

# Microwave dielectric properties of temperature-stable zircon-type (Bi, Ce)VO<sub>4</sub> solid solution ceramics

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## Abstract

In the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> (0 ≤ x ≤ 1) system, we found that the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> (0 ≤ x ≤ 0.1) belongs to the monoclinic scheelite phase and the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> (0.7 ≤ x ≤ 1) belongs to the tetragonal zircon phase, while the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> (0.1 < x < 0.7) belongs to the mixed phases of both monoclinic scheelite and tetragonal zircon structure. Interestingly, two components with near-zero temperature coefficient of resonant frequency (TCF) appeared in this system. In our previous work, a near-zero TCF of ~+15 ppm/°C was obtained in a (Bi<sub>0.75</sub>Ce<sub>0.25</sub>)VO<sub>4</sub> ceramic with a permittivity (ε<sub>r</sub>) of ~47.9 and a Qf (Q = quality factor = 1/dielectric loss; f = resonant frequency) value of ~18 000 GHz (at 7.6 GHz). Furthermore, in the present work, another temperature-stable microwave dielectric ceramic was obtained in (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> composition sintered at 950°C and exhibits good microwave dielectric properties with a ε<sub>r</sub> of ~11.9, a Qf of ~22 360 GHz (at 10.6 GHz), and a near-zero TCF of ~+6.6 ppm/°C. The results indicate that this system might be an interesting candidate for microwave device applications.

## KEYWORDS

dielectric properties, low temperature, solid solutions, X-ray methods

## 1 | INTRODUCTION

Microwave dielectric materials play a key role in global society, with a wide range of applications straddling terrestrial and satellite communications, including Internet of Things (IoT), software radio, GPS, DBS TV, environmental monitoring via satellite, etc. The temperature coefficient of resonance

frequency (TCF) is one of the important parameters of microwave dielectric ceramics. The dielectric resonator generally uses the frequency of a certain vibration mode of dielectric ceramic as its center frequency. Therefore, in order to eliminate the temperature drift of the resonant frequency characteristic of the resonator, it is necessary to make the TCF close to zero.<sup>1-7</sup>

In 2000, Valant and Suvorov<sup>8</sup> first reported that BiVO<sub>4</sub> ceramic not only sinter at a low temperature (<900°C) but also exhibit excellent microwave dielectric properties, with a permittivity ( $\epsilon_r$ ) of ~68, a Qf (Q = quality factor = 1/dielectric loss; f = resonant frequency) value of ~6500 GHz, and a negative TCF of ~-260 ppm/°C. However, the large negative TCF will limit its application in microwave devices, thus, further studies to adjust the TCF of BiVO<sub>4</sub> ceramic to near zero are of great interest. In our previous work,<sup>9</sup> the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $x \leq 0.6$ ) ceramics were prepared via a solid-state reaction method and a near-zero TCF (+15 ppm/°C) was obtained in a (Bi<sub>0.75</sub>Ce<sub>0.25</sub>)VO<sub>4</sub> ceramic with a  $\epsilon_r$  of ~47.9 and a Qf value of ~18 000 GHz. However, we have noticed that the (Bi<sub>0.4</sub>Ce<sub>0.6</sub>)VO<sub>4</sub> has a TCF = +173 ppm/°C and the microwave dielectric properties of zircon-structured CeVO<sub>4</sub> were reported by Zuo et al<sup>10</sup> with a  $\epsilon_r$  of ~12.3, a Qf value of ~41 460 GHz, and a negative TCF of ~-34.4 ppm/°C. Furthermore, from the pseudo phase diagram of the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> system reported in the literature,<sup>9,11</sup> (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> should be a tetragonal zircon phase between  $x = 0.6 \sim 1$ . Therefore, there are possibilities to design a temperature-stable microwave dielectric ceramic in (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $0.6 < x < 1$ ) solid solutions.

In this investigation, the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $0.7 \leq x \leq 0.95$ ) solid solution ceramics were synthesized by a conventional solid-phase reaction method to prepare a temperature-stable microwave dielectric ceramic with near-zero TCF. The structural evolution, sintering behaviors, microstructures, and microwave dielectric properties were investigated in detail.

## 2 | EXPERIMENTAL PROCEDURES

Proportionate amounts of reagent-grade starting materials of CeO<sub>2</sub> (99%), Bi<sub>2</sub>O<sub>3</sub> (99%), and V<sub>2</sub>O<sub>5</sub> (99%) were measured based on the stoichiometric formulation of (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $0.7 \leq x \leq 0.95$ ). Details of the processing can be found in our previous work.<sup>9</sup> Samples were sintered in the temperature range 870 ~ 970°C for 2 hours. The samples were investigated using room-temperature X-ray diffraction (XRD) with CuK $\alpha$  radiation (Rigaku D/MAX-2400 X-ray diffractometry). The microstructure images of the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $0.7 \leq x \leq 0.95$ ) ceramics were obtained by scanning electron microscopy (FEI Quanta F250). The selected area electron diffraction (SAED) and high-resolution transmission electron microscopy (HRTEM) images were measured using a transmission electron microscope (TEM) (JEM-2100 Electron Microscope) operated at 200 kV. The surface properties of the (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> ceramic were characterized using X-ray photoelectron spectroscopy (XPS) on a Thermo Fisher ESCALAB Xi+. The infrared reflectivity spectra and Raman spectra were taken by a Bruker IFS 66v FTIR spectrometer (NSRL)

and a LabRAM HR Evolution with laser excitation at 532 nm, respectively. The  $\epsilon_r$  and Qf value of (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $0.7 \leq x \leq 0.95$ ) ceramics were obtained using a network analyzer (8720ES, Agilent). Since the TCF value was tested at the temperature ranging from 25°C to 85°C, the instruments used for the test were network analyzer and temperature chamber (Delta 9023, Delta Design). The formula for calculating TCF is as follows:

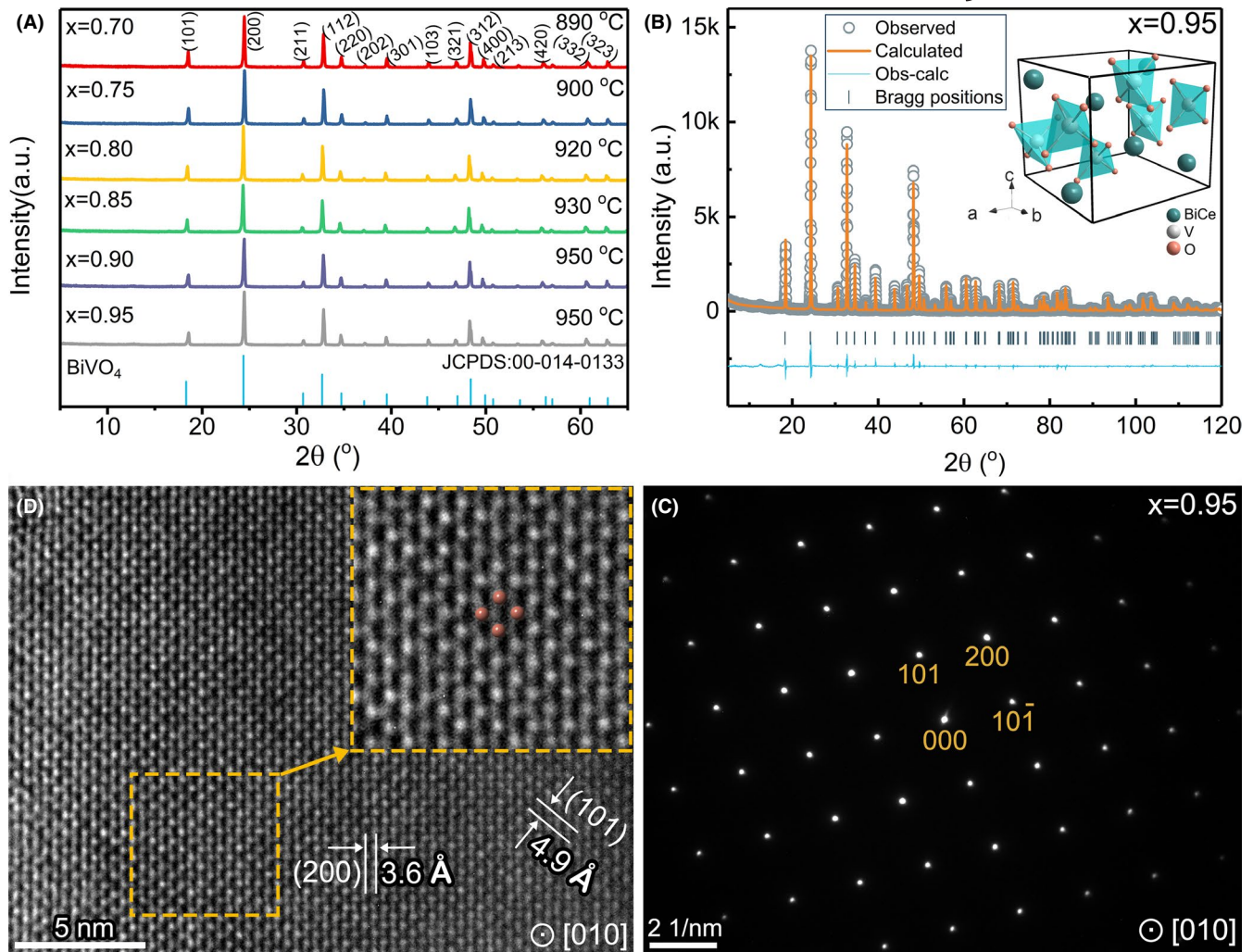
$$\text{TCF}(\tau_f) = \frac{f_T - f_{T_0}}{f_{T_0} \times (T - T_0)} \times 10^6, \quad (1)$$

where  $f_{T_0}$  and  $f_T$  are the resonant frequencies at temperatures  $T_0$  and  $T$ , respectively.

## 3 | RESULTS AND DISCUSSION

Figure 1A shows the XRD patterns of (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $0.7 \leq x \leq 0.95$ ) ceramics sintered at their optimum temperatures. It can be seen that the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $0.7 \leq x \leq 0.95$ ) ceramics were crystallized in a zircon-type tetragonal structure and no second phase is found, which indicates that the zircon-type tetragonal structure (space group I4<sub>1</sub>/amd) is stable in the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $0.7 \leq x \leq 0.95$ ) ceramics. In order to study the crystal structure of (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> ceramic in more detail, refinements were performed using GSAS software based on the XRD data recorded on (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> ceramic powders. The refinement results indicate that the (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> ceramic is a tetragonal zircon structure with a space group I4<sub>1</sub>/amd (No. 141) and the lattice parameters are  $a = b = 7.3777(4)$  Å,  $c = 6.4809(1)$  Å. Figure 1B shows the calculated and measured XRD patterns, and the illustration is schematic crystal structure of the (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> ceramic. In addition, the refined atomic fractional coordinates are listed in Table 1. The goodness-of-fit of refinement ( $R_{wp}/R_{exp}$ ) is 1.9. Furthermore, we also used TEM to further analyze the structure of (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> ceramic. The SAED pattern and HRTEM images of (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> ceramic recorded along the [010] zone axis are presented in Figure 1C,D. The HRTEM image demonstrates that the characteristic spacings of the (200) and (101) lattice planes of (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> ceramic are 0.36 and 0.49 nm, respectively, which correspond well with the refined lattice parameters. The schematic diagram of crystal structure can be well matched with the HRTEM image, and the small dots shown in Figure 1D are oxygen atoms. All of these results are well matched, which confirm that (Bi<sub>0.05</sub>Ce<sub>0.95</sub>)VO<sub>4</sub> ceramic belongs to the tetragonal zircon structure with a space group I4<sub>1</sub>/amd (No. 141).

The surface micromorphology of the (Bi<sub>1-x</sub>Ce<sub>x</sub>)VO<sub>4</sub> ( $0.7 \leq x \leq 0.95$ ) ceramics was studied by scanning electron



**FIGURE 1** A, X-ray diffraction patterns of the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.7 \leq x \leq 0.95$ ) ceramics sintered at optimal temperatures. B, The experimental (circle) and calculated (line) X-ray powder diffraction profiles for  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  sample sintered at  $950^\circ\text{C}$  (the short vertical lines below the patterns mark the positions of Bragg reflections. The bottom continuous line is the difference between the observed and calculated intensity.). Inset is the schematic crystal structure of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$ . C and D, Selected area electron diffraction pattern and high-resolution transmission electron microscopy image of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  viewed along the  $[010]$  zone axis [Color figure can be viewed at wileyonlinelibrary.com]

**TABLE 1** Refined atomic fractional coordinates from X-ray diffraction data of the  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic and the cell parameters are  $a = b = 7.3777(4)$  Å,  $c = 6.4809(1)$  Å with a space group  $I4_1/amd$  (No. 141)

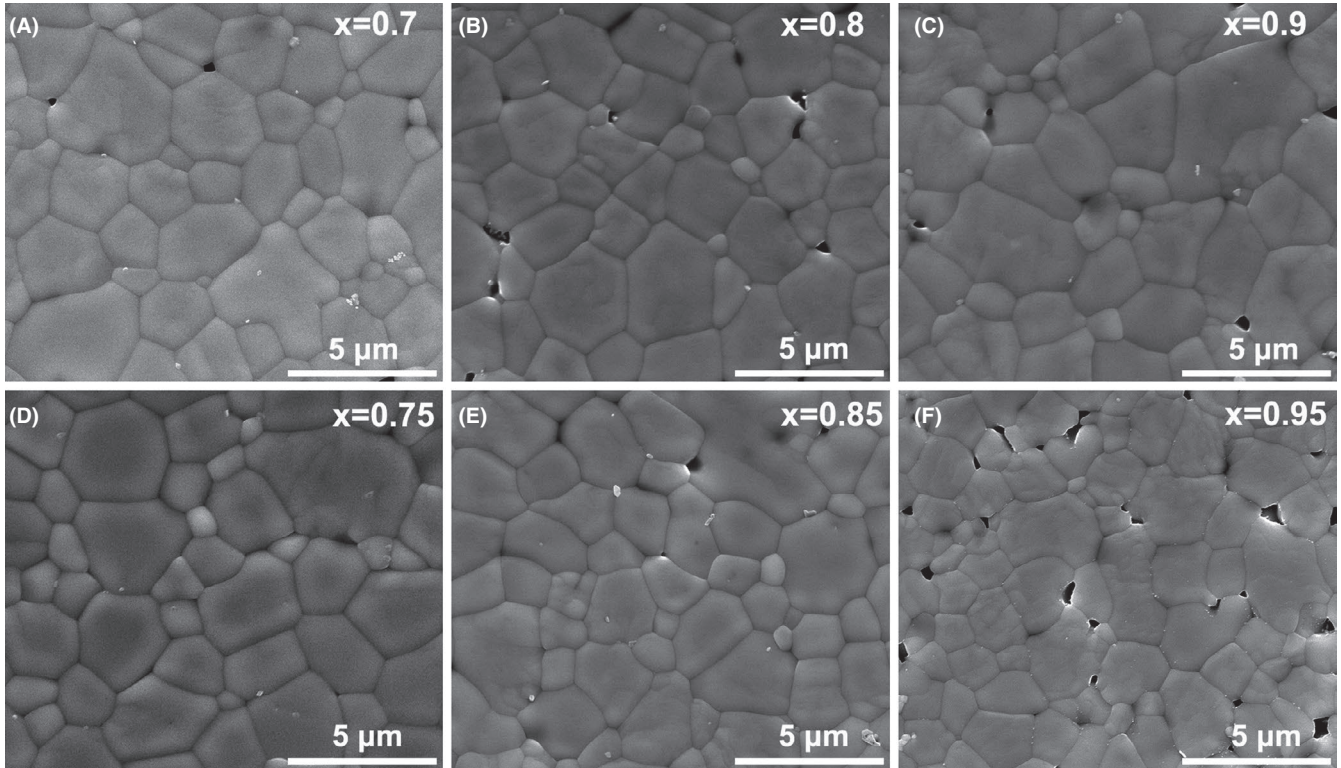
Atom	Wyckoff position	Occ.	x	y	z	Biso
Bi	4a	0.05000	0.00000	0.75000	0.12500	0.00914
Ce	4a	0.95000	0.00000	0.75000	0.12500	0.00914
V	4b	1.00000	0.00000	0.25000	0.37500	0.00992
O	16 h	1.00000	0.00000	0.07309	0.20880	0.01314

microscopy (SEM). The SEM images of thermally etched surface of the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.7 \leq x \leq 0.95$ ) ceramics sintered at optimal temperatures are shown in Figure 2A-F. Dense and homogeneous microstructures with almost no pores could be revealed in all compositions. Furthermore, the sintering temperatures of  $\text{BiVO}_4$  and  $\text{CeVO}_4$  ceramics are  $820^\circ\text{C}$  and  $950^\circ\text{C}$ , respectively.<sup>8,10</sup> So, the optimum sintering temperature of  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.7 \leq x \leq 0.95$ ) ceramics increased from  $890^\circ\text{C}$  to  $950^\circ\text{C}$  as  $x$  increased. This result

indicates that the sintering temperatures of  $\text{CeVO}_4$  ceramic can be lowered by the formation of solid solution and similar phenomena also exist in many other solid solution systems, such as  $(1-x)\text{BiVO}_4-x\text{LaNbO}_4$ ,  $(1-x)\text{BiVO}_4-x\text{La}_{2/3}\text{MoO}_4$ ,  $(\text{Ca}_{1-x}\text{Bi}_x)(\text{Mo}_{1-x}\text{V}_x)\text{O}_4$ , and  $(1-x)\text{BiVO}_4-x(\text{Ag}_{0.5}\text{Bi}_{0.5})\text{MoO}_4$  etc.<sup>12-15</sup>

A temperature-stable microwave dielectric ceramic with good microwave dielectric properties could be obtained at  $x = 0.95$  (as discussed in Figure 5 below). Therefore, it is





**FIGURE 2** A-F, Scanning electron microscopy images of thermally etched surface of the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.7 \leq x \leq 0.95$ ) ceramics sintered at optimal temperatures

necessary to study the  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic in more detail. Raman spectroscopy is a good means to analyze the vibration modes of structural units such as  $[\text{VO}_4]$ . Therefore, Raman spectroscopic investigation was also performed on  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic. Pure  $\text{CeVO}_4$  belongs to a tetragonal zircon structure with a space group  $I4_1/amd$  and a point group  $D_{4h}$  ( $4/mmm$ ). It is predicted by group theory that it has 12 distinct Raman active modes:

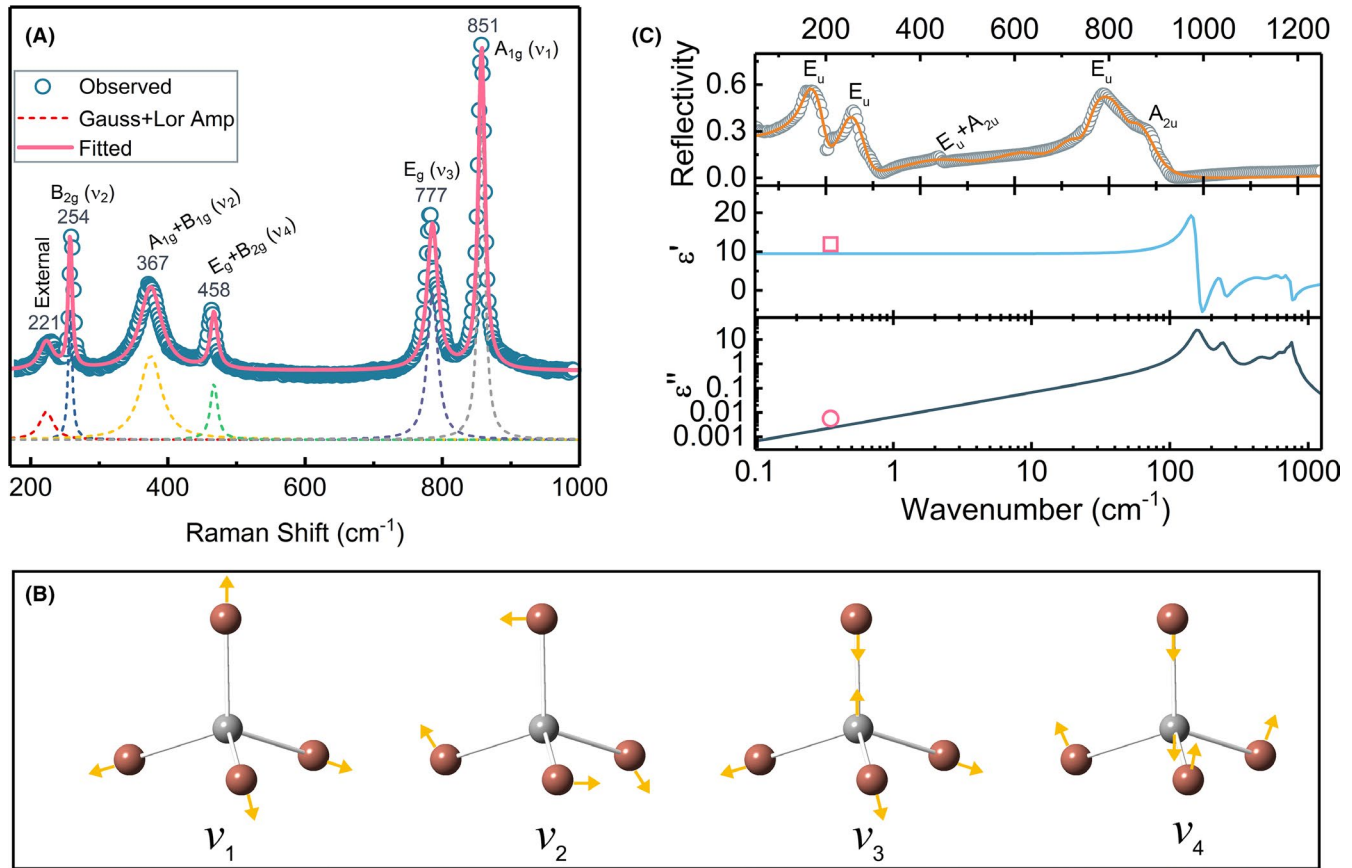
$$\Gamma = 2A_{1g} + 4B_{1g} + B_{2g} + 5E_g. \quad (2)$$

These vibration modes can be divided into two categories: internal models and external models. In  $\text{CeVO}_4$ , the vibration of the internal models is derived from the intermolecular vibration of the  $\text{VO}_4^{3-}$ . The vibration of each  $\text{VO}_4^{3-}$  anion is associated with other  $\text{VO}_4^{3-}$  ions in the same unit cell, resulting in abundant multi-vibration structure. One of the peaks shown in the spectrum may be due to the mixing of the vibrational compositions of different types of molecules. In order to observe the lattice vibration modes, the standard Gaussian-Lorentzian model was used to fit the Raman spectrum of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic to obtain the specific position information of all peaks. The fitted Raman spectra are presented in Figure 3A as red solid lines. As shown in Figure 3A, the strongest mode at  $851 \text{ cm}^{-1}$  is assigned as  $A_{1g}$  symmetric stretch ( $\nu_1$ ). The  $777$ ,  $458$ , and  $367 \text{ cm}^{-1}$  Raman modes are assigned as  $E_g$

asymmetric stretch ( $\nu_3$ ),  $E_g + B_{2g}$  deformation ( $\nu_4$ ), and  $A_{1g} + B_{1g}$  deformation ( $\nu_2$ ), respectively. The  $B_{2g}$  mode at  $254 \text{ cm}^{-1}$  can be interpreted as symmetric bending of the  $[\text{VO}_4]$  tetrahedron. Furthermore, the external modes appear at frequencies below  $250 \text{ cm}^{-1}$ . All vibration modes are consistent with the results reported in the previous literature.<sup>9,16,17</sup> The four normal vibration modes of tetrahedral  $[\text{VO}_4]$  are shown in Figure 3B. In addition, Figure 3C shows the calculated and measured infrared reflectivity spectra of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic. The bands at  $880$ ,  $788$ , and  $259 \text{ cm}^{-1}$  can be assigned as  $A_{2u}$  asymmetric stretch ( $\nu_3$ ),  $E_u$  asymmetric stretch ( $\nu_3$ ), and  $E_u$  deformation ( $\nu_2$ ), respectively. The weak band at  $441 \text{ cm}^{-1}$  is assigned as  $E_u + A_{2u}$  deformation ( $\nu_4$ ). While the band at  $176 \text{ cm}^{-1}$  can be assigned to the Bi-O band ( $E_u$ ). The infrared spectra of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic are similar to the reports in the literature.<sup>9,17,18</sup> In order to investigate the intrinsic microwave dielectric properties in detail, the infrared reflectivity spectra of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic were analyzed using a classical harmonic oscillator model:

$$\epsilon^*(\omega) - \epsilon(\infty) = \sum_{j=1}^n \frac{(z_j e)^2 / m_j V_j \epsilon_0}{\omega_{Tj}^2 - \omega^2 - j\gamma_j \omega}, \quad (3)$$

where  $z_j$  is the equivalent price of the  $j$ th vibration mode,  $m_j$  is the equivalent mass of the  $j$ th vibrational mode,  $V_j$  is the equivalent unit volume of the  $j$ th vibrational mode,  $\gamma_j$  is the damping



**FIGURE 3** A, The experimental (circle) and calculated (black solid line) Raman spectra of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic sintered at  $950^\circ\text{C}$  (the short dot lines represent the Gaussian-Lorentzian fitting results). B, Four normal vibration modes of tetrahedral  $[\text{VO}_4]$ . C, Measured and calculated infrared reflectivity spectra (solid line for fitting values and circle for measured values) and fitted complex dielectric spectra of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic (square and circles are experimental in microwave region) [Color figure can be viewed at wileyonlinelibrary.com]

coefficient of the  $j$ th vibrational mode,  $\omega_{Tj}$  is the angular frequency of the transverse optical modes of the  $j$ th mode of vibration, and  $n$  is the number of transverse phonon modes. The relation between complex reflectivity  $R(\omega)$  and dielectric constant can be written as follows:

$$R(\omega) = \left| \frac{1 - \sqrt{\epsilon^*(\omega)}}{1 + \sqrt{\epsilon^*(\omega)}} \right|^2. \quad (4)$$

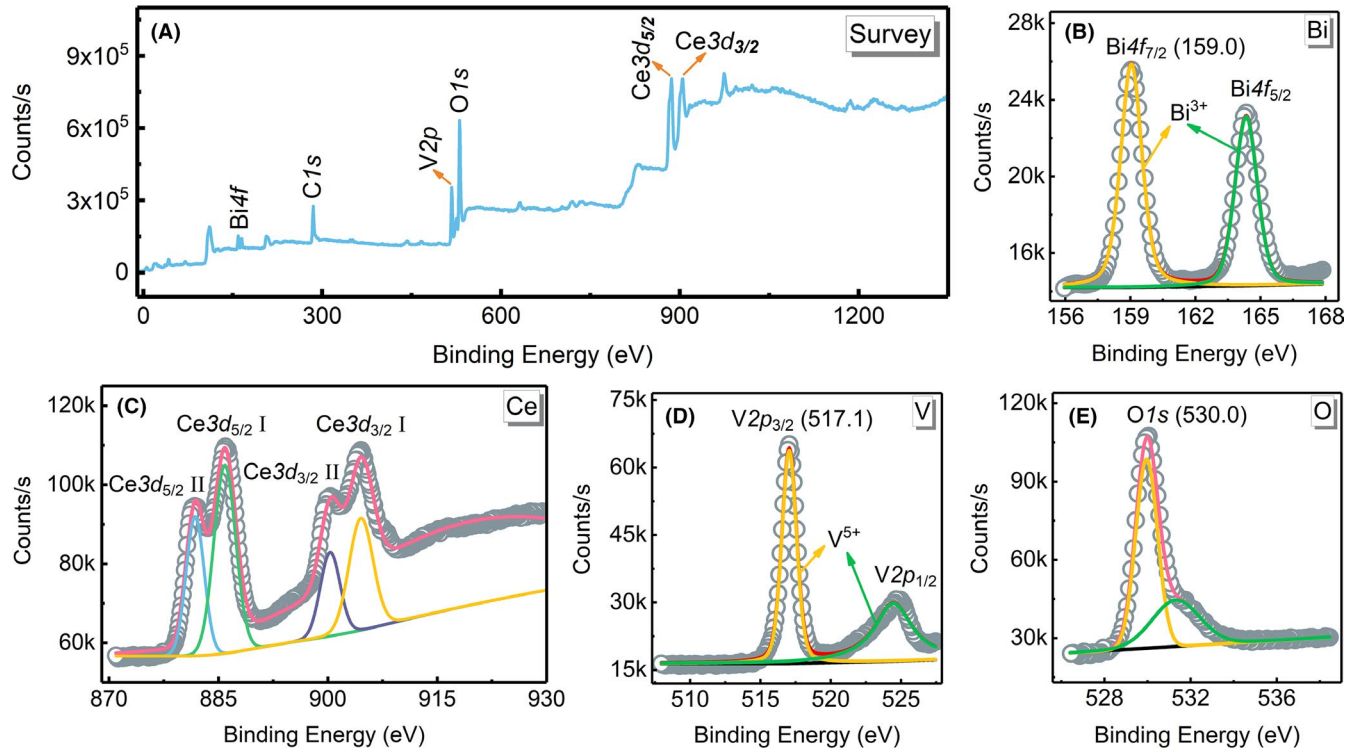
Figure 3C shows the fitted infrared reflectivity values and the complex permittivities, and Table 2 lists the relevant parameters. It can be seen that the measured values (using the  $\text{TE}_{018}$  method) are very close to the calculated dielectric constant and dielectric loss values, indicating that in the microwave region, the dielectric polarization is mainly caused by phonon absorption in the infrared region.

X-ray photoelectron spectroscopy was used to characterize the chemical composition and oxidation state of each element in the  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic. The XPS spectrum of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  sample with the survey and high-resolution spectrum of all elements are shown in Figure 4A-E. It is seen that the survey spectrum (Figure 4A) revealed the

**TABLE 2** Phonon parameters obtained from the fitting of the infrared reflectivity spectra of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic

Mode	$\omega_{oj}$	$\omega_{pj}$	$\gamma_j$	$\Delta\epsilon_j$
1	158.60	340.24	29.10	4.60
2	241.10	249.53	39.76	1.07
3	463.28	332.93	161.81	0.52
4	622.37	402.31	120.87	0.42
5	716.04	416.28	67.75	0.34
6	761.22	411.21	37.79	0.29
7	845.58	108.77	47.00	0.02
$(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$	$\epsilon_\infty = 2.23$		$\epsilon_0 = 9.48$	

presence of Bi, Ce, V, and O in  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$ . In the Ce 3d spectrum (Figure 4C), the peaks at 881.8 and 885.9 eV correspond to the Ce  $3d_{5/2}$  transitions, while the peaks at 900.2 and 904.3 eV belong to the Ce  $3d_{3/2}$  binding energy. The binding energies at 885.9 and 904.3 eV represent the  $3d^{10}4f^1$  initial electronic state corresponding to  $\text{Ce}^{3+}$  and no peak associated with  $\text{Ce}^{4+}$  was found, which is consistent with the results of  $\text{CeVO}_4$  reported in the literature.<sup>19,20</sup> The



**FIGURE 4** X-ray photoelectron spectroscopy spectra of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic with (A) the survey spectrum and high-resolution spectra of (B) Bi 4f, (C) Ce 3d, (D) V 2p, and (E) O 1s (all peaks have been calibrated with respect to the C 1s peak at 284.8 eV) [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com)]

V 2p spectrum exhibits two contributions,  $2p_{3/2}$  and  $2p_{1/2}$  (resulting from the spin-orbit splitting), located at, respectively, 517.1 and 524.6 eV, which can be matched well with  $\text{V}_2\text{O}_5$ .<sup>21</sup> The Bi 4f<sub>7/2</sub> peak at 159.0 eV agreed with the peak position of  $\text{BiVO}_4$  in the literature,<sup>22</sup> and the peak located at 530.0 eV can be assigned to O 1s of  $\text{O}^{2-}$ .<sup>23</sup> These results indicated that the oxidation states of Bi, Ce, and V in the  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  sample were +3, +3, and +5, respectively.

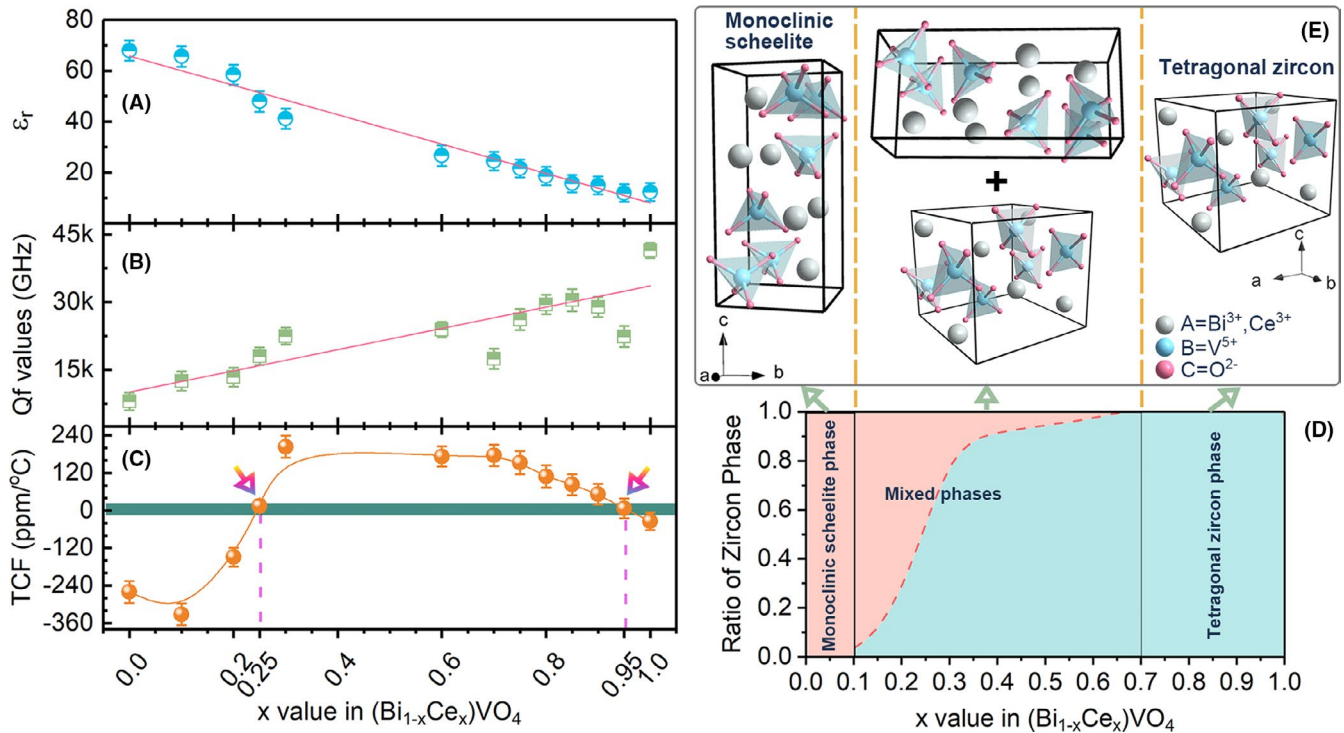
According to our previous work,<sup>9</sup> we found that the TCF of  $\text{BiVO}_4$  can be adjusted from  $-260$  ppm/°C to near zero ( $+15$  ppm/°C) when the substitution amount of Ce is 0.25 in the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 0.6$ ) ceramics. However, we also noticed that the TCF of  $(\text{Bi}_{0.4}\text{Ce}_{0.6})\text{VO}_4$  ceramic is  $+173$  ppm/°C, while Zuo et al reported that the TCF of  $\text{CeVO}_4$  ceramic is  $-34.4$  ppm/°C.<sup>10</sup> Therefore, another component with a near-zero TCF will appear in  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.6 < x < 1$ ) ceramics, which prompted us to find such a temperature-stable microwave dielectric ceramic. To better understand how microwave dielectric properties change with the substitution of Ce for Bi, the microwave dielectric properties,  $\epsilon_r$ , Qf, and TCF, of the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 1$ ) ceramics sintered at their respective optimum temperatures as a function of  $x$  value are presented in Figure 5A-C. Among them, the data of  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 0.6$ ) ceramics are taken from our previous work,<sup>9</sup> and the data of  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.7 \leq x \leq 0.95$ ) ceramics come from this work. In addition, the data of  $\text{CeVO}_4$

ceramic are taken from the literature reported by Zuo et al.<sup>10</sup> In order to make clear the changes of  $\epsilon_r$  and Qf with  $x$  value, we performed a linear fit on them separately. It can be seen that the  $\epsilon_r$  of samples decreases linearly with the increase of  $x$ , mainly because the  $\epsilon_r$  depends on the molecular polarizability. It has been reported in previous literature that the ionic polarizability of  $\text{Ce}^{3+}$  is smaller than that of  $\text{Bi}^{3+}$  in the structural environment of monoclinic scheelite and tetragonal zircon phase, thus resulting in the  $\epsilon_r$  of  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 1$ ) decreases with the cerium content.<sup>9</sup> As plotted in Figure 5B, the Qf values decrease roughly with the increase of  $x$ . In other words, the Qf values are inversely proportional to the permittivities. It is due to the intrinsic dielectric loss caused by absorptions of phonon oscillation in the lattice is proportional to the  $\epsilon_r$  and the optimum Qf value depends on the intrinsic dielectric loss based on the classical harmonic oscillator model. Therefore, the Qf value of  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 1$ ) ceramics shows an increasing trend. At microwave region, the Qf value has inverse relation to  $\epsilon_r$ .<sup>24</sup>

$$\left( Q \times f \approx \frac{(ze)^2 / mV\epsilon_0}{2\pi\gamma \times (\epsilon'(\omega) - \epsilon(\infty))} \right).$$

This relation has successfully explained the relationship between the Qf and the  $\epsilon_r$  of many scheelite solid solutions such as  $(\text{Bi}_{1-x}\text{Y}_x)\text{VO}_4$ ,  $[(\text{Li}_{0.5}\text{Bi}_{0.5})_{1-x}\text{Ca}_x]\text{MoO}_4$  and

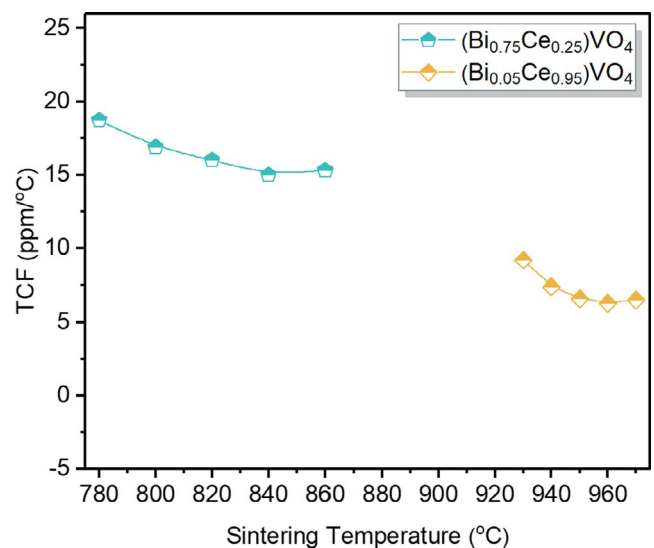




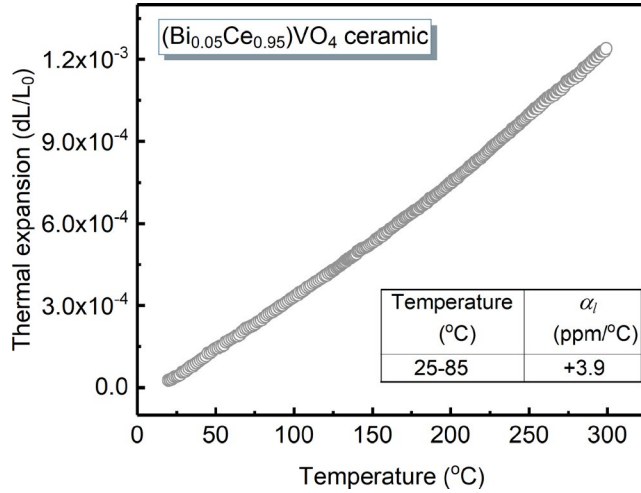
**FIGURE 5** The microwave dielectric properties,  $\epsilon_r$  (A),  $Q_f$  (B) and resonant frequency (C), of  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 1$ ) ceramics sintered at optimal temperatures as a function of  $x$  value. D, The pseudo phase diagram of the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  system. The red dotted line represent the zircon phase contents in samples calculated by Fullprof software (detailed information on the calculation method is described in the literature<sup>9</sup>). E, The associated schematic crystal structures of each region in pseudo phase diagram [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com)]

$(\text{Ca}_{1-x}\text{Bi}_x)(\text{Mo}_{1-x}\text{V}_x)\text{O}_4$ .<sup>15,18,24</sup> Moreover, the facts show that the same qualitative relationship is also suitable for  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 1$ ) ceramics. As presented in Figure 5C, the TCF first increases from a negative value to a positive value, and then decreases from a positive value to a negative value. Therefore, two component points with near-zero TCF appear in  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 1$ ) ceramics, which are  $x = 0.25$  and  $x = 0.95$ , respectively, indicating that the substitution of Ce for Bi in  $\text{BiVO}_4$  is an effective method to adjust TCF to near zero. To understand the effect of sintering temperature on the TCF values of these two component points, the TCF of  $(\text{Bi}_{0.75}\text{Ce}_{0.25})\text{VO}_4$  and  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramics as a function of sintering temperature is shown in Figure 6. It can be seen that the TCF of the  $(\text{Bi}_{0.75}\text{Ce}_{0.25})\text{VO}_4$  and  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramics tends to decrease first and then remain stable as the sintering temperature increases. In order to better understand the crystal structure of the two components with near-zero TCF, the pseudo phase diagram of  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 1$ ) ceramics and the associated schematic crystal structures of each region are shown in Figure 5D,E. It can be seen that the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0 \leq x \leq 0.1$ ) belongs to the monoclinic scheelite phase and the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.7 \leq x \leq 1$ ) belongs to the tetragonal zircon phase, while the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.1 < x < 0.7$ ) belongs to the mixed phases of both monoclinic scheelite and tetragonal zircon structure. Thus, the two components with near-zero TCF

belong to the mixed phases and the tetragonal zircon phase, respectively. It is important to note that the  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic sintered at 950°C can exhibit good microwave dielectric properties, with a  $\epsilon_r \sim 11.9$ , a  $Q_f \sim 22\,360$  GHz (at 10.6 GHz), and a TCF  $\sim +6.6$  ppm/°C. In the microwave region, polarizability is the sum of both ionic and electronic



**FIGURE 6** The resonant frequency of  $(\text{Bi}_{0.75}\text{Ce}_{0.25})\text{VO}_4$  and  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramics as a function of sintering temperature [Color figure can be viewed at [wileyonlinelibrary.com](http://wileyonlinelibrary.com)]



**FIGURE 7** Thermal expansion data of the  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic [Color figure can be viewed at wileyonlinelibrary.com]

components. Shannon<sup>25</sup> suggested that molecular polarizability ( $\alpha$ ) of complex substances maybe estimated by summing  $\alpha$  of the constituent ions which for  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  is:

$$\alpha_{\text{Bi}_{0.05}\text{Ce}_{0.95}\text{VO}_4} = 0.05\alpha_{\text{Bi}^{3+}} + 0.95\alpha_{\text{Ce}^{3+}} + \alpha_{\text{V}^{5+}} + 4\alpha_{\text{O}^{2-}} \approx 17.11 \text{ \AA}^3, \quad (5)$$

where the ionic polarizabilities of  $\text{Bi}^{3+}$ ,  $\text{Ce}^{3+}$ ,  $\text{V}^{5+}$ , and  $\text{O}^{2-}$  are 6.12, 6.15, 2.92, and 2.01  $\text{Å}^3$ , respectively.<sup>25</sup> Considering the Clausius-Mossotti relation,<sup>26</sup>

$$\epsilon_{\text{meas}} = \frac{3V + 8\pi\alpha}{3V - 4\pi\alpha} \Rightarrow \alpha = \frac{3V(\epsilon_{\text{meas}} - 1)}{4\pi(\epsilon_{\text{meas}} + 2)} \approx 16.51 \text{ \AA}^3, \quad (6)$$

where  $V$  is the cell volume ( $352.76/4 = 88.19 \text{ \AA}^3$ ), the molecular polarizability may be obtained from  $\epsilon_r$  to give  $\sim 16.51 \text{ \AA}^3$  which is similar to the calculated value ( $17.11 \text{ \AA}^3$ ) based on Shannon's additive rule. In addition, the TCF can be defined as follows:

$$\text{TCF} = -\left(\alpha_l + \frac{1}{2}\tau_\epsilon\right), \quad (7)$$

where  $\alpha_l$  is the thermal expansion coefficient and  $\tau_\epsilon$  is the temperature coefficient of the dielectric constant. According to the thermal expansion data (as shown in Figure 7), the  $\alpha_l$  of  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic is +3.9 ppm/°C between 25°C and 85°C. Hence, it can be calculated according to Equation 7 that  $\tau_\epsilon$  of the  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic is  $-21.0$  ppm/°C. In addition, using the Clausius-Mossotti relation, Bosman and Havinga<sup>27</sup> derived an expression for  $\tau_\epsilon$  at constant pressure as follows:

$$\begin{aligned} \tau_\epsilon &= \frac{1}{\epsilon} \left( \frac{\partial \epsilon}{\partial T} \right)_p = \frac{(\epsilon - 1)(\epsilon + 2)}{\epsilon} (A + B + C) \\ &= \left( \epsilon - \frac{2}{\epsilon} + 1 \right) (A + B + C), \end{aligned} \quad (8)$$

$$\begin{aligned} A &= -\frac{1}{3V} \left( \frac{\partial V}{\partial T} \right)_p, \quad B = \frac{V}{\alpha_m} \left( \frac{\partial \alpha_m}{\partial V} \right)_T \cdot \frac{1}{3V} \left( \frac{\partial V}{\partial T} \right)_p, \\ C &= \frac{1}{3\alpha_m} \left( \frac{\partial \alpha_m}{\partial T} \right)_V. \end{aligned}$$

The value of the A+B term is about 6 ppm/°C. Moreover, the term C generally lies between  $-1$  and  $\sim -10$  ppm/°C and represents the direct dependence of the polarizability on temperature. According to Equation 8, the (A+B+C) value of the  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic can be calculated to  $-1.6$  ppm/°C, which is within an acceptable range.

## 4 | CONCLUSIONS

In the  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.7 \leq x \leq 0.95$ ) ceramics, tetragonal zircon-type structured solid solution was formed. As  $x$  increased from 0.7 to 0.95, the sintering temperature of  $(\text{Bi}_{1-x}\text{Ce}_x)\text{VO}_4$  ( $0.7 \leq x \leq 0.95$ ) ceramics increased from 890°C to 950°C, while the TCF decreased linearly from +176.3 to +6.6 ppm/°C. Importantly, the  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic sintered at 950°C can exhibit good microwave dielectric properties, with a  $\epsilon_r \sim 11.9$ , a Qf  $\sim 22$  360 GHz (at 10.6 GHz), and a TCF  $\sim +6.6$  ppm/°C. It is proved that a temperature-stable microwave dielectric ceramic with zircon-type tetragonal phase can be obtained by the substitution of Ce for Bi in  $\text{BiVO}_4$ . This work presents a novel method to modify the TCF of  $\text{BiVO}_4$ -type materials.  $(\text{Bi}_{0.05}\text{Ce}_{0.95})\text{VO}_4$  ceramic has a good potential for microwave equipment and devices with near-zero TCF.

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