

# Digital Control Technique

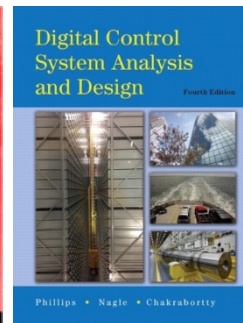
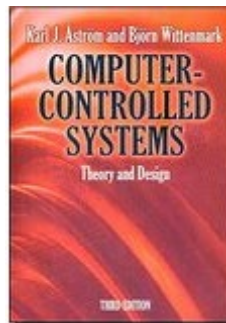
## Chapter 1 Introduction

Kou Peng



# Course Information

- Time: 16:40-18:30, Monday  
14:30-16:20, Thursday
- Venue: #326, #1 East Building
- Modules + Experiments
- Text book:
  - ▶ K. J. Astrom, Computer control system: theory and design
  - ▶ C. Phillips, et al., Digital control system analysis and design
  - ▶ 康波, 计算机控制系统



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- Office room: #110, #1 East Building  
#4197, Gongxing Building

# Contents

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- **1.2 Introduction to digital control systems**
- **1.3 Categories of digital control systems**
- **1.4 digital control theory**



# 1.1 Control Problem

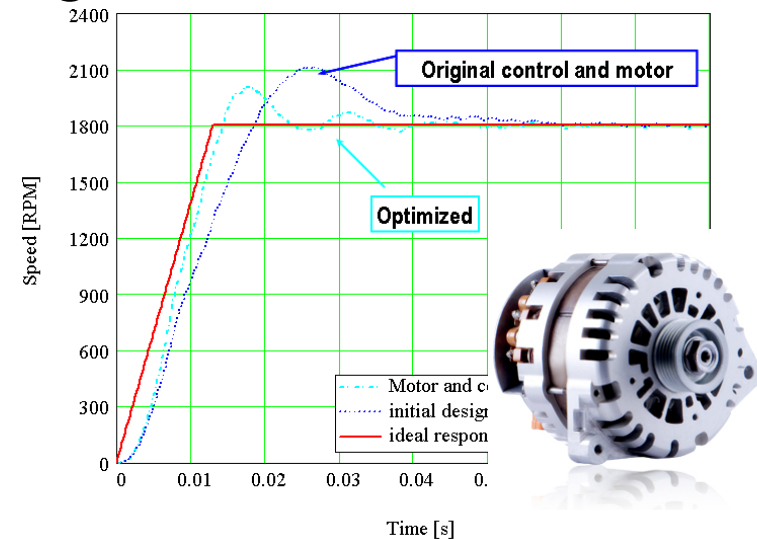
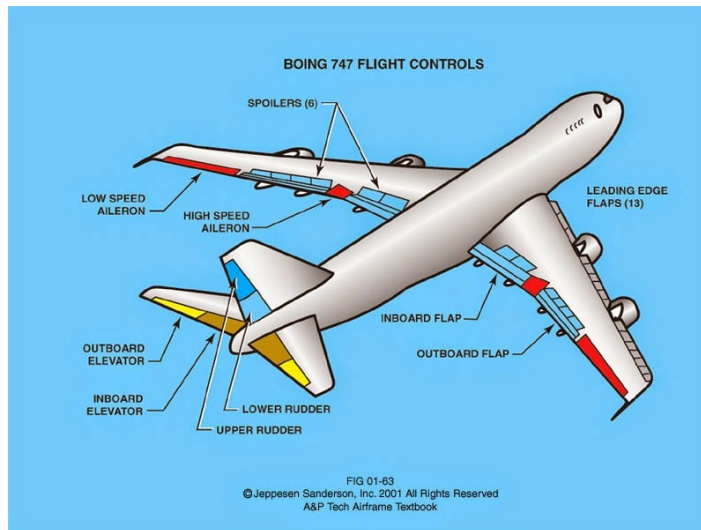
What do these two have in common?



- ▶ Highly nonlinear, complicated dynamics!
  - ▶ Both are capable of transporting goods and people over long distances
- BUT**
- ▶ One is controlled, and the other is not.

## Why do we need control system

- ▶ Industrial processes are not static but rather very **dynamic**; they are continuously changing as a result of many types of **disturbances**
- ▶ Every process has **inertia** in some degree

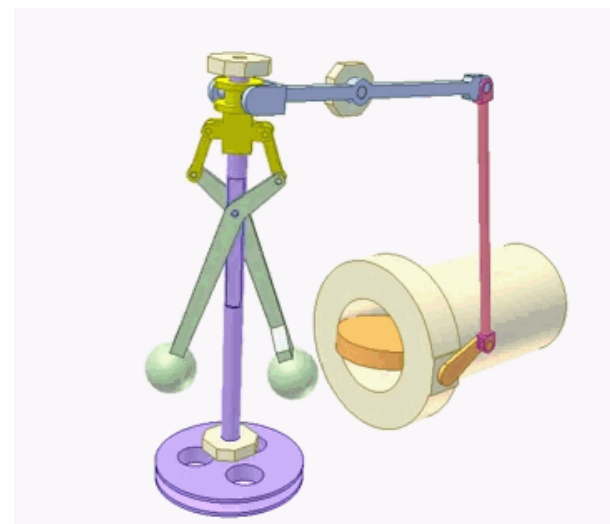
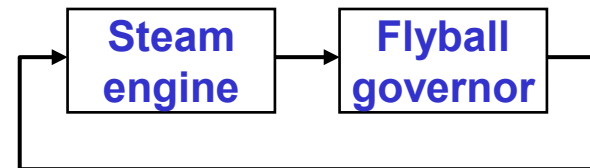
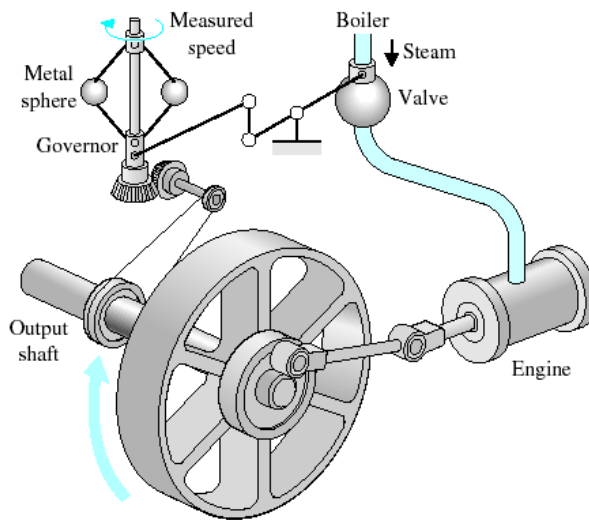


- ▶ It is principally because of this **dynamic** and **inertia** nature that control systems are needed to continuously and automatically watch over the variables that must be controlled

## ■ Fundament of modern control system

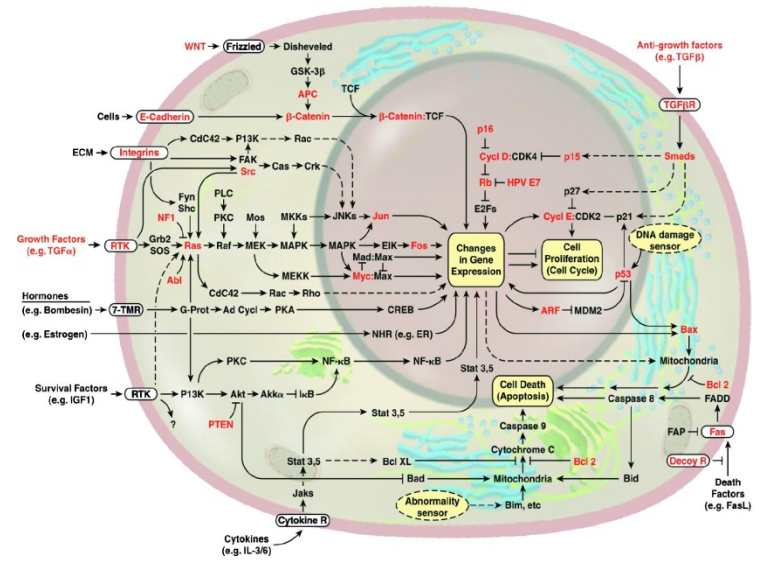
### ▶ Feedback

- Miriam Webster: the **return** to the **input** of a part of the **output** of a machine, system, or process (as for producing changes in an electronic circuit that improve performance or in an automatic control device that provide **self-corrective** action) [1920]



# Other Examples of Feedback

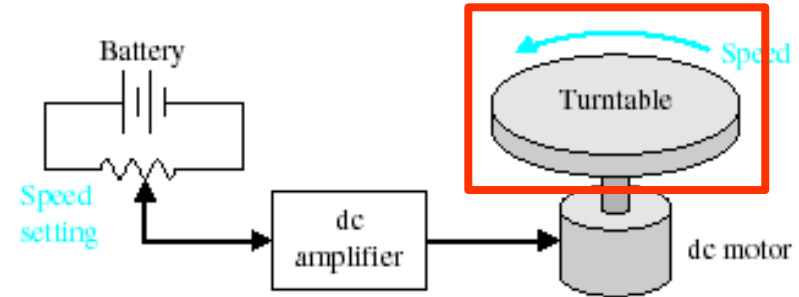
- Biological Systems
  - ▶ Physiological regulation (homeostasis)
  - ▶ Bio-molecular regulatory networks
- Population
  - ▶ Family planning
  - ▶ Two children policy
- Financial Systems
  - ▶ Markets and exchanges
  - ▶ Investment



## Open-loop and closed-loop control

### Open-Loop

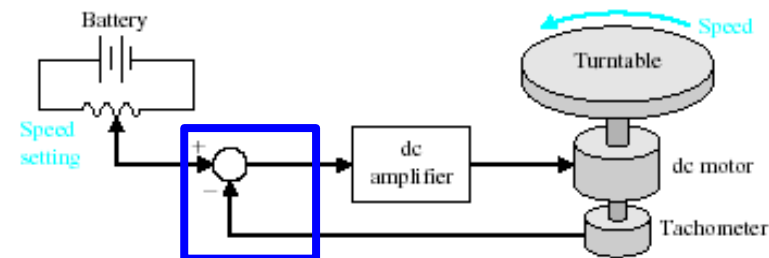
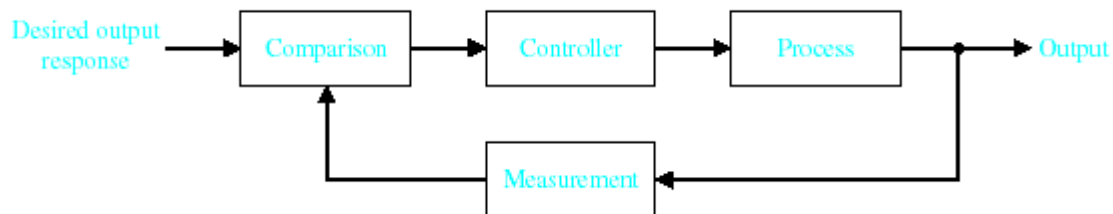
- Control Systems utilize a controller or control actuator to obtain the desired response



### Closed-Loop

- Control Systems utilizes feedback to compare the actual output to the desired output response

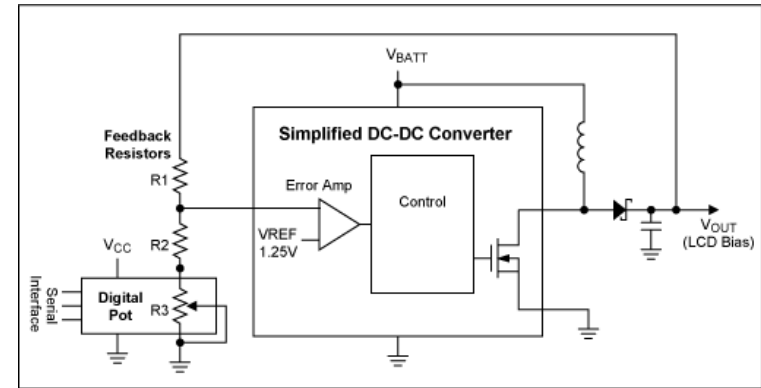
**Robust**



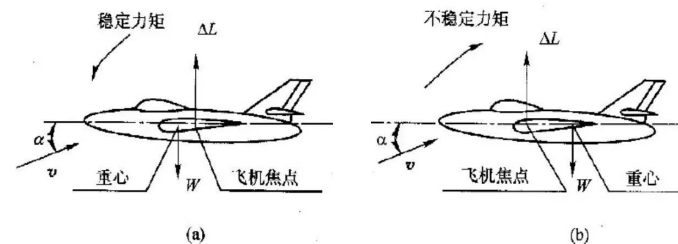


# Two main advantages of closed loop control

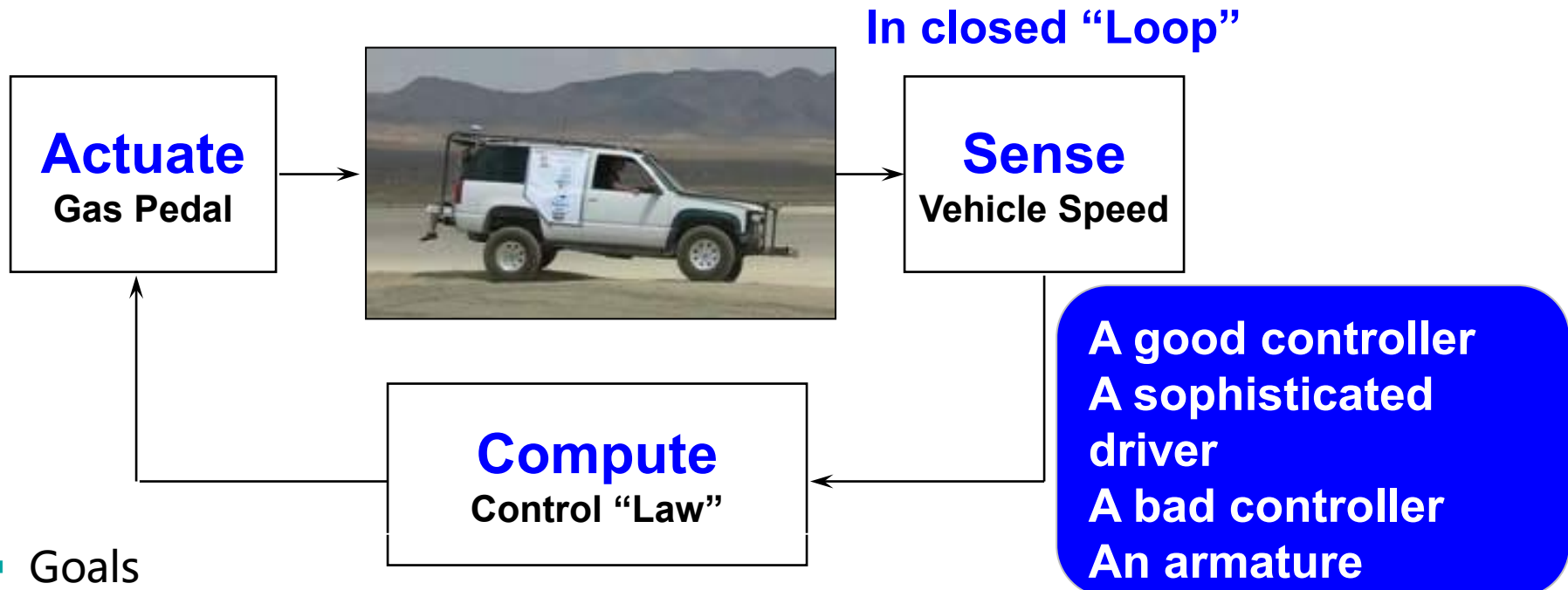
- **Robustness to uncertainty** through Feedback
  - ▶ Feedback allows high performance in the presence of uncertainty
  - ▶ Example: DC-DC converter with varying load
  - ▶ Key idea: accurate **sensing** to compare actual to desired, correction through **computation** and **actuation**
  
- **Design of dynamics** through feedback
  - ▶ Feedback allows the dynamics of a system to be modified
  - ▶ Example: stability augmentation for highly agile, unstable aircraft
  - ▶ Key idea: interconnection gives **closed loop** that modifies natural behavior



X-29 experimental aircraft



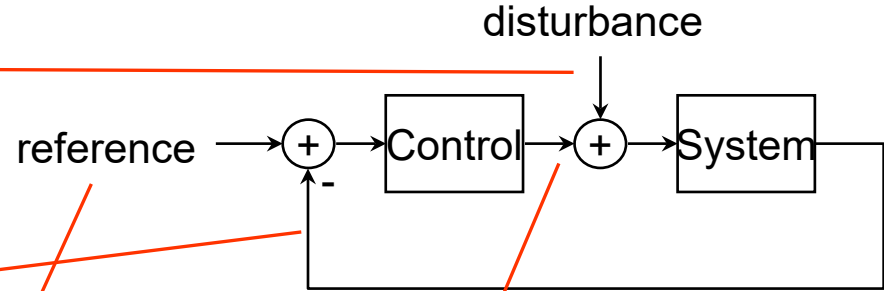
*Close loop control* = Sensing + Computation + Actuation



■ Goals

- ▶ **Stability**: system maintains desired operating point (hold steady speed)
- ▶ **Accurate**: small steady state error (close to 65 mph)
- ▶ **Dynamic performance**: system responds rapidly to changes (accelerate to 65 mph as soon as possible, overshoot as small as possible)
- ▶ **Robustness**: system tolerates perturbations in dynamics (mass, drag, etc)

Control is “the hidden technology that you meet every day”



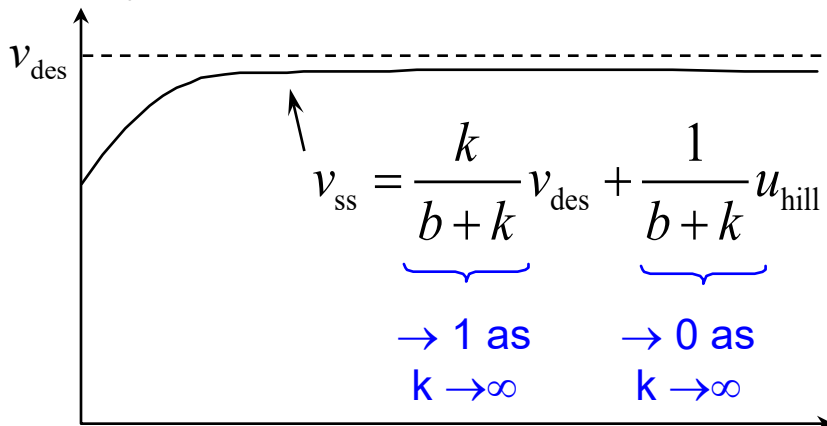
Model

$$m\dot{v} = -bv + u_{\text{engine}} + u_{\text{hill}}$$

P Law

$$u_{\text{engine}} = k(v_{\text{des}} - v)$$

velocity



Stability/performance

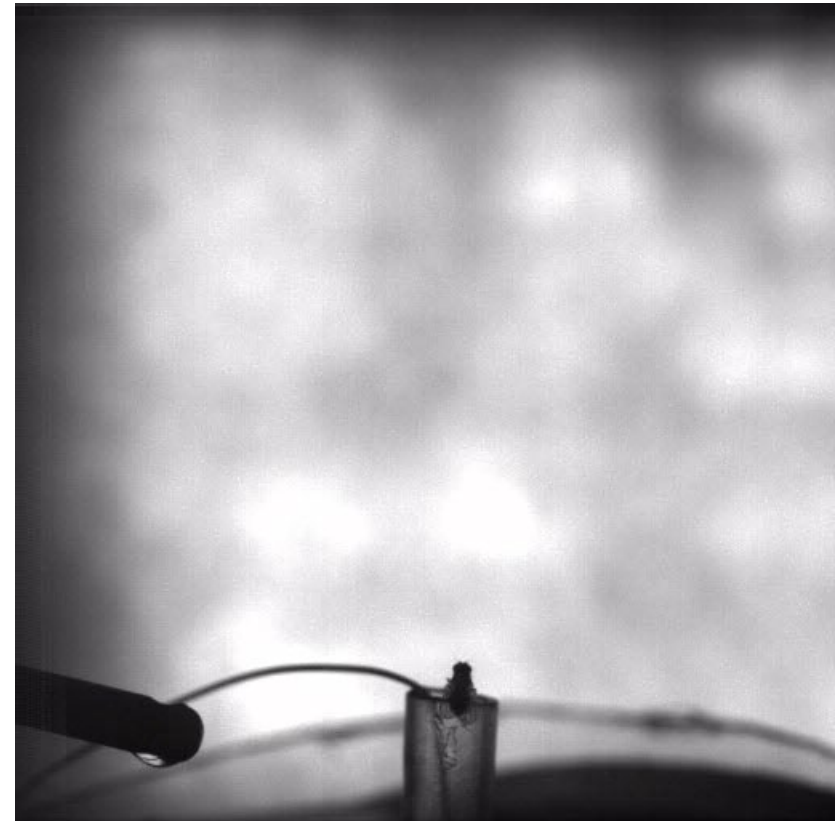
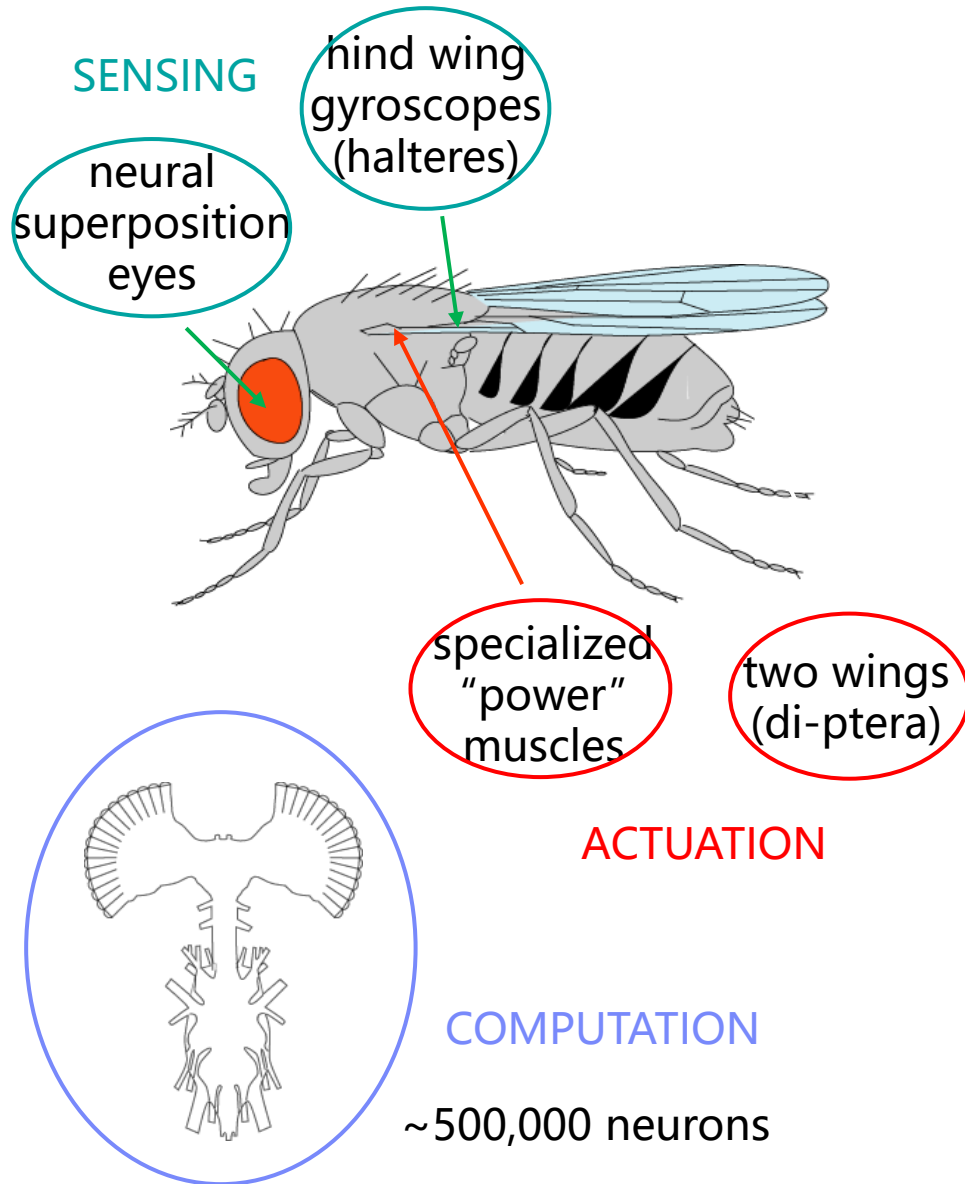
- Steady state velocity approaches desired velocity as  $k \rightarrow \infty$
- Smooth response; no overshoot or oscillations

Disturbance rejection

- Effect of disturbances (hills) approaches zero as  $k \rightarrow \infty$

Robustness

- Results don't depend on the specific values of  $b, m$ , for  $k$  sufficiently large



- More information:
  - M. D. Dickinson, Solving the mystery of insect flight, *Scientific American*, June 2001.

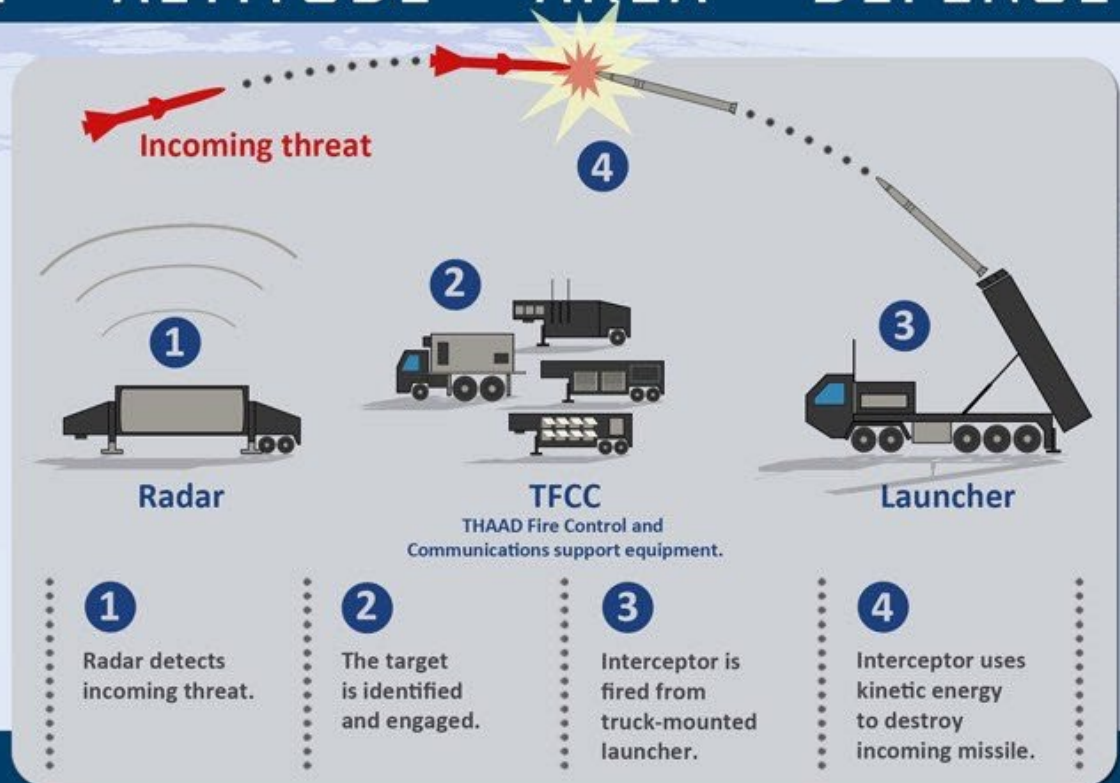
# Missile

## TERMINAL • HIGH • ALTITUDE • AREA • DEFENSE

# THAAD

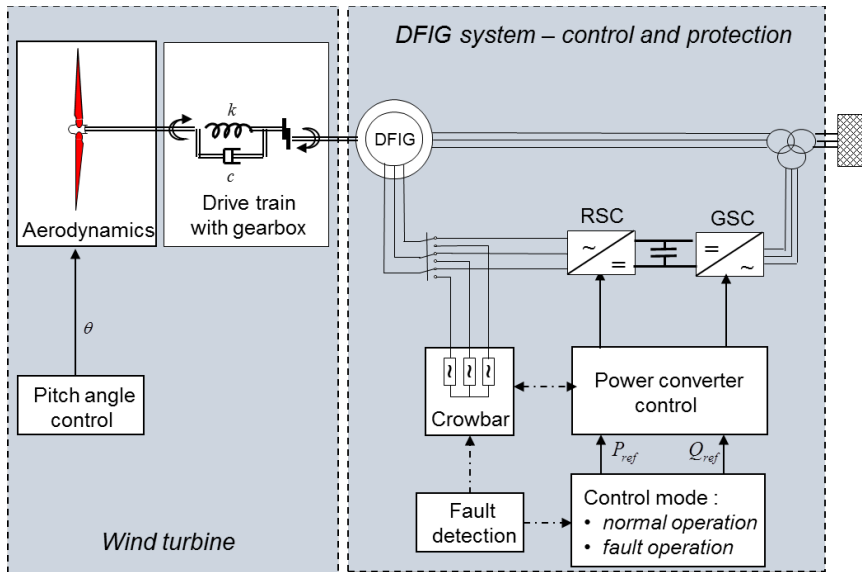
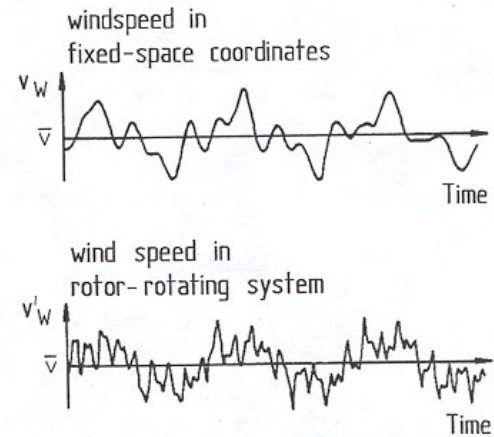
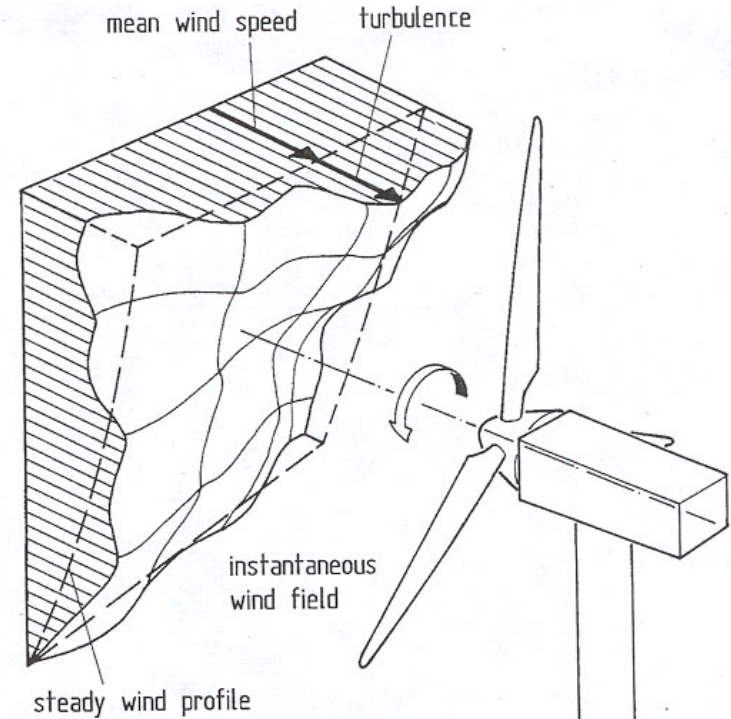
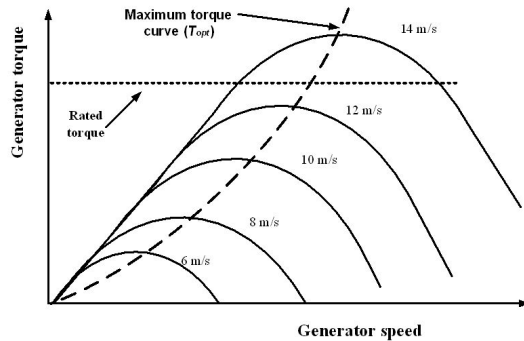
## INTERCEPTING A MISSILE.

The system has a track record of 100% mission success in flight testing.



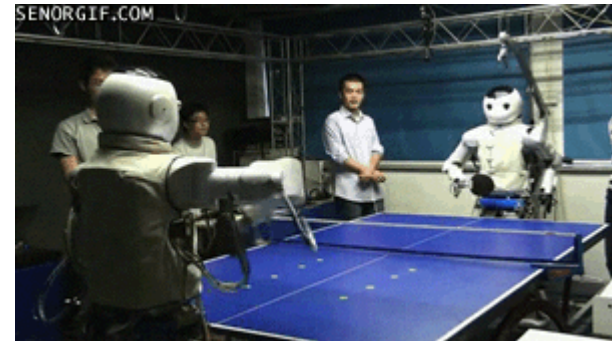
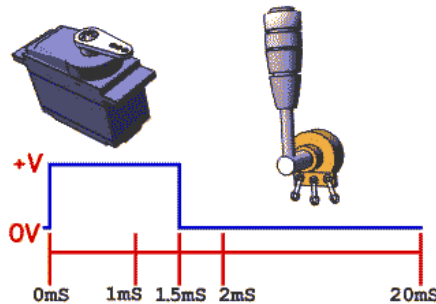
# How to maximum the captured energy under uncertainties?

- Stochastic Winds
- Wind Turbulence and Gusts

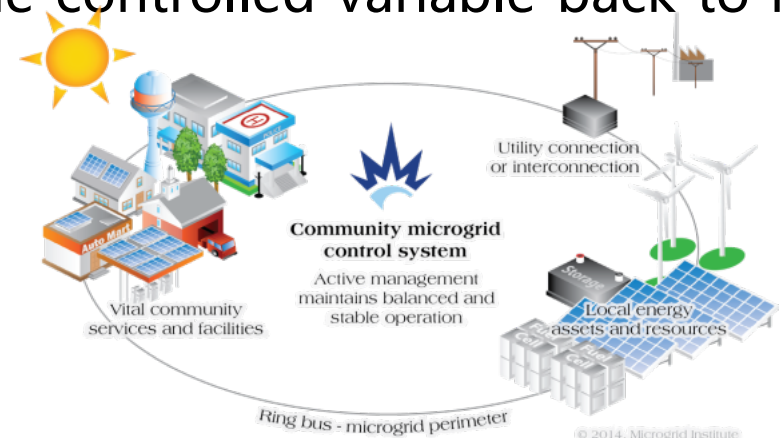


## Control task

- ▶ **Servo control** - The set-point signal is **changed** and the manipulated variable is adjusted appropriately to achieve the new operating conditions



- ▶ **Regulatory control** – The set-point is **fixed** at a constant value. When any disturbance enters the system, the manipulated variable is adjusted to drive the controlled variable back to its fixed set-point.



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- **1.3 Categories of digital control systems**
- **1.4 digital control theory**



## 1.2 Introduction to Digital Control Systems

- Analog control system and digital control system



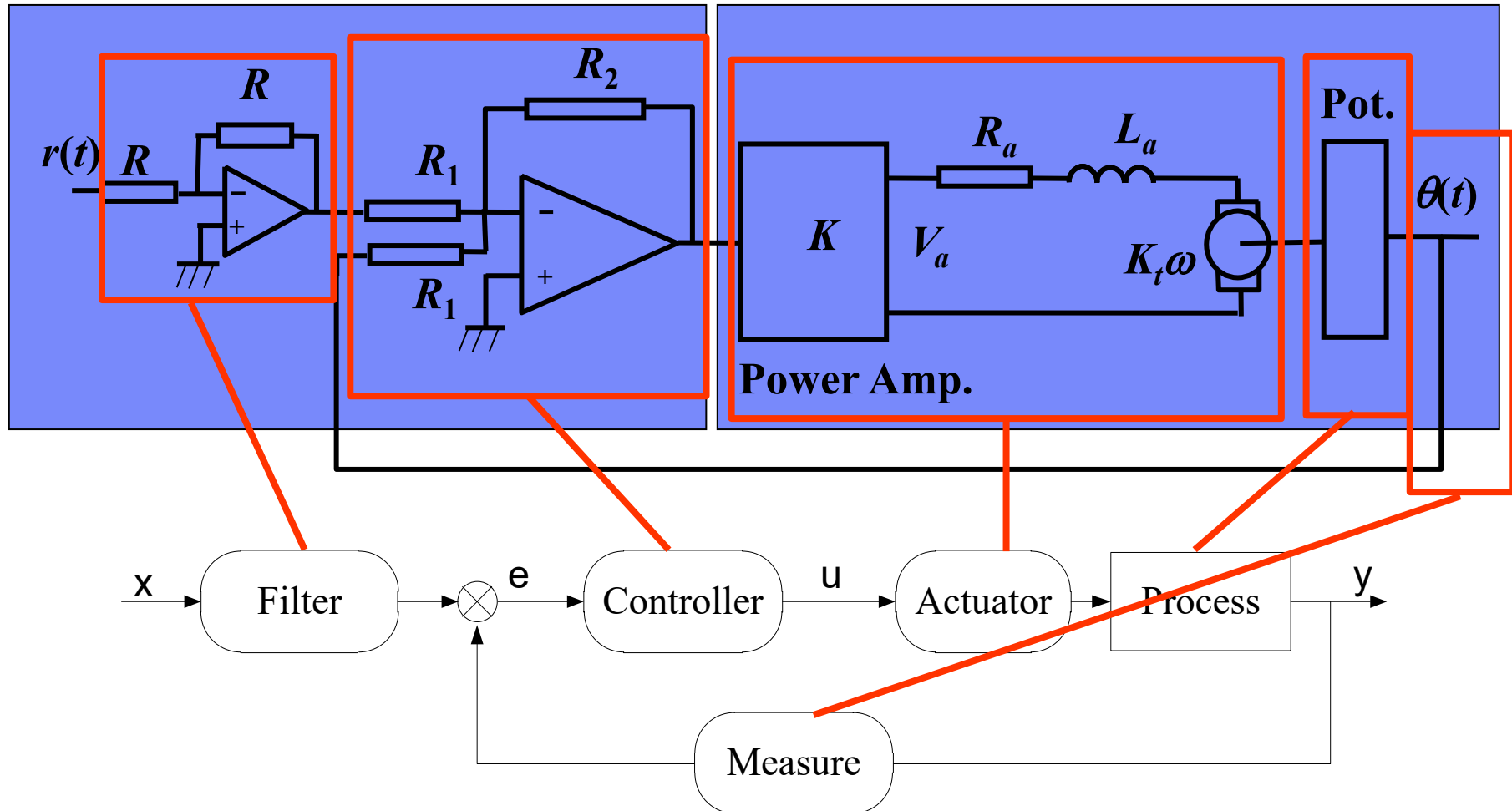
Analog



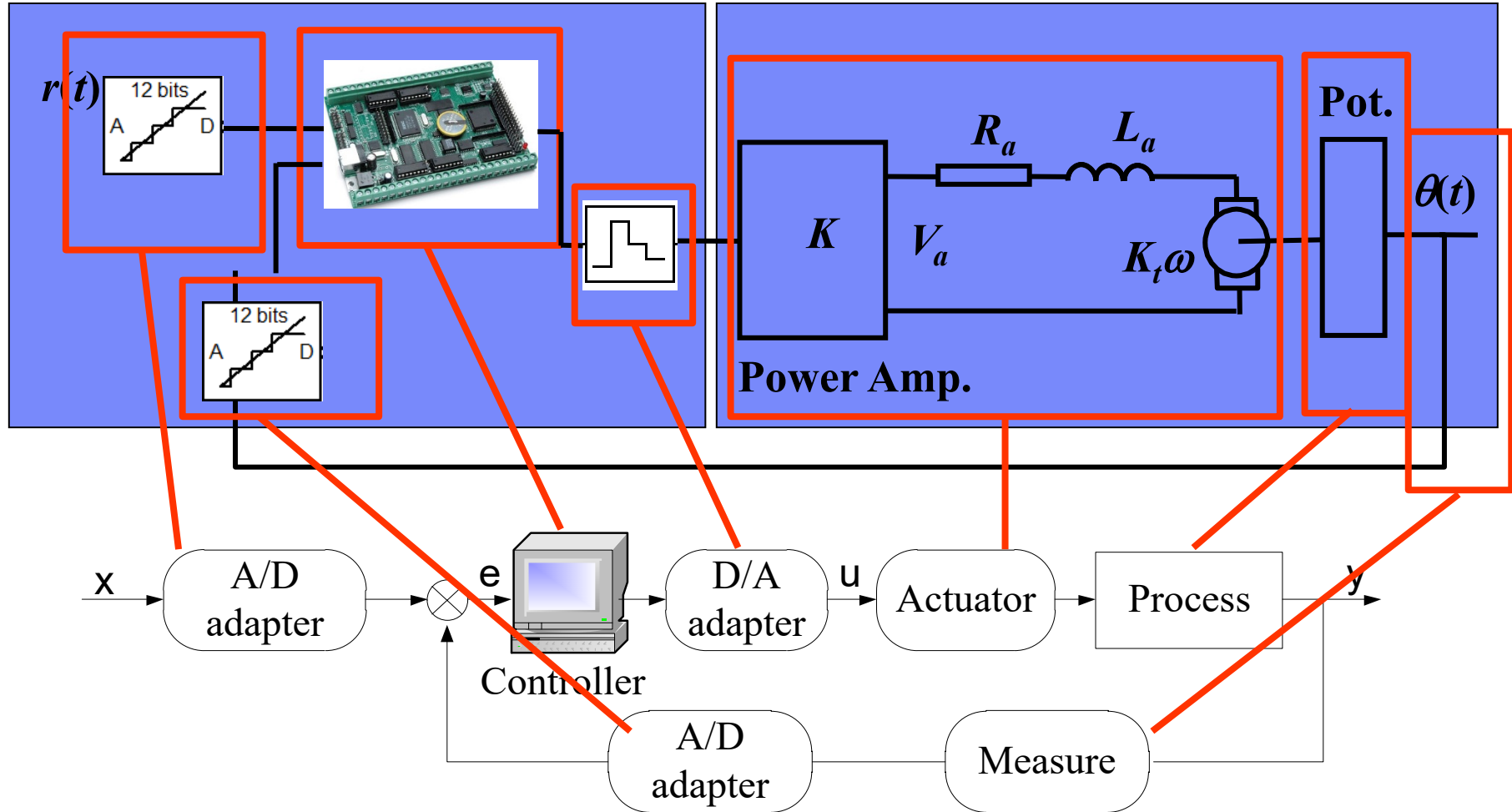
Digital



## ■ Analog control system

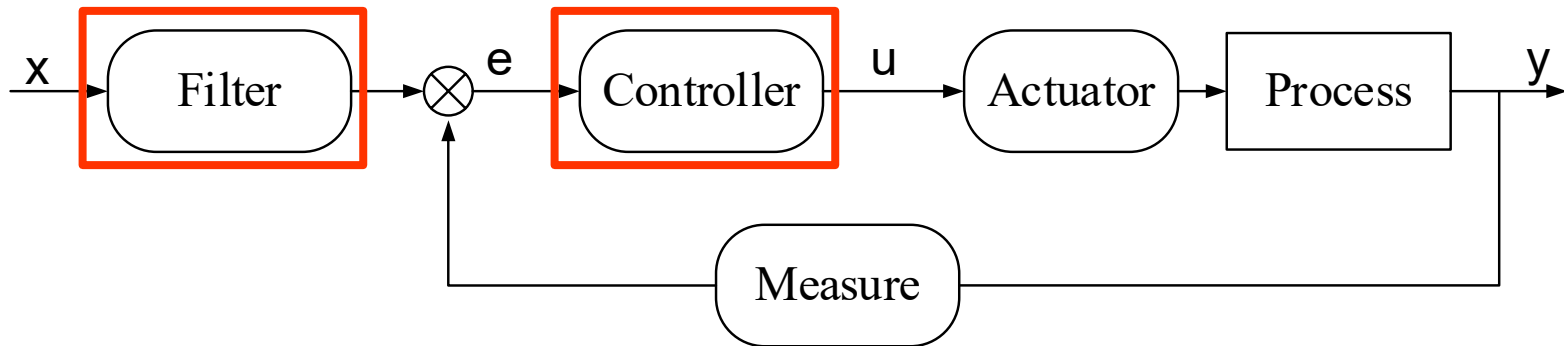


## ■ Digital control system

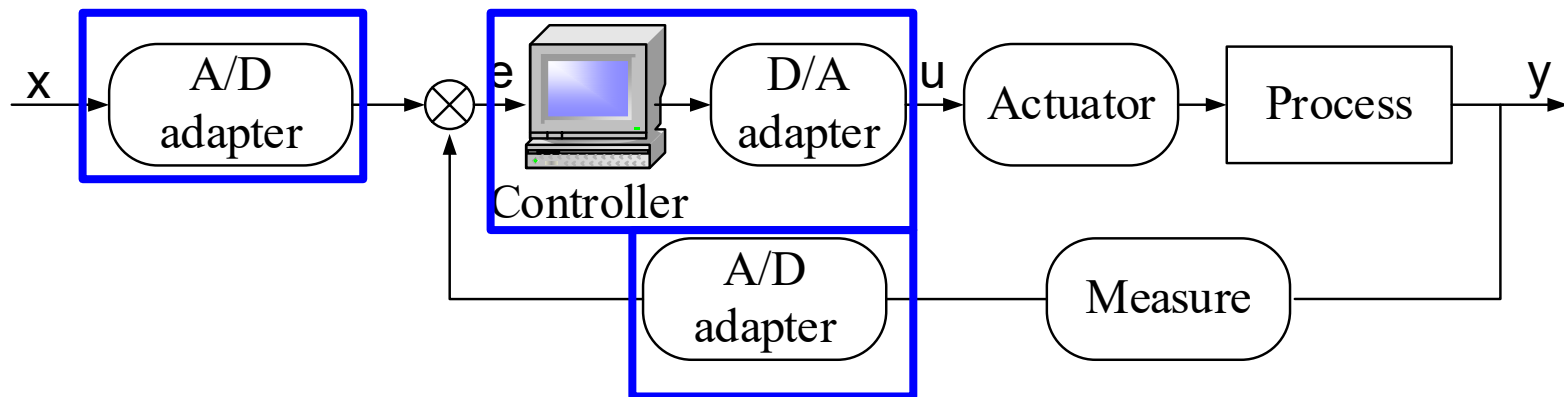


- Analog control system and digital control system

Analog Control System(ACS)



Digital Control System(DCS)



## Comparison between analog and digital control systems

	<b>ACS</b>	<b>DCS</b>
<b>Structure:</b>	Plant Actuator Measure <b>Controller (correcting network)</b>	Plant Actuator Measure <b>Controller (digital computer)</b> <b>Adapter (A/D, D/A)</b>
<b>Components:</b>	Analog	Digital + Analog
<b>Signals:</b>	Analog	Continuous analog Discrete analog Discrete digital

## ■ Virtues

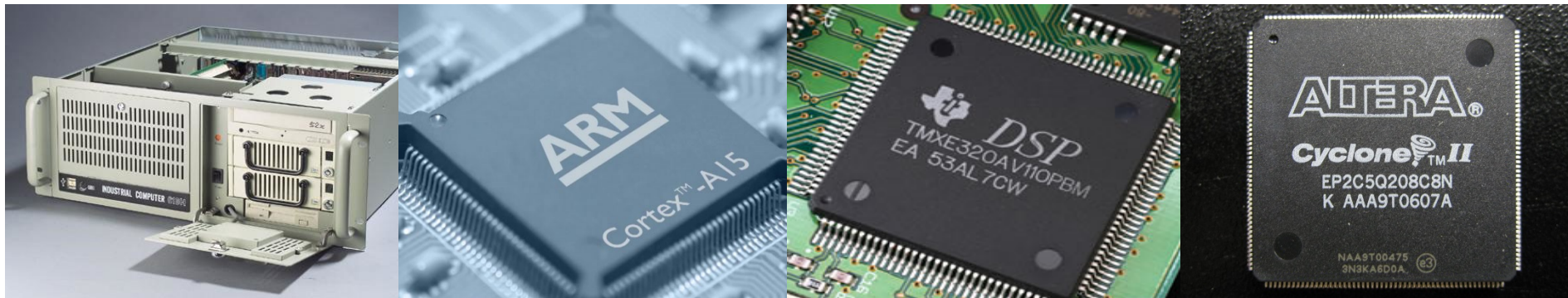
- ▶ Strong **computation** ability for realizing complex control algorithms
- ▶ High **precision**:  $10^{-70}$  (analog:  $10^{-2}$ )
- ▶ High volume **memory**: store a great deal of information
- ▶ **Robust**: use digital components
- ▶ **Flexible**: control algorithms easily modified

## ■ Defects

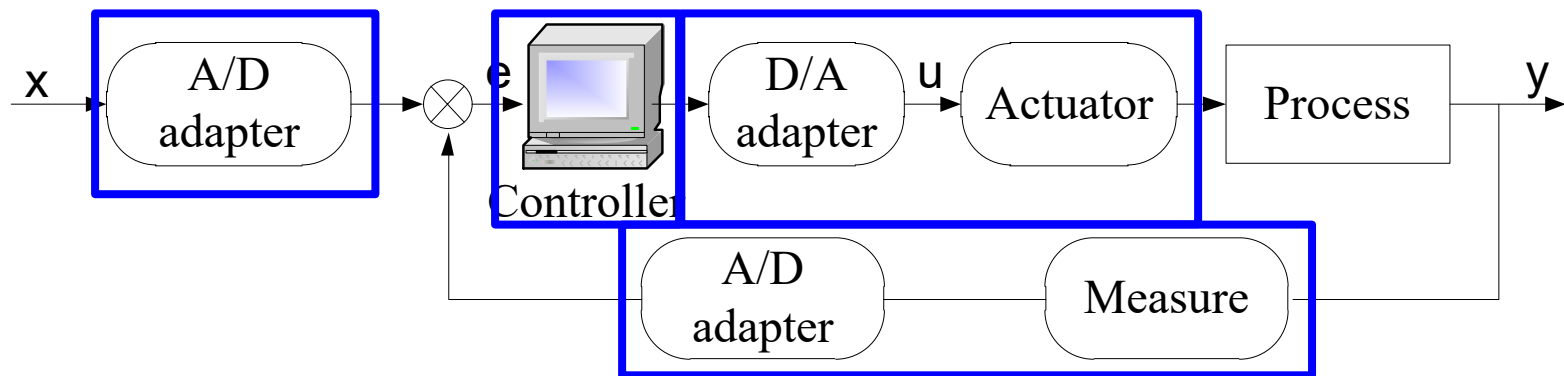
- ▶ **Lose information** during conversions: quantization error
- ▶ Computation **delay**: especially for serial computation and complex control algorithms



- The role of **computer** in a digital control system:
  - ▶ Compute the control actions
  - ▶ Collect data
  - ▶ Implement some advance control algorithms, such as optimal control, neural network control, predictive control, etc
- Typical computers used in the digital control system



- In each control cycle, the operation of a digital control system can be summarized as **three steps**:
  - ▶ Real time data **collection**: Measure and collect the states of the plant
  - ▶ Real time **decision**: Compute the control actions based on the reference and measurements
  - ▶ Real time **implementation**: Implement the computed control actions to the plant

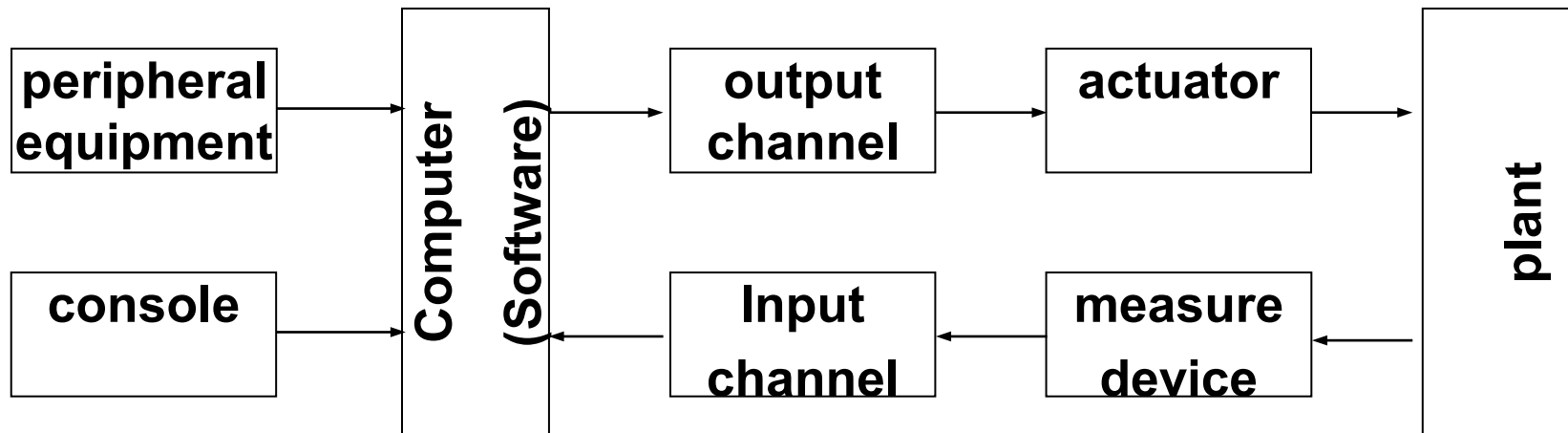


- In the next control cycle, these three steps are repeated



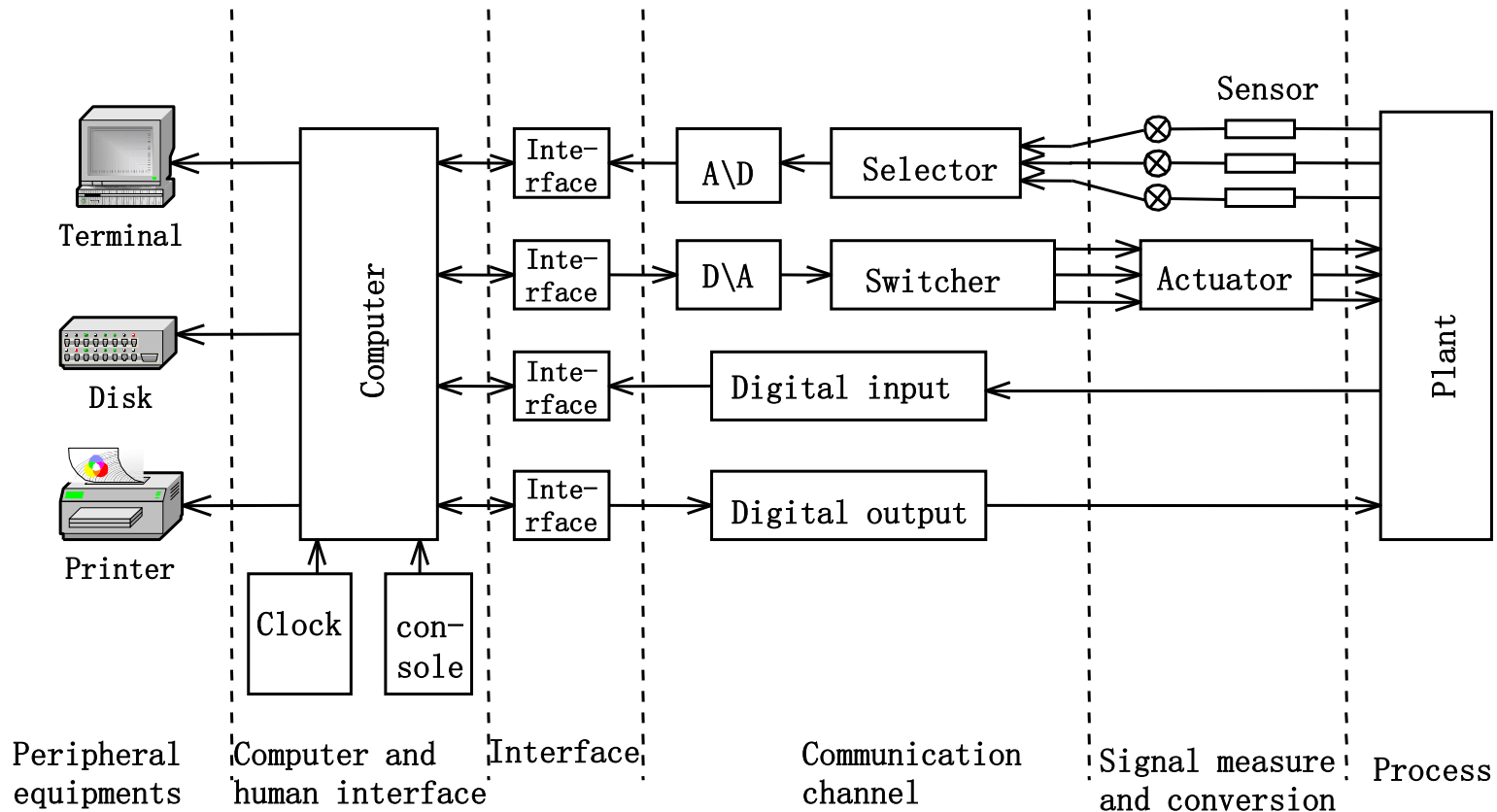
## Practical Structure of digital control systems

- In general, a digital control system is constitute of computer, peripheral equipment, console, input and output channels, actuator, measure devices, plant, and software
  - ▶ Hardware
  - ▶ Software



# Hardware components

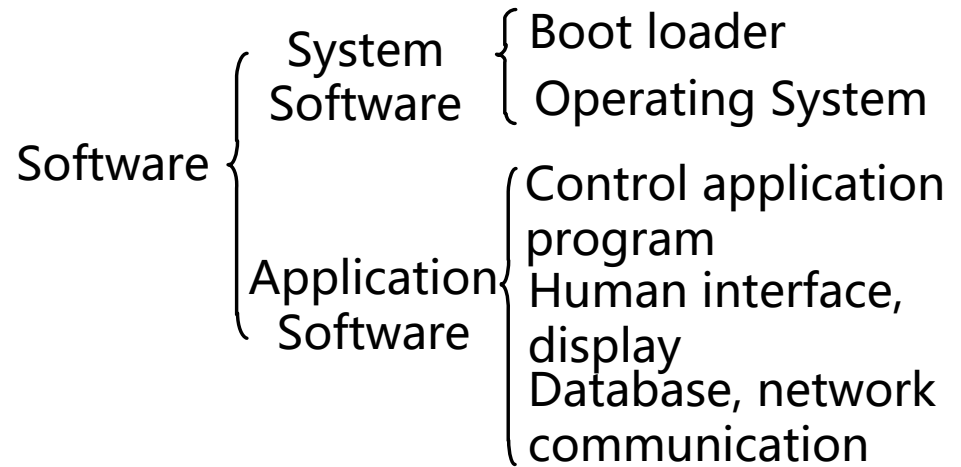
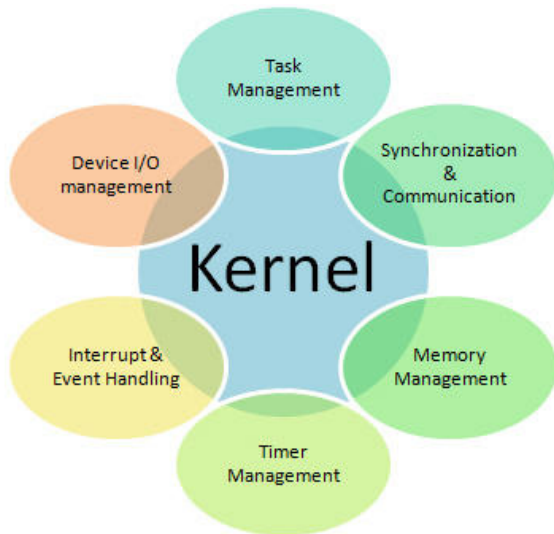
- Hardware components include the computer, human interface, peripheral equipment, input and output channels, and process



# Software components

- Soul of a digital control system

- ▶ System software
- ▶ Application software



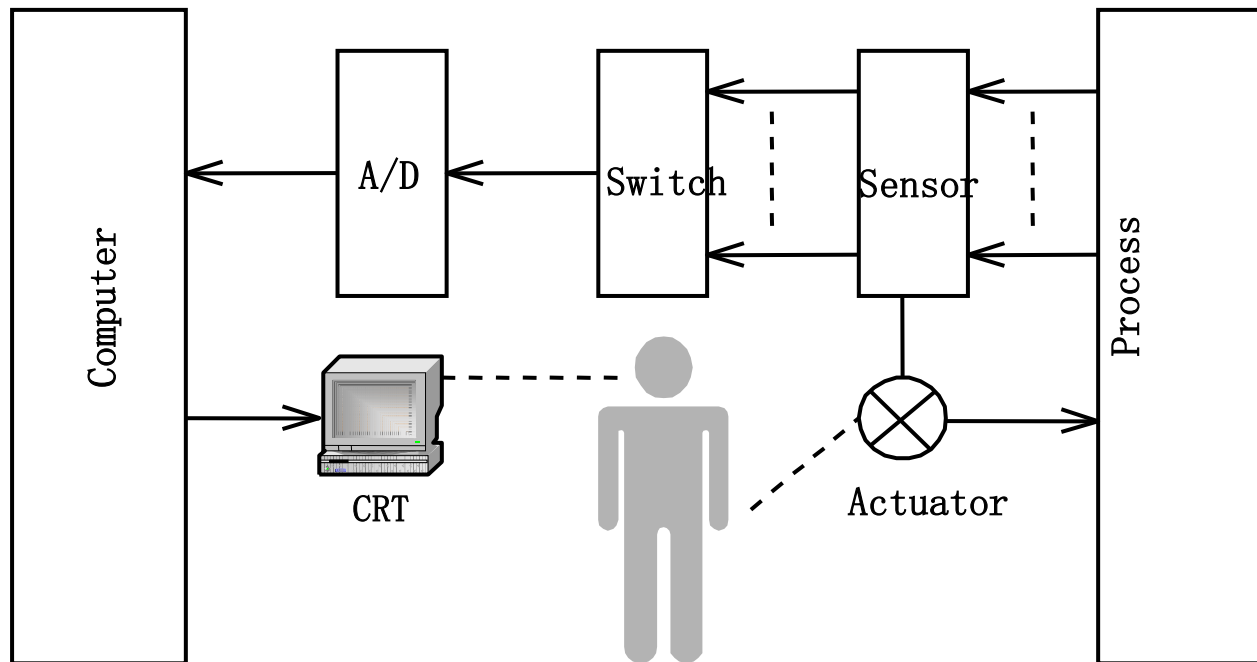
- Simple control applications
  - ▶ Boot loader + Interrupt
- Complex control applications
  - ▶ uC/OS-II, Windows CE, VxWorks, Embedded Linux

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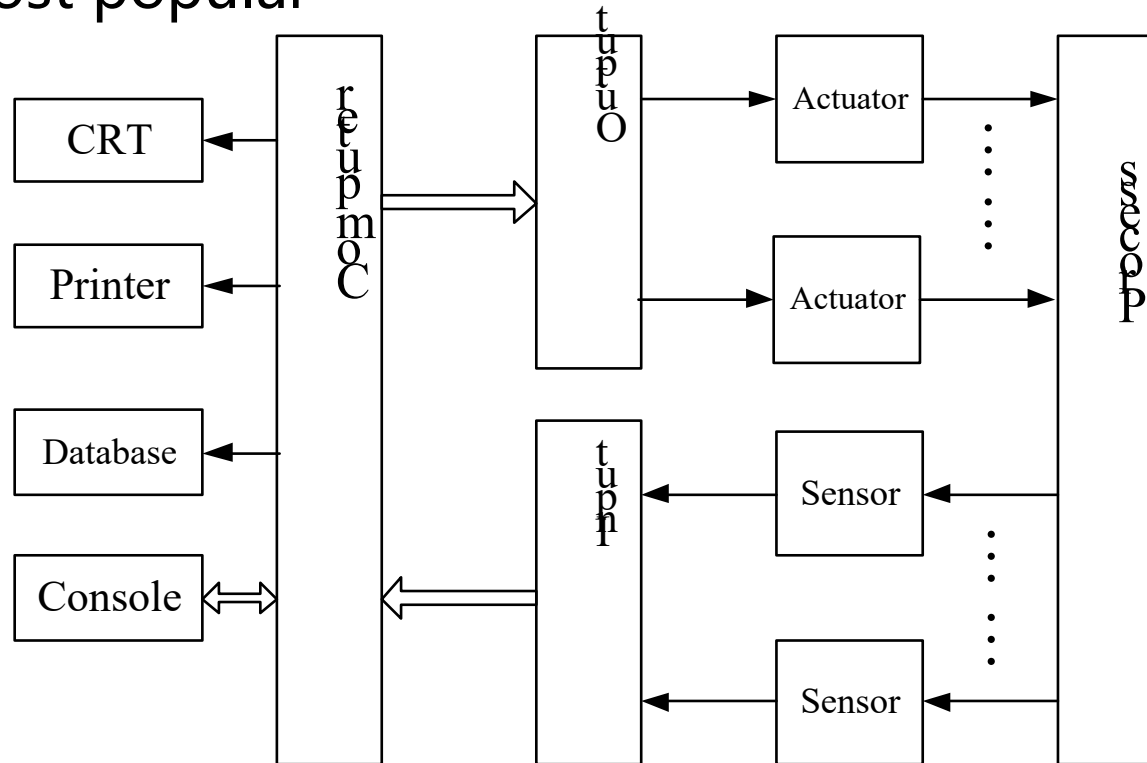
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## 1.3 Categories of digital control systems

- Operation guide control system
  - ▶ Simple, flexible, safe
  - ▶ Slow, single channel
  - ▶ For design and tuning

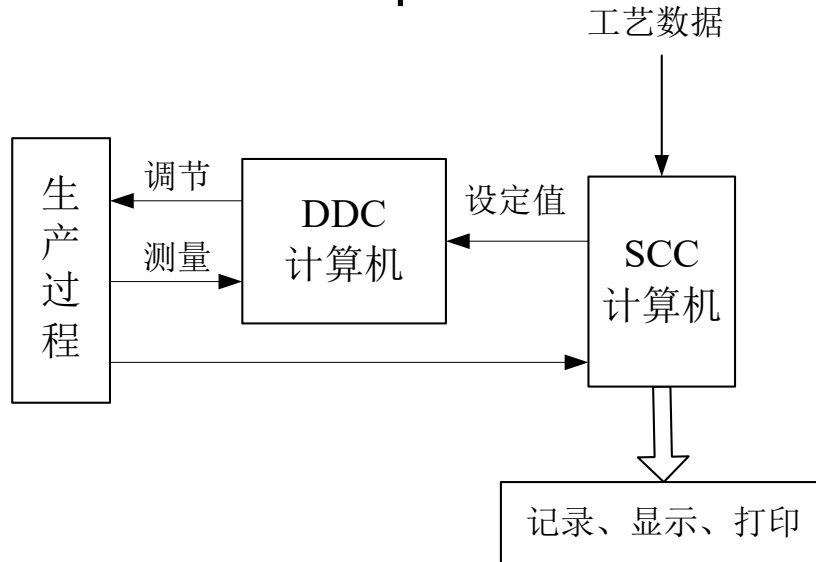


- Direct digital control
  - ▶ Close-loop control system
  - ▶ Multi-control algorithms
  - ▶ Control multi-loops simultaneously
  - ▶ Most popular

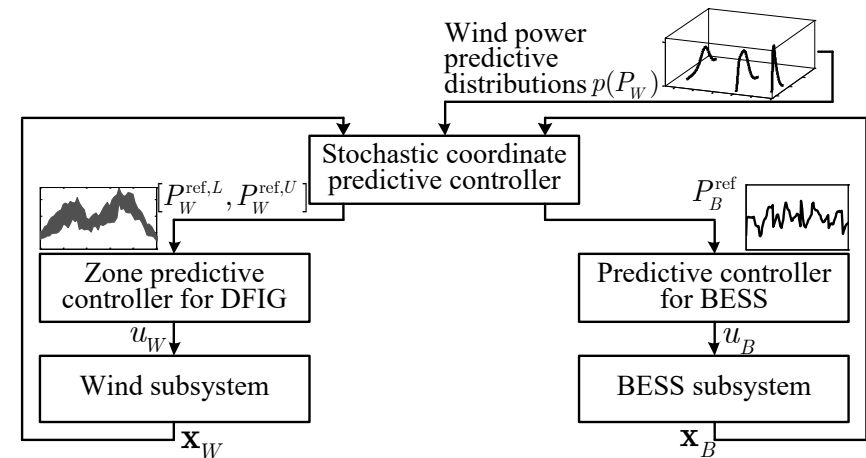


## Supervisory digital control

- ▶ Upper computer control + lower computer control (analog or digital)
- ▶ Upper computer: high-level control and management for **set point control**, sequential control and optimal control
- ▶ Lower computer: **control the process**

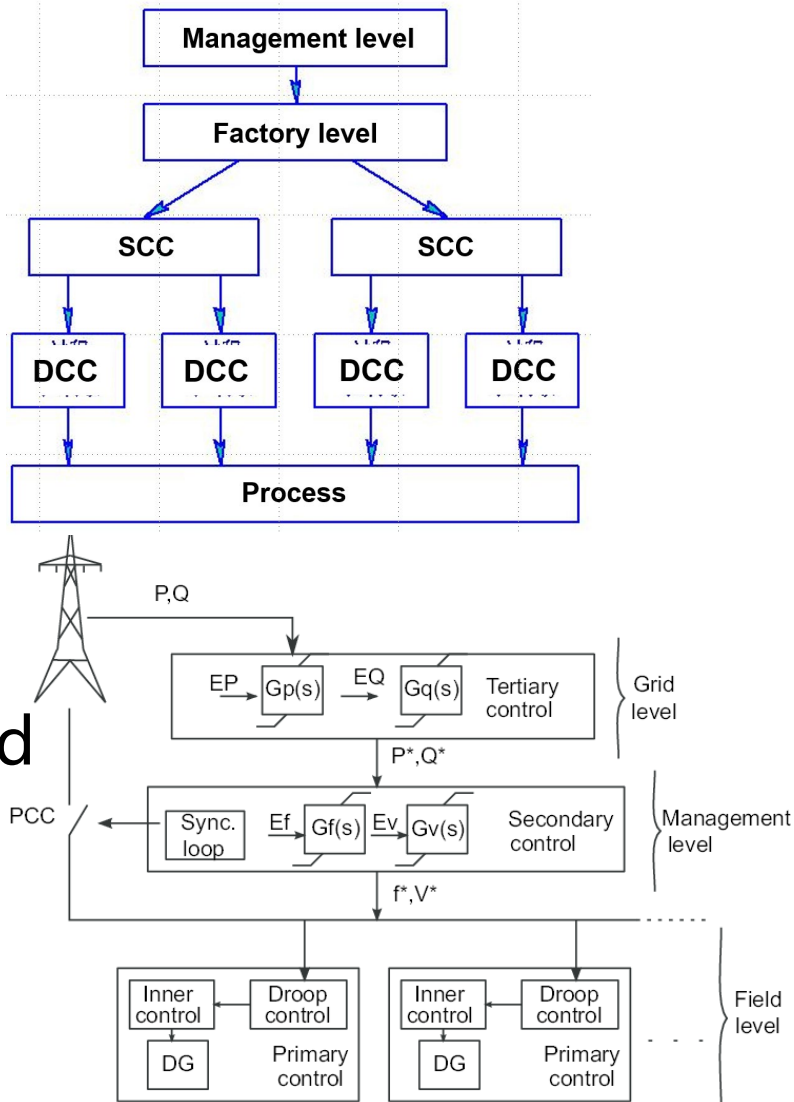


SCC + ACS



Coordinated control of WBHS

## ■ Hierarchical control system



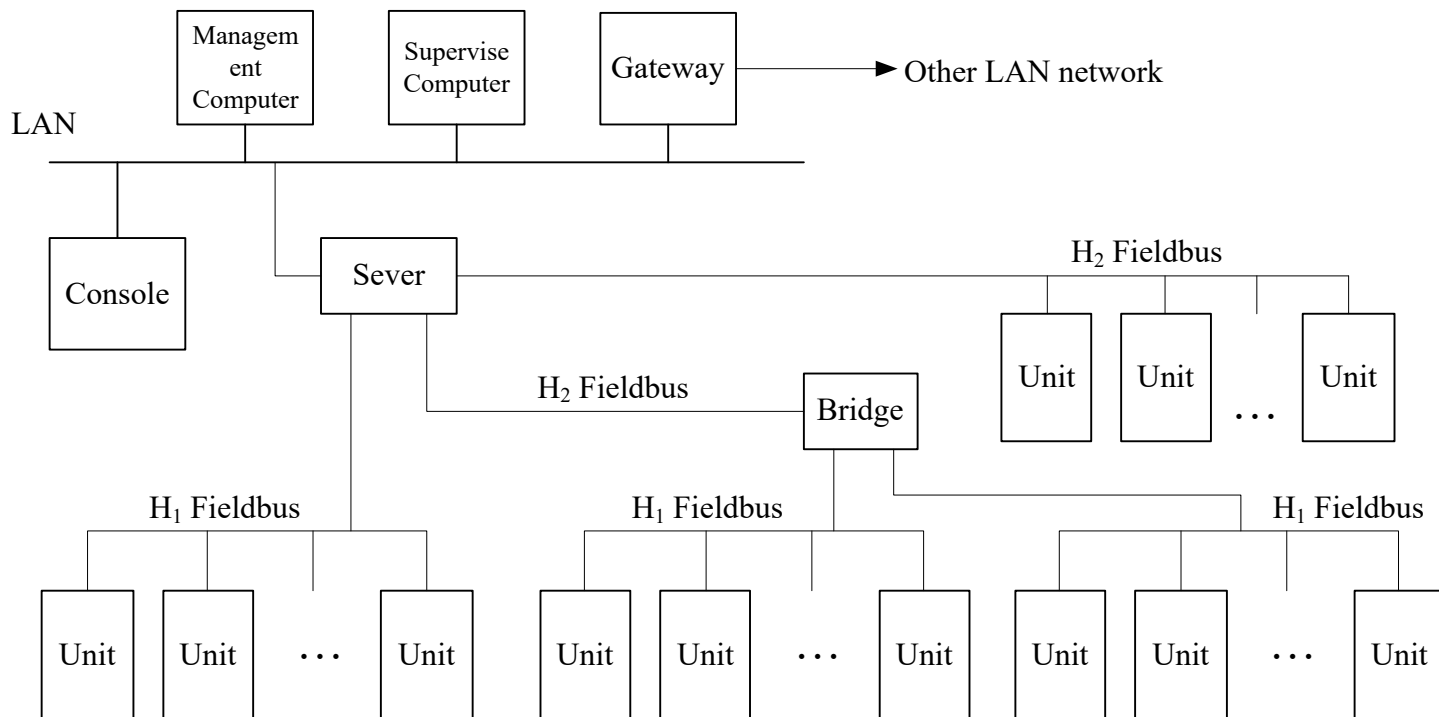
Microgrid  
control

- DCC: for process
- SCC: coordinate and supervise DCCs for shop' s optimal control
- Factory level: make **plan** for the factory and report the data of SCCs and DCCS
- Management level: make **long-term plan**, coordinate the full company and global optimization



## ■ Fieldbus control system

- ▶ Communication technologies and products used in automation and process control industries
- ▶ Reduces the complexity of the control system in terms of hardware outlay



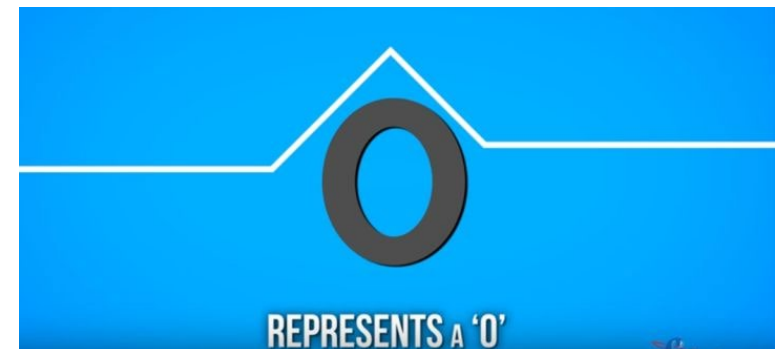
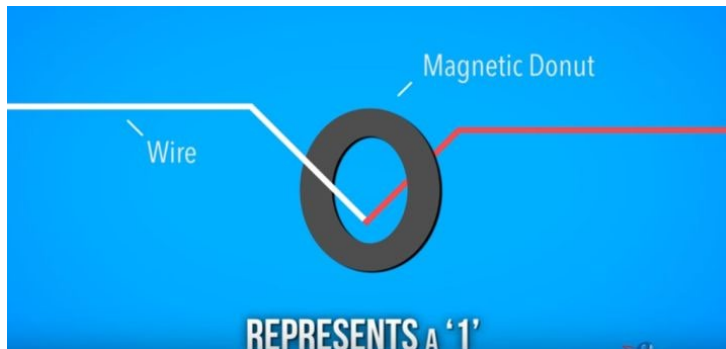
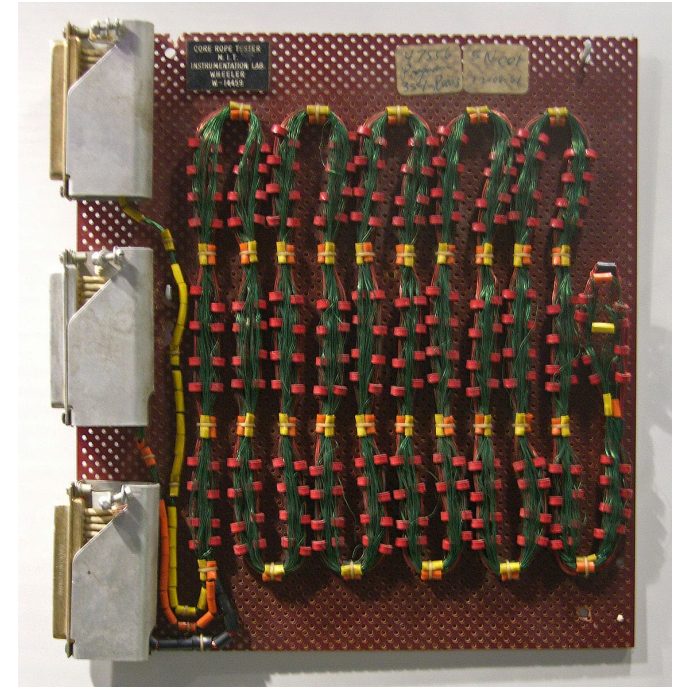
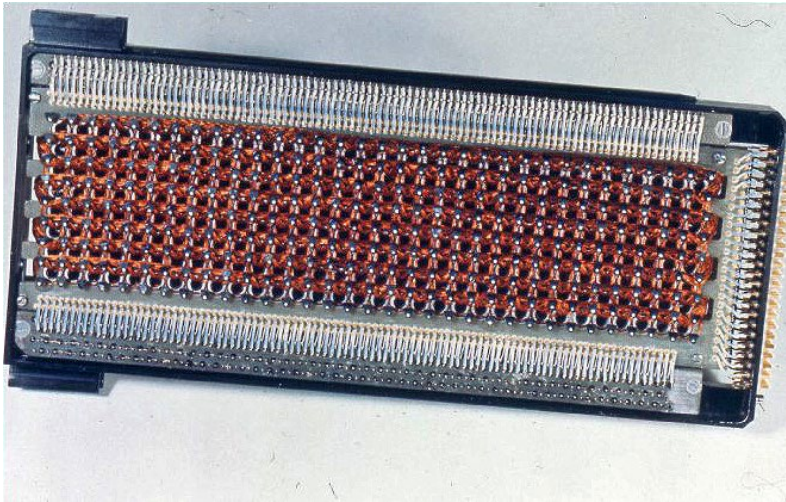
# History of digital control

- 1952-1965: pioneering period
  - ▶ Thomson Ramo Woodridge and Texaco: a computer-controlled system for the polymerization unit in a refinery factory in Texas was designed
  
- 1965-1972: industry application period
  - ▶ Minicomputer
  - ▶ Computer central control



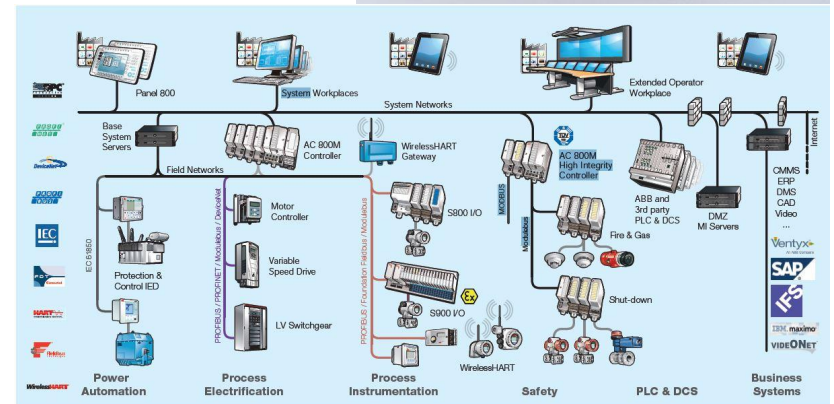
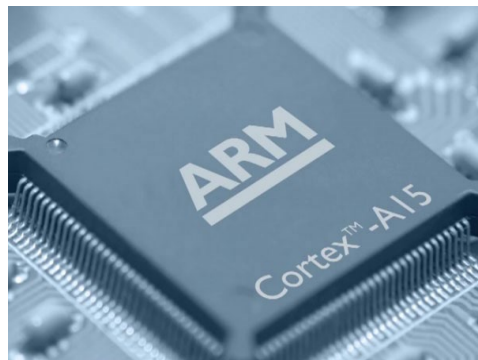
# Core rope memory

- Used in Apollo program (1960-1972)
- Textile worker

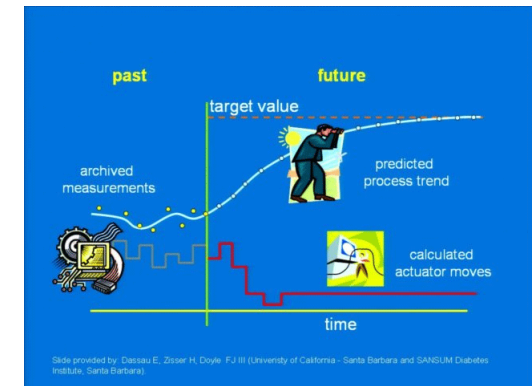


## ■ 1972-: development period

- ▶ Microcomputer period and general use of computer control
- ▶ PLC (Programmable logic controller)
- ▶ Distributed control system
- ▶ Embedded system
- ▶ Network control system
- ▶ Fieldbus system



- The future of the technology related to DCS
  - ▶ Process knowledge
    - Continuous increasing process knowledge
    - System learning
  - ▶ Measurement technology
    - Data merging
    - Soft measurement
  - ▶ Computer technology
    - Computation ability, visualization, communication
    - Programming (Code generation)
  - ▶ Control theory
    - Model predictive control, adaptive control
    - More complex control algorithm
    - Data-driven modeling and control



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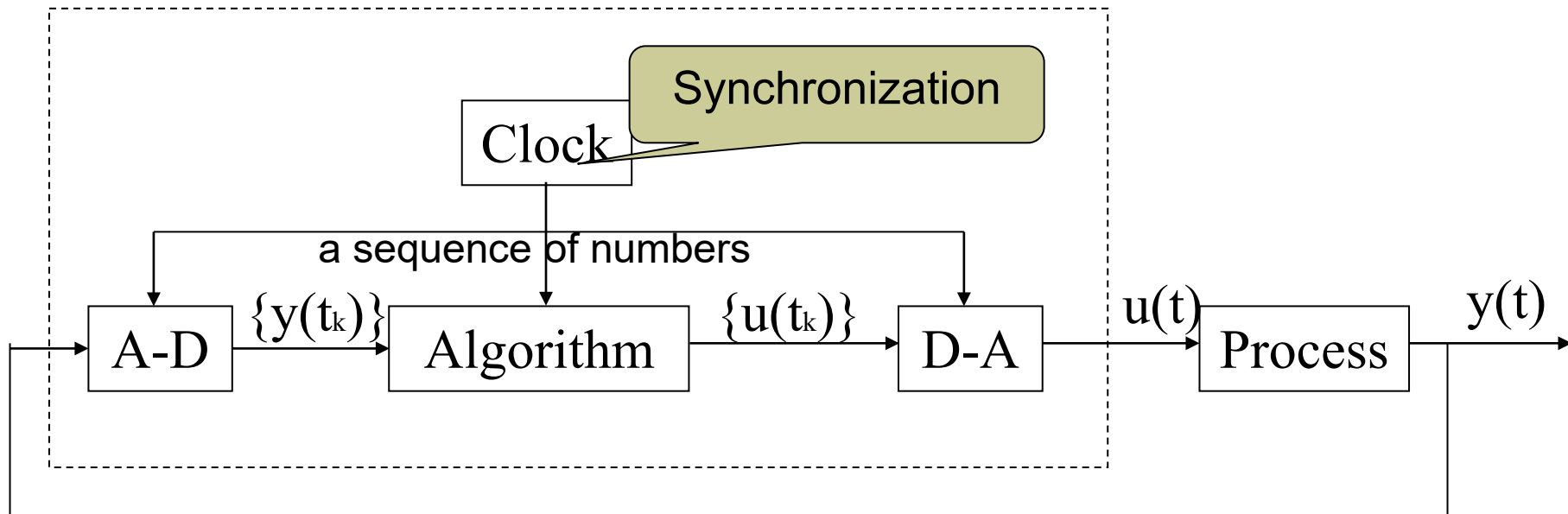
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## 1.4 Digital control theory

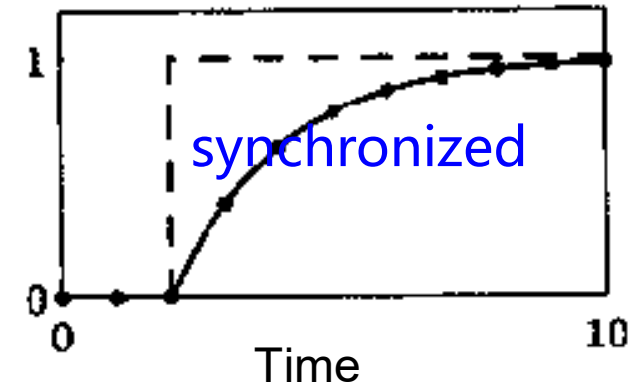
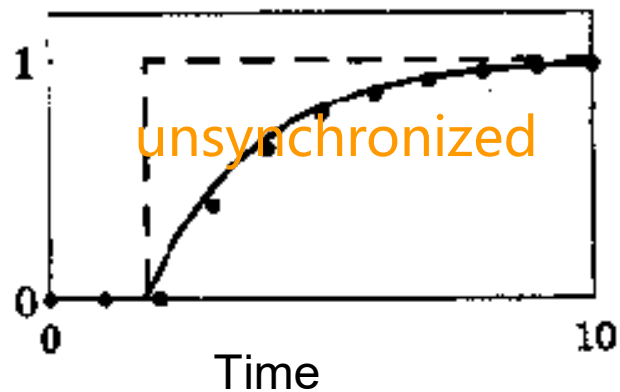
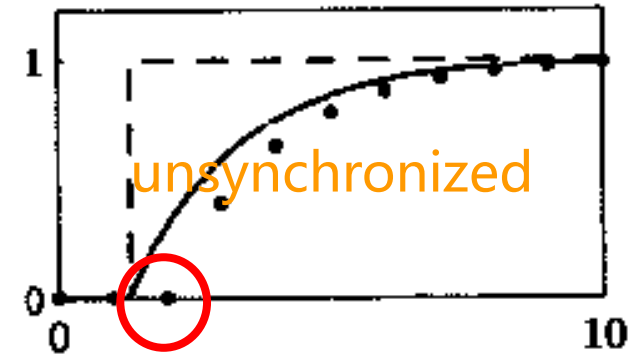
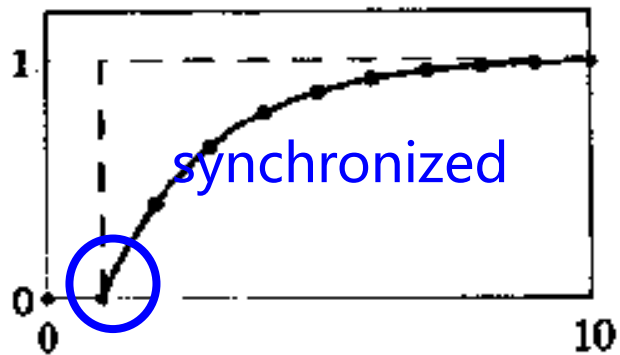
- ▶ Digital control system has its own particular characteristics
- ▶ The theory of analog control system cannot be applied directly

### Synchronize

Example Time dependence in digital controller



► Synchronized and unsynchronized systems





## ■ Phenomena:

- ▶ The figure clearly shows that the sampled system is **not time-invariant** because the response depends on the time when the step occurs.

## ■ Summary:

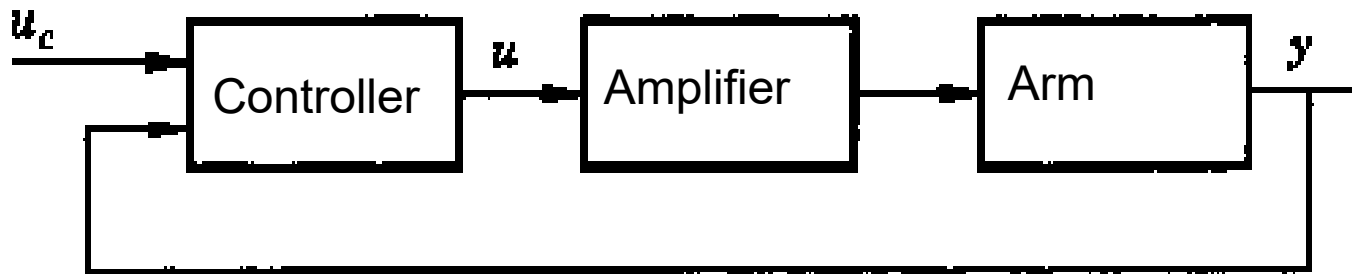
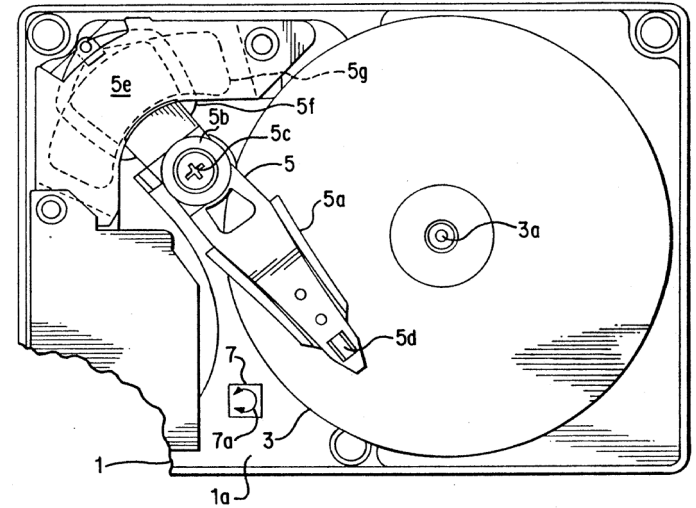
- ▶ The response of the system to an external stimulus will then depend on how the external event is **synchronized** with the internal clock of the computer system.

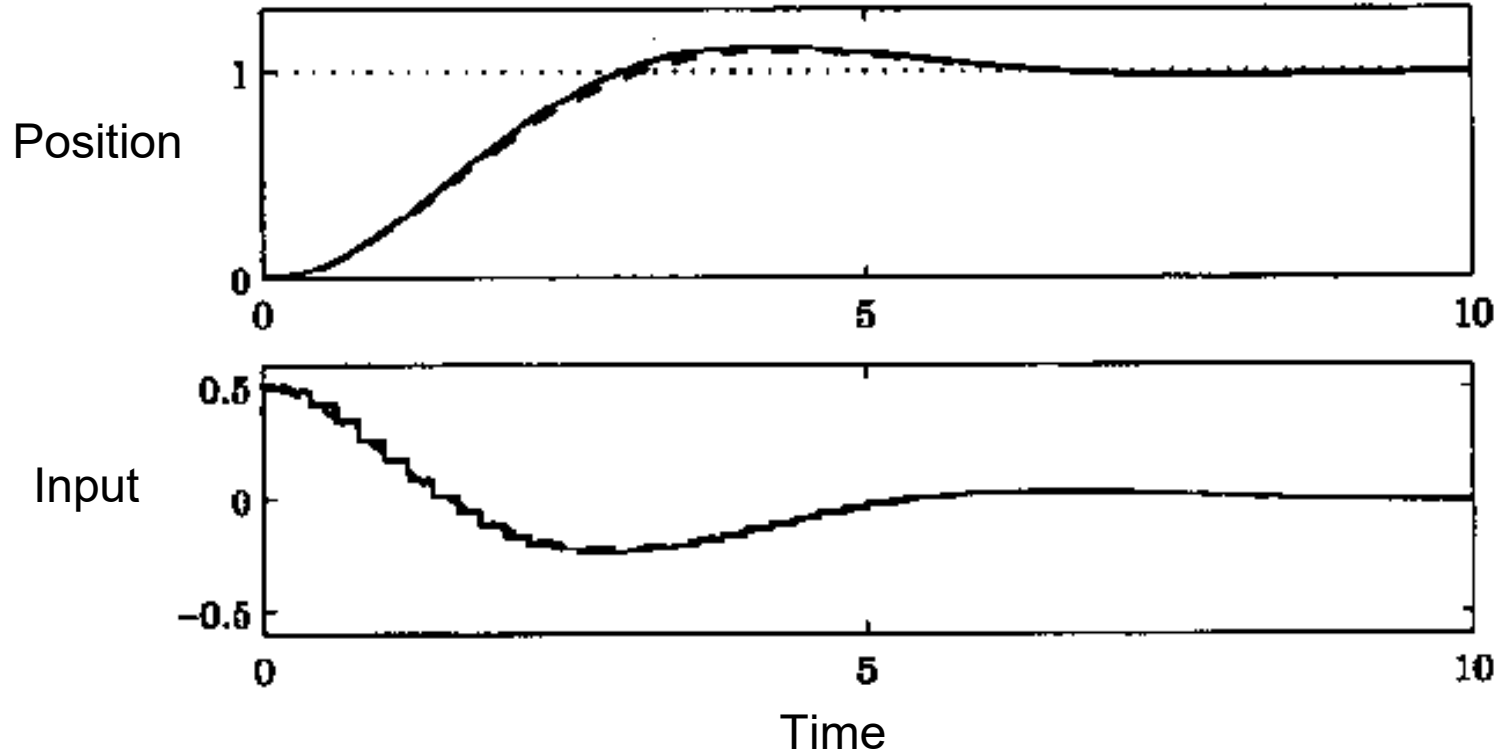


## Sampling interval

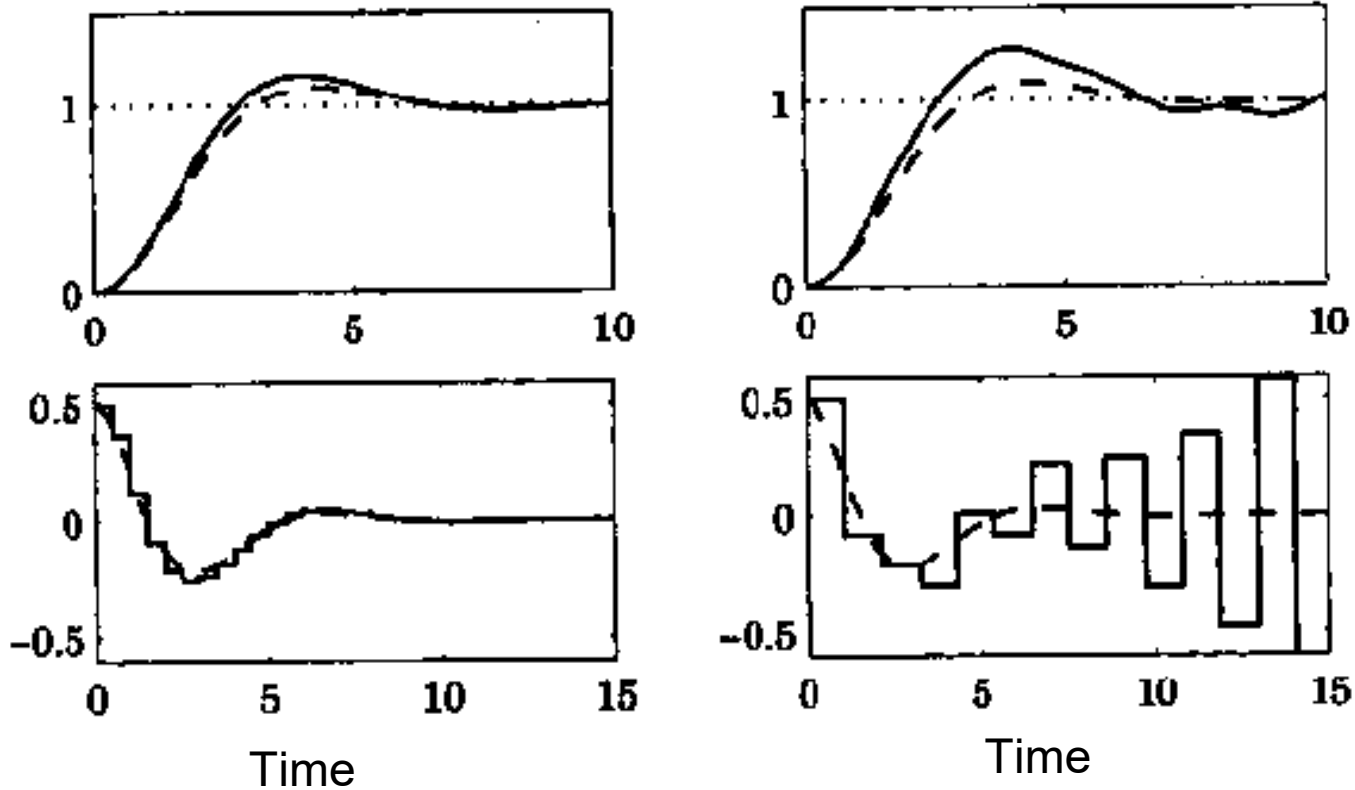
A naive approach to DCS

Controlling the arm of a disk drive





Control inputs and performance of ACS and DCS



Control performance of DCS with different sampling intervals

## ■ Phenomena:

- ▶ When sampling period is very small, the difference between the outputs of the systems is very small.
- ▶ When the sampling period getting longer, the performance of DCS will deteriorate.

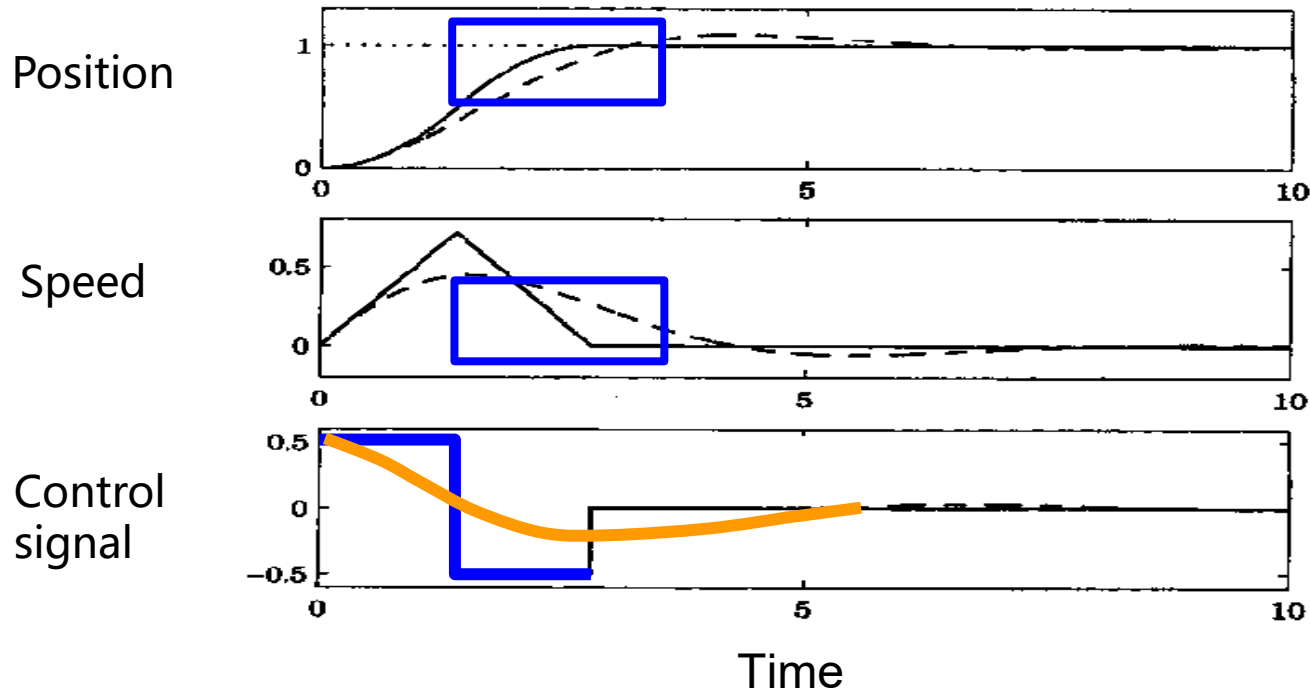
## ■ Summary:

- ▶ The performance and stability of DCS are highly dependent on the sampling interval.



## Deadbeat control

### Disk drive with deadbeat control



Position control using the deadbeat control method

- Phenomena:
  - ▶ The excellent behavior of the DCS.
  - ▶ This behavior cannot be obtained with continuous-time system.
  
- Summary:
  - ▶ This kind of control strategy is called deadbeat control because the system is at rest when the desired position is reached. Such a control scheme, as well as some other advance control schemes, cannot be obtained with a ACS.



## Aliasing

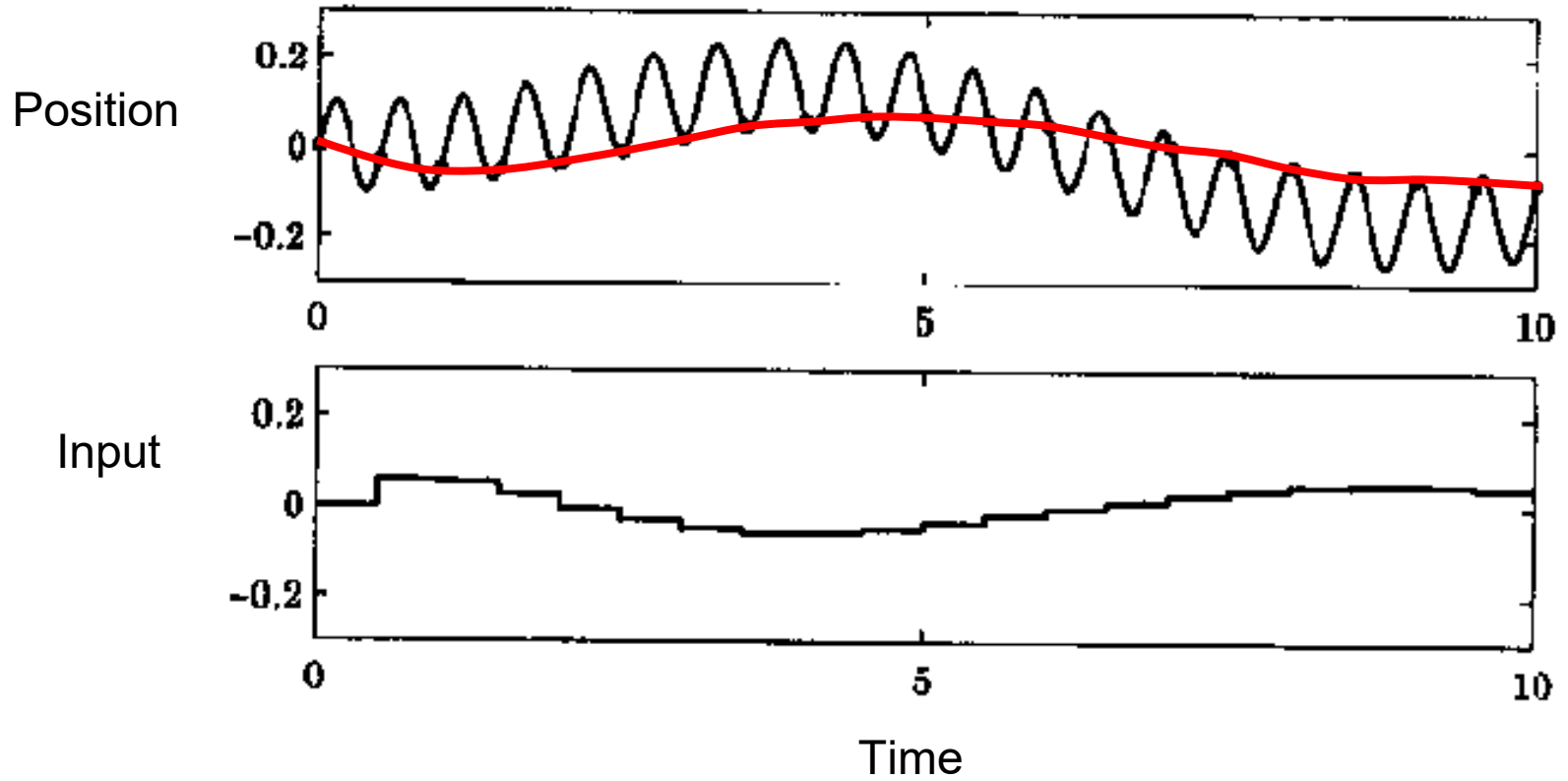
- Aliasing: The phenomenon that the sampling process creates new frequency components.
- Sampling of a signal with frequency  $\omega$  creates signal components with frequencies

$$\omega_{\text{sampled}} = n\omega_s \pm \omega$$

where  $\omega_s$  is the sampling frequency, and  $n$  is an arbitrary integer.







- Phenomena:
  - ▶ Sampling creates new frequencies.
  - ▶ Information distortion.
  
- Summary:
  - ▶ There will be low-frequency components created whenever the sampled signal contains frequencies are larger than half the sampling frequency.



- Presampling filters or antialiasing filters
  - ▶ Nyquist frequency: half of sampling frequency
  - ▶ To avoid the above difficulties, it is essential that all signal components with frequencies higher than the Nyquist frequency are removed before a signal is sampled.
  - ▶ The filters that reduce the high-frequency components of the signals are called antialiasing filter.
  - ▶ These filters are an important component of DCS.
  - ▶ The proper selection of sampling periods and antialiasing filters are important aspects of the design of DCS.

## Conclusion

- ▶ DCS has particular characteristics.
- ▶ DCS have the potential of giving control schemes with behavior that cannot be obtained by ACS.
- ▶ Sampling operation leads to some phenomena that are not found in ACS systems (e.g., aliasing).
- ▶ The selection of the sampling period is important and it is necessary to use anti-aliasing filters.
- ▶ All show that DCS cannot be fully understood within ACS framework, it is thus useful to have other tools for analysis.

**Call for the theory of digital control**



## How theory developed

- The Sampling Theorem
- Difference Equation
- Numerical Analysis
- Transform Methods
- State-Space Theory
- Optimal and Stochastic Control
- System Identification
- Adaptive Control
- Automatic Tuning



## Main contents of this course

- Goal: Understand, analyze and design computer-controlled systems
  - ▶ Sampling and reconstruction
  - ▶ Description of computer-controlled systems
  - ▶ Analysis
  - ▶ Indirect design
  - ▶ Direct design