Lecture 5 Auctions (拍卖)



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Overview

- First-price Sealed Bid Auction
- Second-price Sealed Bid Auction (Vickrey Auction)
- Ascending-price Auction (English Auction)
- Descending-price Auction (Dutch Auction)

First-price Sealed Bid Auction

- Each bidder submits a sealed bid b_i
- Auctioneer opens the bids, and then:
 - Bidder *i* with highest b_i wins.
 - Bidder *i* pays her bid amount b_i .
- No dominant strategy
- Players have to reason about other player's values and strategies to come up with a bid.

First-price Sealed Bid Auction

- N bidders, with values uniformly distributed in [0,1].
- b(v) must be strictly increasing in v
- There is a unique symmetric Bayes-Nash equilibrium, in which any bidder with valuation v bids: b(v) = [(N-1)/N] v
- In this equilibrium, bidder with highest valuation wins

Second-price Sealed Bid

- William Vickrey (1961)
- Each bidder submits a sealed bid b_i
- Auctioneer opens the bids, and then:
 - Bidder *i* with highest b_i wins.
 - Bidder *i* pays an amount equal to the secondhighest bid b_{j} .
- If bidders have private values t_i ,
 - It is a dominant strategy for bidders to bid $b_i = t_i$.
 - Very simple for bidders to play.

• Revenue is second-highest bid bj. school of Economics & Finance, XJTU December 12, 2016 http://zqiao.gr.xjtu.edu.cn



Second-price Sealed Bid

- Note: for common-value auctions, or auctions with side-effects, bidding truthfully may not be optimal.
- Vickrey auctions are much studied in economic literature, but are not particularly common in practice.

Ascending-price Auction

- Also called English auction.
- This is an example of an oral/iterative/open outcry auction.
- Auction procedure
 - Bidding starts from 0 or base price.
 - At any time, any bidder can raise the price by bidding.
 - When no one wants to raise the price any more, the auction ends.
 - Last bidder gets the item, at the price he bid. December 12, 2016
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Ascending-price Auction

- Variation Japanese auction
 - Auctioneer calls out increasing prices until only one bidder left.
 - At any price, bidder can quit but cannot reenter the auction.

Descending-price Auction

- Also called Dutch auction.
- This is an example of an oral/iterative/open outcry auction.
- Auction procedure
 - Bidding starts from a high price.
 - Auctioneer calls out a decreasing sequence of prices.
 - If bidder *i* wants to buy at the current price, she raises her hand.

Descending-price Auction

- Usually fast, because auction requires only one bid.
- Bidder must reason about other bidders' strategies, take risk tolerance into account.

Equivalence between SP-SB and English auction

- If bidders in an English auction have fixed private valuations
 - Dominant strategy is to keep raising your bid until either
 - No other bidders left, or
 - Current price exceeds your valuation
 - Result: Player with highest valuation wins, pays (a little more than) second highest valuation.
 - This is the same as the Vickrey (SP-SB) auction!

Equivalence between SP-SB and English auction

- Revenue
 - English auction revenue is (approximately) the second highest valuation.

Proxy bidding on eBay

et?

Place Bid					
Hello auctionsi! (<u>Not you</u> ?)					
Item you're bidding on: Canon Digital Camera ELPH PowerShot SD700 IS Current bid: US \$197.50 Your maximum bid: US \$ 197.50 (Enter US \$200.00 or more) You'll review your maximum bid, shipping cost, and payment methods in the next step.	What is a maximum bid? A maximum bid is the highest price you're willing to pay for an item. You won't necessarily pay the amount of your maximum bid. eBay will increase your bid on your behalf, using only as much of your bid as is necessary to maintain your high bid position. Your maximum bid is kept confidential. eBay increases your bid Current bid Minimum bid Learn more about bidding and bid increments.				

Equivalence between FP-SB and Dutch auctions

- In a Dutch auction:
 - Strategies for player *i* are of the form "Bid if price reaches *b_i* and no one else has bid"
 - Winning bidder is player *i* with highest b_i , pays b_i
 - Equivalent to each player *i* bidding b_i in a FP-SB auction.
- Does not require independence of valuation
- Revenue of Dutch and FP-SB are the same.

Equivalence between Auctions

- Milgrom & Weber(1982) studied the case of auctions in which player valuations are affiliated: higher value for a competitor makes a higher bid more likely.
- ER(Ascending auction) >= ER(Vickrey) >= ER(FP-SB)
 - (Assuming bidders can see other bidders drop out in ascending auction)
- Intuition: In this kind of setting, more information about other players reduces the risk-of_bidding too high
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Common Value Auctions

- There is a true common value for the item, but players know only an approximation of the value.
- Example: "Signals" of value distributed about the true value.

Common Value Auctions

- Winner's curse:
 - Winning bidder probably has a higher signal than true value.
 - May actually incur a loss when true value is accounted for.
- Winner's curse: Why?
 - Overconfidence: people think they know more than they do
 - Disregard: people think others know less (or think less about what others know)

Reverse Auction

- Seller-bid (Reverse) Auction
 - Sellers bid the prices at which they are willing to sell. The buyer can accept the lowest offer

Reverse Auction

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All Pay Auction



Other Design Choices

- Reserve price
 - Price below which item will not be sold.
 - Can be treated as seller's bid.
 - Any of the classic auction forms can accommodate reserve prices.
- Stopping rule
 - Fixed time (e.g., eBay)
 - 5 minutes after last bid (e.g., Amazon (still?), Yahoo (seller's choice))
- Bid units and increments.
- Information revealed during open outcry auctions

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Other Design Choices

- Tricks to encourage entry (esp. of weaker bidders)
 - Discount on final price.
 - Premium to second-highest bidder.
 - Not-always-efficient auctions.
- Auction fees
 - Listing fee
 - Closing fee
- Preferential treatment to selected bidders.
- Include non-price attributes (usually for procurement auctions).
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Behaviors in Auctions

- Seller Biding
- Sniping