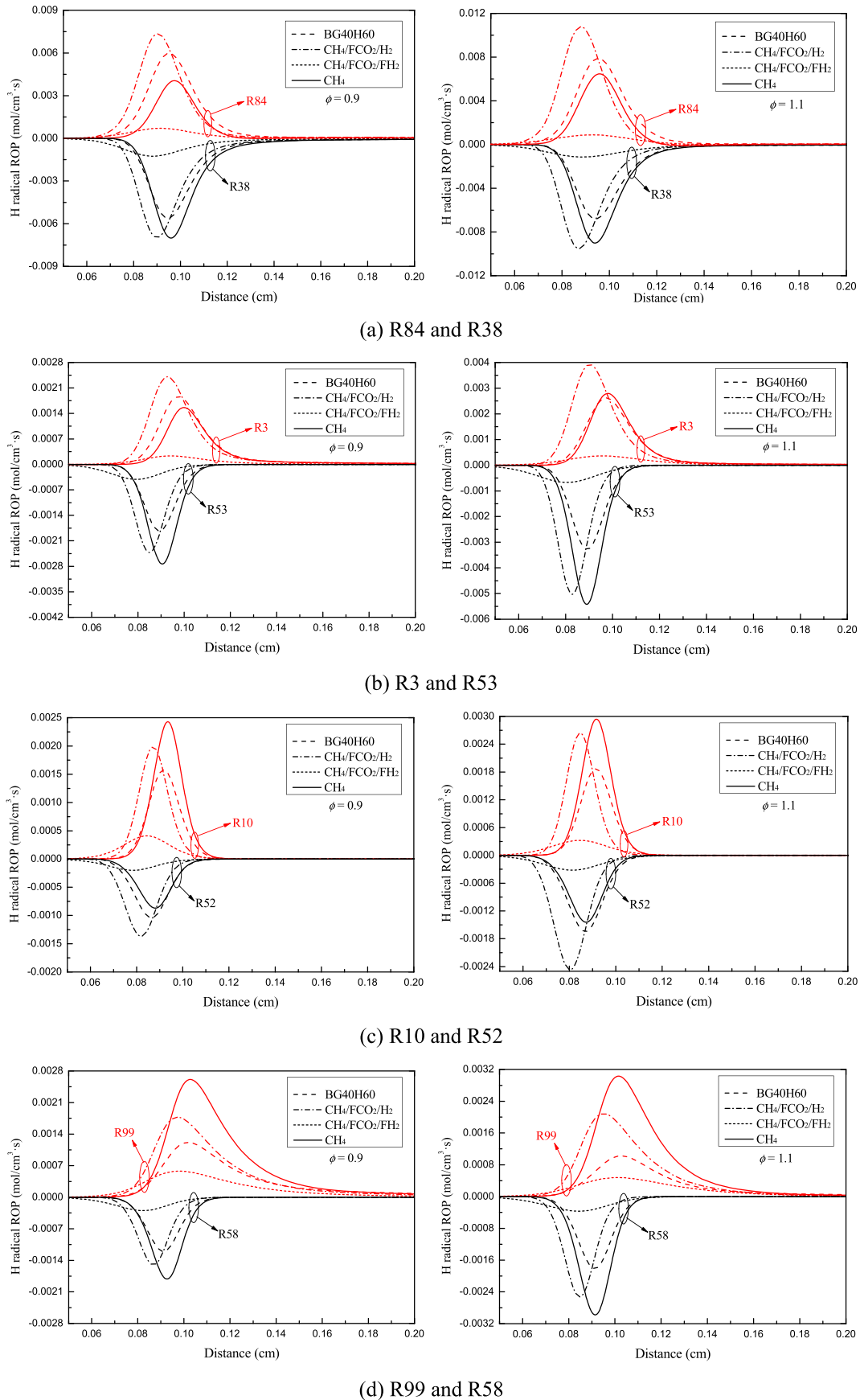


Fig. 9 – The effects of H₂ and CO₂ on the ROP of H radical in the biogas-hydrogen flames at $\phi = 0.9$ and 1.1.

significances of R84, R3 and R52 on the H radical pool are increased effectively in the biogas-hydrogen flames. R84 and R3 are the H radical production reactions while R52 is the H radical consumption reaction. Considering the ROPs of these reactions, the increased contributions of R84, R3 and R52 means that the positive effects on the H radical pool are improved more effectively than that of negative effects. This consequently contributes to the reduced dropping trend of H radical and laminar flame speed from BG60H40 to BG40H60. Overall, it is known that the H₂ chemical effects dominate the reduced dropping trend of H radical primarily through R84 and R3, which finally leads to the moderate variation of laminar flame speed from BG60H40 to BG40H60 as shown in Fig. 2.

Apart from this, it is noted that CO₂ chemical effects exert more apparent suppressions on the ROPs of these reactions at the fuel-rich condition than that at the fuel-lean condition as shown Fig. 9, which could be attributed to the higher CO₂ concentration at the fuel-rich condition. For example, from CH₄/FCO₂/H₂ to BG40H60, the peak ROPs of R84, R3, R38 and R53 are decreased by around 18.6%, 22.8%, 19.5% and 24.4% respectively at the fuel-lean condition due to the CO₂ chemical effects while they are decreased by approximately 27.0%, 33.2%, 28.6% and 35.0% respectively at the fuel-rich condition. For the H radical production, the more evident suppressions of CO₂ chemical effects on the major H radical production reactions (R84, R3, R99 and R10) at the fuel-rich condition can suppress the H radical production more effectively than that at the fuel-lean condition, which can give rise to the decreased concentration of H radical in the flame. In addition, for the H radical consumption reactions, their ROPs are also decreased considerably with the CO₂ chemical effects owing to the direct competition with the large amount of CO₂ in the flame for the H radical. Furthermore, with the stronger CO₂ chemical effects at the fuel-rich condition, the peak ROPs of R53, R52 and R58 are decreased more evidently than that at the fuel-lean condition, which seems to decelerate the consumption of H radical at the fuel-rich condition. Whereas, it is noted that R53, R52 and R58 can play the more significant roles in the H radical consumption at the fuel-rich condition than that at the fuel-lean condition as shown in Fig. 9. Hence, R53, R52 and R58 can still consume the H radical more efficiently at the fuel-rich condition in consideration of their higher contributions on the H radical consumption at fuel-rich condition. This can lead to the more effective consumption of H radical in the BG40H60 flame at the fuel-rich condition than that at the fuel-lean condition. As a result, thanks to the more effective suppressions on the H radical production caused by the more evident CO₂ chemical effects and the more effective H radical consumption due to the increased contributions of the major consumption reactions of H radical, H radical is reduced more evidently at the fuel-rich condition as illustrated in Fig. 6, which then results in the obviously decreased laminar flame speed from CH₄ to BG40H60 at $\phi = 1.1$ as shown in Fig. 2.

Coupling effects on the reaction pathways

In order to further reveal the coupling effects of H₂ and CO₂, main reaction pathways of CH₄ and biogas-hydrogen flames are investigated based on the ROP analysis and results are illustrated in Fig. 10. In the figure, the black arrows denote the

primary pathways of CH₄ chemistry while the blue arrows indicate the weakened pathways of CH₄ chemistry in the biogas-hydrogen flame. The major pathways of H₂ chemistry are presented with the red arrows. In addition, CO₂ chemistry is represented by the dash arrow considering that R99 still proceeds in its forward direction in the biogas-hydrogen flame even though the added CO₂ can improve the reverse reaction of R99 considerably. Besides, the pathways whose importance are increased drastically in the biogas-hydrogen flames are highlighted with the red boxes while the pathways with the drastically decreased contributions are highlighted with blue boxes.

In both CH₄ and biogas-hydrogen flames, methane is primarily consumed via the H-abstraction reactions by OH, O and H (R98: OH + CH₄) = CH₃+H₂O, R11: O + CH₄) = CH₃+OH and R53) to generate the CH₃ radical. In the CH₄ flame, CH₃ radical is mainly consumed via R10, R97: OH + CH₃) = CH₂(S)+H₂O, R284: O + CH₃) = H + H₂+CO, R158: 2CH₃(+M) = C₂H₆(+M) and R52. Among these reactions, R10, R97 and R284 have the higher contributions on the CH₃ radical consumption at the fuel-lean condition while the significances of R158 and R52 are enhanced at the fuel-rich condition. With the increased amounts of H₂ and CO₂, R10 and R284 still have the stable contributions on the CH₃ consumption in the biogas-hydrogen flames while R97 becomes less important. In addition, the contribution of R52 is enhanced by around 80%, which is resulted from the enhanced collision efficiency by the drastically third-body amount in the flame. As a termination reaction, the increased importance of R52 on the CH₃ radical consumption indicates that the CH₄ consumption is suppressed more effectively with the increased amounts of H₂ and CO₂, which can consequently suppress the flame propagation. The contribution of R158 can reflect the importance of the C₂ pathways in the flame. With the increased H₂ and CO₂ contents, R158 becomes much less important with its contribution dropped by about 40%. This indicates the increasingly important role of the H₂/CO₂-related chemistry in the biogas-hydrogen flame.

Formaldehyde (CH₂O) is primarily produced via R10, which then generate the HCO radical primarily by R101: OH + CH₂O) = HCO + H₂O and R58 in both methane and biogas-hydrogen flames. HCO radical can be consumed via various reactions as shown in Fig. 10. In either methane or biogas-hydrogen flame, more than 80% of HCO radical can be consumed via R166: HCO + H₂O) = H + CO + H₂O, R167: HCO + M) = H + CO + M and R168: HCO + O₂) = CO + HO₂. R168 plays a more important role at the fuel-lean condition due to the abundant O₂ while the contributions of R167 and R166 are increased at the fuel-rich condition owing to the improved collision efficiency. In addition, with the increased contents of H₂ and CO₂, R168 and R55: HCO + H) = CO + H₂ have the increased contributions on the HCO radical consumption while the contributions of R166 and R167 are declined steadily. In the biogas-hydrogen flames, CO is still primarily consumed by OH radical via R99. However, the consumption rate of CO is decreased considerably than that in the methane flame owing to the reduced CH₄ and the increased CO₂ in the flame, which can be reflected by the considerably reduced net reaction rate of R99 as shown in Fig. 11.

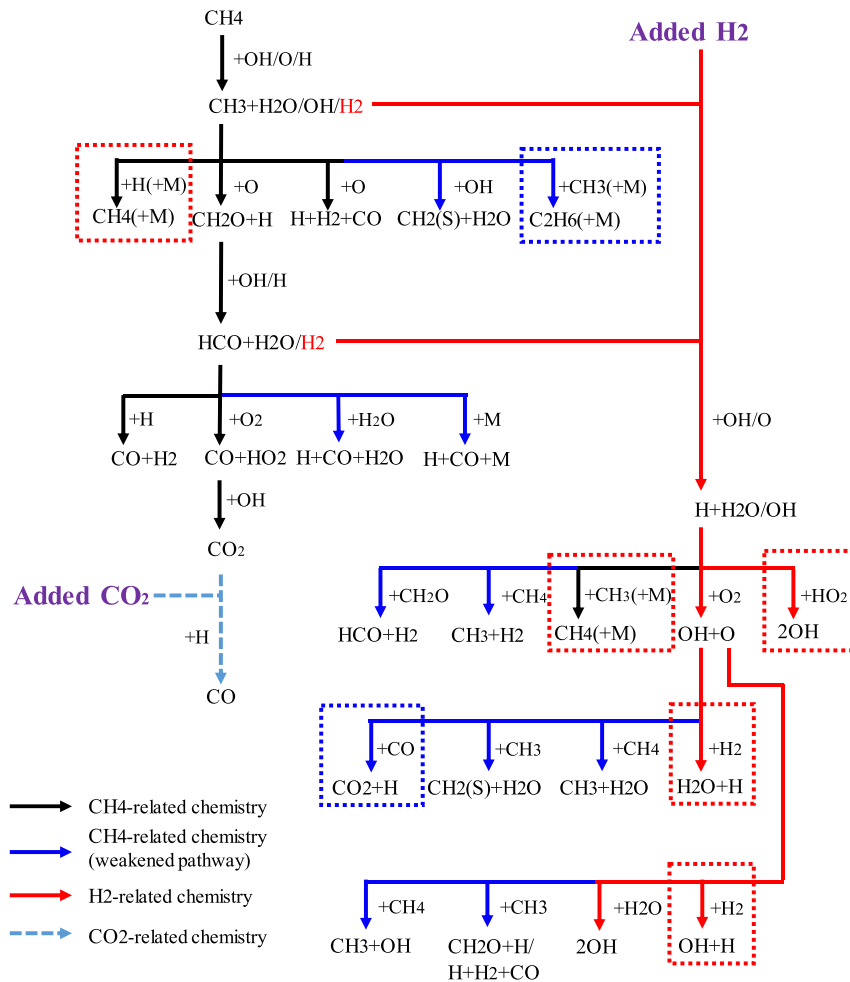


Fig. 10 – Reaction network based on the ROP analysis in the CH₄ and biogas-hydrogen flames.

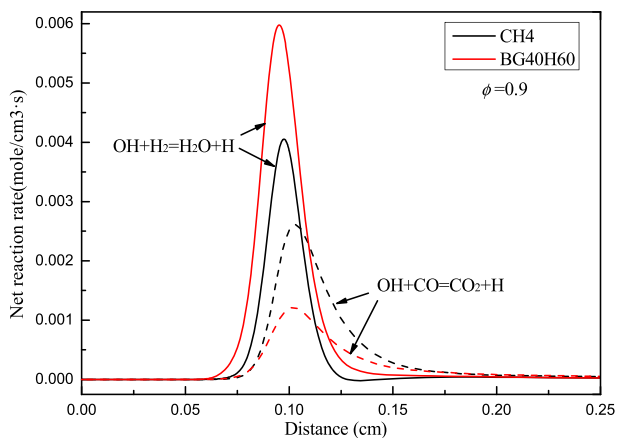


Fig. 11 – Net reaction rates of R84 and R99 in the CH₄ and biogas-hydrogen flames.

H₂ can be produced primarily via R53 and R58 in the methane flame, which is marked with the red font in Fig. 10. Meanwhile, the added H₂ is presented with the purple bold font in Fig. 10. For the H₂, it is primarily consumed by OH and O radicals via R84 and R3 in the methane and biogas-hydrogen

flames. R84 is the most important reaction to produce the H radical while R3 is an important chain-branching reaction in the flame. These two reactions can be improved with the increased H₂ and CO₂, which can then make for the flame propagation. H radical can be consumed via various reactions due to its critical role in the flame propagation. In both methane and biogas-hydrogen flame, R38 can account for the largest part of H radical consumption. With the increased contents of H₂ and CO₂, the contributions of R53 and R58 are declined due to reduced CH₄, while the importance of R52 is increased effectively. R53 and R58 are the major reactions to consume H radical in the CH₄ flame, and their declined contributions imply the weakened CH₄-related chemistry. Besides, the increased contribution of R52 further indicates its suppressions on the flame propagation, which confirms its dominated role in the decrease of laminar flame speed of the biogas-hydrogen mixture [33]. By contrast, the contribution of R46: H + HO₂ = 2OH is increased by more than 80% in the biogas-hydrogen flame, which implies the increasingly significant role of H₂-related chemistry.

OH radical is primarily generated via R38 and then reacts with CH₄, CH₃, H₂ and CO primarily to form H₂O and CO₂ in the methane flame. In the biogas-hydrogen flame, the contribution of R84 on the OH radical consumption is enhanced drastically

while that of R97, R98 and R99 are decreased due to the weakened CH₄-related chemistry. For the OH radical consumption, the considerably increased contribution of R84 and drastically decreased contribution of R99 in the biogas-hydrogen flame are highlighted in the red box and blue box respectively as shown in Fig. 10. As the primary oxidization reactions of H₂ and CO, it is general that the net reaction rates of R84 and R99 are enhanced simultaneously with the H₂ addition but decreased simultaneously with the CO₂ addition. Whereas, with the coupling effects of H₂ and CO₂, the net reaction rate of R84 is increased while that of R99 is decreased as shown in Fig. 11. Thanks to the high reactivity and diffusivity of H₂, the increased H₂ concentration leads to the higher flame temperature and the increased amounts of active radicals, which gives rise to the evidently enhanced net reaction rate of R84 and contributes to the improved R99. However, as the same amount of CO₂ is introduced, the reactivity of CO₂ can improve the backward reaction of R99 effectively, which can then overcome the improvements of H₂ and decrease the net reaction rate of R99 finally. In addition, less CO is produced in the biogas-hydrogen flame due to the reduced CH₄ and it needs to compete with H₂ for the OH radical, which can also decelerate the forward reaction of R99 effectively. As a result, the net reaction rate of R99 is decreased considerably with the coupling effects of H₂ and CO₂ as shown in Fig. 11. R84 and R99 can be thus seen as the indicators for the increased importance of H₂/CO₂-related chemistry in the biogas-hydrogen flame.

For the O radical, it is mainly consumed via R3, R10, R11, R86: $O + H_2O = 2OH$ and R284 in the methane and biogas-hydrogen flames. With the increased contents of H₂ and CO₂, the importance of R10, R11 and R284 are decreased owing to the reduced CH₄ concentration while the contribution of R3 is enhanced effectively. This also implies the more important role of H₂-related chemistry in the flame. Overall, it is known that the decreased contributions of R158 and R99 indicate the weakened CH₄-related chemistry while R3, R46, R52 and R84 can be seen as the indicator of improved H₂-related chemistry in the biogas-hydrogen flame. Furthermore, coupling effects of H₂ and CO₂ can be monitored directly by the contribution variations of R84 and R99 on the OH radical.

Conclusions

The coupling effects of H₂ and CO₂ on the laminar flame speed and reaction pathways of the biogas-hydrogen mixtures were analyzed using the chemical kinetics simulations. The coupling dilution effects, chemical effects and thermal effects of H₂ and CO₂ were isolated respectively at fuel-lean and fuel-rich conditions in the simulation. The contributions of different effects of H₂ and CO₂ were calculated to identify the dominating factor. The results are summarized as follows:

1. The lower laminar flame speed of biogas-hydrogen mixture is dominated by the coupling dilution effects of H₂ and CO₂, and the more evident dropping trend at the fuel-rich condition is resulted from the more suppressions of CO₂ chemical effects. Furthermore, combined with the stronger suppressions of CO₂ chemical effects at the fuel-rich condition, the more evidently improvements of H₂

chemical effects give rise to the increased and decreased laminar flame speed from BG60H40 to BG40H60 at $\phi = 0.9$ and 1.1, respectively.

2. The variation of laminar flame speed is determined by the variation of H radical in the biogas-hydrogen flame. The coupling dilution effects of H₂ and CO₂ can lead to the considerable decrease in ROP of H radical for all major reactions thanks to the considerably decreased temperature and reduced active radicals. The H₂ chemical effects improve R84 and R3 more effectively, which makes for the more efficient H radical production and increased H radical pool. With the CO₂ chemical effects, the major H radical production reactions of R84, R3, R99 and R10 are suppressed, while R52 plays the more important role in the H radical pool owing to the coupling chemical effects of H₂ and CO₂. This results in the decrease of H radical with the CO₂ chemical effects.
3. Based on the ROP analysis of H radical, it is found that the reduced dropping trends of H radical and laminar flame speed from BG60H40 to BG40H60 are attributed to considerably improved R84 and R3 caused by H₂ chemical effects. Besides, with the stronger CO₂ chemical effects at the fuel-rich condition, the more obviously suppressed H radical production reactions and the higher contributions of consumption reactions (R53, R52 and R58) on the H radical pool codetermine the more evident decrease of H radical pool in the biogas-hydrogen flame at the fuel-rich condition than that at the fuel-lean condition.
4. Based on the ROP analysis, R3, R46, R52, R84, R99 and R158 have the primary contributions on the chemistry transition caused by the coupling effects of H₂ and CO₂. The decreased contribution of R158 and R99 indicate the weakened CH₄-related chemistry while the increased contributions of R3, R46, R52 and R84 mean the improved H₂-related chemistry in the biogas-hydrogen flame. Furthermore, the H₂/CO₂-related chemistry can be monitored directly by the contribution variations of R84 and R99 on the OH radical.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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