High Thermoelectric Performance in Two-Dimensional Tellurium: An Ab Initio Study

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Abstract: In 2016, bulk tellurium was experimentally observed as a remarkable thermoelectric material. Recently, two-dimensional (2D) tellurium, called tellurene, has been synthesized and has exhibited unexpected electronic properties compared with the 2D MoS2. They have also been fabricated into air-stable and highly efficient field-effect transistors. There are two stable 2D tellurene phases. One (β-Te) has been confirmed with an ultralow lattice thermal conductivity (κL). However, the study of the transport properties of the other more stable phase, α-Te, is still lacking. Here, we report the thermoelectric performance and phonon properties of α-Te using Boltzmann transport theory and first-principles calculations. A maximum ZT value of 0.83 is achieved under a reasonable hole concentration, suggesting that the monolayer α-Te is a potential competitor in the thermoelectric field.

Key words: tellurene, stability, Seebeck coefficient, strong anharmonicity, thermoelectric material

1. Introduction

Recently, two-dimensional (2D) materials have triggered huge interest due to the striking physical properties related to low dimensionality.1−3 Graphene1 in group IV, borophene in group III,4−6 and black phosphorous in group V7−9 have been extensively investigated experimentally and theoretically. However, research studies related to group VI monolayer materials are still lacking to date.

Recently, Zhu et al.8 firstly have proposed three novel types of monolayer tellurene, namely α-, β-, and γ-Te. Afterwards, tellurene has been synthesized and has attracted lots of interest.8−15 These findings indicate that tellurene possesses unusual physical properties, especially for applications in electronic and thermoelectric devices. Furthermore, Wang et al.10 pointed out that tellurene can be obtained in a very large scale and can be fabricated into air-stable and high-performance field-effect transistors, which makes it different from other 2D materials. Furthermore, tellurene has much larger carrier mobility than that of 2D MoS2.8 Few-layer tellurene also has extraordinary electronic transport properties.10,14,15

β-Te has the intrinsic κL of 2.16 and 4.08 W/(m K) along both directions (300 K)12 and also shows significant anisotropy, indicating good potential in the application of thermoelectric devices with ZT = 0.8.16 Besides, in 2016, bulk tellurium was experimentally observed as a remarkable thermoelectric material.17 Energetically, monolayer α-Te is the most stable structure compared with the metastable β- and γ-Te phases.8 As the most stable phase, α-Te is also a promising one to be synthesized experimentally and has applications in practical nanoelectronics.

Generally, we use ZT to assess the degree of thermoelectric material by ZT = S2σT/(κe + κL), where S means Seebeck coefficient, σ is the electric conductivity, T is the absolute temperature, κe and κL are the electronic and lattice thermal conductivity, respectively. Ideally, one would like to enhance the numerator and weaken the denominator at the same time. Fortunately, one can enhance the scattering of phonons by boundary, defect, isotopic effect, resonant bonding,18 rattle-like scattering,19 lone electron pairs,20 making composite structures,21 and even forming solid solutions.22 Unfortunately, S and σ usually interweave and behave in an opposite trend, which induces the complexity to efficiently realize the waste heat recovery.21

Interestingly, low-dimensional such as 2D materials have the potential to break the above relation between S and σ due to the quantum confinement effect pointed by Dresselhaus et al.3 There are three phases of atomically thin tellurium, namely α-, β-, and γ-Te. The first two are energetically, dynamically, and mechanically stable. Furthermore, α-Te is more stable than β- Te that has an unusually low κL12 and superior thermoelectric
properties. However, relevant works about the $\kappa_i$ and thermoelectric properties of the more stable $\alpha$-Te phase is still lacking. In this letter, we focus on the more stable phase, $\alpha$-Te, and would like to explore its novel electronic and thermal properties. We found that a largest $\kappa_\alpha$ is obtained\textsuperscript{12} and $\sigma$ are the lattice vectors spanning the 2D lattice. (c, d) Electronic band structure and density of states (DOS) of $\alpha$-Te at the HSE06 level. The Fermi levels are set to zero.

2. COMPUTATIONAL METHODS

We use the VASP code and PBE functional.\textsuperscript{23–25} The cutoff energy is 500 eV. To obtain a more accurate electronic band structure and density of states, we use a HSE06 approach.\textsuperscript{26} The van der Waals (vdW) correction proposed by Grimme\textsuperscript{27} was taken into consideration in our calculations. The criterion of convergence energy and force are $10^{-6}$ eV and 1 meV/Å. We use $17 \times 17 \times 1$ k-mesh in the Brillouin zone.

In the framework of Boltzmann transport theory (BTE), the electrical transport properties, such as $\sigma$, $S$, and $\kappa_\alpha$ can be expressed as\textsuperscript{28,29}

$$\kappa_\alpha = \frac{1}{4\pi} \sum_{i,k} \tau_{i}(k)\nu_{i}(k) \otimes \nu_{i}(k)(\varepsilon_{i}(k) - \mu)^n \times \left[ -\frac{\partial f(\mu, T, \varepsilon_{i})}{\partial \varepsilon_{i}} \right]$$

(1)

$$\sigma = e^2 K_0$$

(2)

$$S = \frac{1}{\pi^2} K_0 K_0^{-1}$$

(3)

$$k_\alpha = \frac{1}{T} (K_{2} - K_{1} T K_0^{-1})$$

(4)

where, $\tau_{i}(k)$ and $\varepsilon_{i}$ are the electronic relaxation time and energy eigenvalue. $k_\alpha$ can be obtained based on the tensor $\kappa_\alpha$.

The in-plane $\kappa_{\parallel\parallel}$ under relaxation time approximation can be obtained\textsuperscript{12}

$$\kappa_{\parallel\parallel} = \frac{1}{V} \sum_{j} C_{ij} n_{ij} v_{ij} f_{ij}$$

(5)

where the meaning of each parameter is explained elsewhere.\textsuperscript{12} We use Phonopy\textsuperscript{30} and ShengBTE\textsuperscript{31} to deal with the harmonic and anharmonic force constants. We use eq 4 to calculate the electronic thermal conductivity $k_\alpha$ since sometimes the results from the Wiedemann–Franz law is unreasonable, such as in metallic VO$_2$.\textsuperscript{32} Clean graphene near the charge neutral point,\textsuperscript{33} and single-electron transistor.\textsuperscript{11} As a matter of fact, the Wiedemann–Franz law is only suitable for the system where the scattering of electrons in the material is dominated by the elastic collision ("good metal").\textsuperscript{35} Therefore, we use the definition to calculate $k_\alpha$. It should be noted that an effective thickness should be defined to calculate the electronic and thermal properties for 2D materials. The thickness of $\alpha$-Te is 7.74 Å, whose definition is clearly defined elsewhere.\textsuperscript{12,36}

3. RESULTS AND DISCUSSION

The optimized structure of $\alpha$-Te is shown in Figure 1a,b with a lattice constant of 4.238 Å obtained by PBE+U functional. The $\alpha$-Te possesses a P3M1 (164) symmetry group belonging to the trigonal system and isotropic pattern in the 2D plane, which is quite different from the anisotropic bulk Te\textsuperscript{37} and 2D $\beta$-Te.\textsuperscript{5,12} From the top and side views, $\alpha$-Te and sandwiched 1T-MoS$_2$ look alike in many ways. The intermediate Te atom is octahedrally coordinated to six neighboring Te atoms and upper and lower Te layers form the A–B like stacking. The coordination numbers in outer and centered Te are 3 and 6, which is characteristic of the multivalency formation of the Te atom located in the near-bottom of the periodic table. The bond length in $\alpha$-Te is all 3.04 Å, which is larger than those of 2.77 and 3.03 Å (two types of bonds) in monolayer $\beta$-Te.\textsuperscript{12}

Bulk Te was reported to be a direct semiconductor ($E_g = 0.25$ eV)\textsuperscript{37} and it also has recently been experimentally observed as a remarkable thermoelectric material.\textsuperscript{17} Figure 1c,d shows the electronic band structure and density of states (DOS) of $\alpha$-Te, indicating a near-direct band gap material ($E_g = 1.11$ eV) at the HSE06 level. Our result is very consistent with the previous theoretical work.\textsuperscript{9}

A good thermoelectric material not only needs a minimum thermal conductivity, but also requires a simultaneously maximum power factor (PF). However, Seebeck $S$ and $\sigma$ are usually inter-weaved. A large $S$ requires a large carrier effective mass decided by\textsuperscript{38}\textsuperscript{39} $S = \frac{8\pi^2 k_B^2 T^3 m^*(T)}{3e}$ in 3D semiconducting materials, but $\sigma$ is inversely proportional to the carrier effective mass due to $\mu = \frac{e}{m^*}$. In 1993, Hicks and Dresselhaus proposed a seminal idea that improves the energy dependence of the DOS in 1D and 2D systems to alleviate the coupling between $S$ and $\sigma$, consequently enhancing the PF.\textsuperscript{39,40} Mahan and Soto further generalized it to a refined sentence.\textsuperscript{41} Afterwards, these guiding principles triggered two interesting band structure shapes. One is the "pudding-mold"\textsuperscript{42,43} and the other one is the "Mexican-hat-shape".\textsuperscript{44} Recently, backward thinking has emerged, which introduces quasi-one-dimensional electronic band dispersions in 2D or 3D materials to increase the thermoelectric performance.\textsuperscript{45,46} A relatively flat band means a large DOS in a narrow energy region near the Fermi level. The dispersive band leads to a large carrier velocity, and also indicates a small $m^*$ and therefore a high $\mu$.\textsuperscript{47–50}
Interestingly, the valence bands near the Fermi level of $\alpha$-Te shown in Figure 1c has some hole pockets and relatively flat bands, which are characteristic of good thermoelectric properties and are similar to renowned PbTe$_{1-x}$Se$_x$ thermoelectrics.\(^5\)

On the basis of the band structure, we could evaluate $S$, $\sigma$, and $\tau$ of $\alpha$-Te. Since the melting point of tellurium is 723 K, we select three typical temperatures (300, 500, and 700 K) in the whole calculations. Figure 2a shows the Seebeck coefficient $S$ in the n- and p-type of $\alpha$-Te as a function of carrier concentration. Overall, the absolute values of $S$ decrease for both n- and p-type when increasing the carrier concentration, which reflects the inverse proportion between $S$ and carrier concentration $n$. Moreover, the absolute value of $S$ of hole doping is bigger than the electron doping in $\alpha$-Te. For instance, the value of $|S|$ for the n-type is 242.9 $\mu$V/K at $10^{12}$ cm$^{-2}$ carrier concentration at 500 K temperature, only around half of p-type 529.6 $\mu$V/K at the same conditions. The maximum value $S$ of p-type $\alpha$-Te is around 700 $\mu$V/K at room temperature, which is the double of that of 350 $\mu$V/K in bulk tellurium.\(^17\) This is the physical reason that the ZT of $\alpha$-Te are comparable with bulk tellurium, although the $\kappa_t$ in $\alpha$-Te (9.85 W/(m K)) is around 7 times of that in bulk tellurium (1.5 W/(m K)).\(^17\) In this sense, if one further increases the phonon scattering using some defects and isotope effect in $\alpha$-Te, the $\kappa_t$ will decrease but with the same level of Seebeck coefficient $S$. Then the ZT of $\alpha$-Te will be significantly enhanced and will surpass the bulk tellurium.\(^17\)

The difference between electron and hole doping in Seebeck $S$ originates from the electronic band structure and DOS in Figure 1c,d. As we discussed above, $S$ is primarily regulated by the effect mass $m^*$ and the magnitude of DOS. A more smooth valence band (hole doping) compared with a conduction band (electron doping) corresponds to a larger carrier $m^*$, indicating a large $S$ since $S$ is proportional to $m^*$. Furthermore, DOS of p-type is obviously much larger than n-type of $\alpha$-Te around the Fermi level shown in Figure 1d. These evidences verify the superior performance of the hole doping compared with the electron doping in $\alpha$-Te.

According to the BTE, the electronic conductivity $\sigma$ is dependent and is proportional to the relaxation time $\tau$. Therefore, a reasonable relaxation time $\tau$ should be chosen. As a matter of fact, $\tau$ in materials is a function of temperature and carrier concentration. So far, experimental measurement may be the only effective way to solve this issue. For theoretical calculations, $\tau$ is difficult to obtain with high precision. Specifically, there are mainly three methods, such as using a designated $\tau$ based on relevant experiments,\(^{52,53}\) electro-
In contrast to the Seebeck $S$, electronic conductivity $\sigma$ increases with the increasing carrier concentration. Figure 2b shows a larger $\sigma$ of electron doping compared with hole doping at the same carrier concentration due to the smaller effective mass ($0.107m_e$ for electrons and $<0.164m_e$ for holes). Furthermore, $\sigma$ of two type $\alpha$-Te are insensitive to temperature, which is similar to that of $\beta$-Te.\(^{16}\)

A high PF needs a large $S$ and a large $\sigma$ simultaneously. One should compromise between the decreasing function of $S$ and increasing function of $\sigma$. The calculated power factor $(S^2\sigma)$ that can demonstrate the thermoelectric performance of $\alpha$-Te is shown in Figure 2c. The PF for both types first increase, climb the summit at moderate carrier concentrations, and then decrease when increasing the concentration. The p-type PF is significantly larger than n-type of $\alpha$-Te, though they exhibit a similar trend dependent on the carrier concentration. For instance, the maximum PF of holes and electrons are 74.6 mW/(m K\(^2\)) at 6.12 $\times$ 10\(^3\) concentration and 21.2 mW/(m K\(^2\)) at 2.86 $\times$ 10\(^3\) concentration at 500 K. The former one is around 2.5 times larger than that of the latter one and is 2 times larger than 2D SnSe.\(^ {56}\)

More interestingly, the maximum PF of bulk tellurium at room temperature is around 1.3 mW/(m K\(^2\)), which is around a 10th of that in $\alpha$-Te (12 mW/(m K\(^2\))) at the similar conditions shown in Figure 2c. The physical reason behind it is the very small effective mass $m^*$ of $\alpha$-Te. The $m^*$ of standard 2H-MoS\(_2\) is 0.47$m_e$ for electrons and 0.58$m_e$ for holes.\(^ {8}\) However, in $\alpha$-Te, the $m^*$ is 0.107$m_e$ for electrons and 0.164$m_e$ for holes. Obviously, the effective mass of carriers in $\alpha$-Te is quite smaller than 2H-MoS\(_2\). A smaller $m^*$ will result in a larger electronic conductivity, qualitatively decided by the simple model: $\sigma = \frac{e^2}{m^*}$. Moreover, Liu et al.\(^ {14}\) pointed out that lone-pair electrons in bulk Te will significantly enhance the interchain electronic transport. Similarly, the coordination

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**Figure 3.** (a) Phonon spectra and DOS of $\alpha$-Te. (b) Intrinsic lattice thermal conductivity $\kappa_\alpha$ as a function of temperature. Blue dashed line is $T^{-1}$ fitting. The values of relaxation time approximation (RTA) are also shown by red dots. (c) Normalized contributions to total $\kappa_\alpha$ of phonon branches from 100 to 700 K. (d) Frequency-resolved $\kappa_\alpha$ at room temperature. (e) Room temperature $\kappa_\alpha$ as a function of sample size. (f) Cumulative $\kappa_\alpha$ as a function of phonon mean free path (MFP) at room temperature. The fitted curve is plotted in a dashed line.
number in α-Te is 3 for the outer Te atoms, which is only half of valence electrons in Te atoms (group VI). Therefore, for each outer Te atom there exist 3 lone-pair electrons. These lone-pair electrons will enhance the hopping terms between electrons and contribute to the superior electronic transport properties in α-Te.6,14

An optimal ZT also needs a minimum thermal conductivity (κ_e + κ_i). For electronic thermal conductivity, κ_e has been discussed in the computational methods. Next, we would like to explore the phonon transport properties of α-Te, as phonon dominates the thermal transport in semiconductors. The calculated phonon dispersions are shown in Figure 3a. Firstly, it shows that all phonon branches are free from negative frequency and this result confirms the dynamical stability of α-Te. Moreover, there is no phonon gap between acoustic and optical branches, indicating a strong optical-acoustic phonon coupling.12,63 Furthermore, there is no phonon gap between acoustic and optical branches, indicating a strong optical-acoustic phonon coupling which will suppress the κ_L of materials.

A high-order (≥3) scattering of phonons leads to a limited κ_L.58,59 Figure 3b shows the intrinsic κ_L computed with both noniterative and iterative method from 100 to 700 K. We note that both methods give similar trends of κ_L in the whole temperature range. However, the iterative method always gives values of κ_L higher than the noniterative method at the same temperature. We choose the values of the iterative method in the following discussion. We found that the κ_L of α-Te can be well described by the T^{-1} curve. This phenomenon is also found in bulk Te17 and β-Te.12 The value of intrinsic κ_L is 9.85 W/(m K) (300 K), which is twice as much as that of β-Te at the same temperature.12 Furthermore, κ_L of α-Te is also larger than bulk Te (2.77 W/(m K)),12 which is consistent with the familiar trend (κ_{2D} > κ_{3D}).12,60,61

The normalized contribution of ZA, TA, LA, and optical branches varying with temperature are plotted in Figure 3c, in which each mode varies little at different temperatures especially beyond 200 K, and can be regarded as independent of temperature, similar to the β-Te.12 At room temperature, three acoustic branches contribute about 90% to the total intrinsic κ_L, whereas the summation of all optical phonons is only 10%. Furthermore, the proportions of contributions to total κ_L are about 25, 47, and 17% for LA, TA, and ZA phonons, in which the ZA mode is the smallest one among the three acoustic branches in α-Te, quite different from graphene, where the proportion of the ZA mode is about 75%.64

It was reported that there is a symmetry selection rule in flat graphene that only even number of ZA modes can be involved in scattering processes.65,66 This rule originates from the reflection symmetry about the c axis in the structure. The thermal resistance roots in the high order of phonon scattering. Due to the selection rule, the ZA mode contributes mainly to the κ in graphene. However, the lattice does not have reflection symmetry about the c axis in α-Te. As a result, the selection rule is broken and the importance of the ZA mode in the thermal transport of α-Te is much lower than graphene.

Moreover, it is worthwhile to explore the contribution of phonons with different frequencies to the total κ_L. Here, the frequency-resolved κ_L for α-Te at 300 K is displayed in Figure 3d. It can be found that the main contribution originates from acoustic phonons with frequencies lower than 2 THz, whereas the contribution of optical phonons is very small. This is consistent with Figure 3c. Furthermore, the acoustic phonons with very low frequency (lower than 1 THz) contribute most to κ_L. In the following, we will find the reason behind this is that the phonons around the Γ point usually possess a large phonon relaxation time.

All samples of material have finite size in practical experiment and device application, thus the additional boundary scattering will reduce κ_L especially at nanoscale or at low temperatures. Usually, in nanostructures, κ_L related to boundary scattering can be evaluated as12,61

![Figure 4](image-url)

**Figure 4.** (a) The frequency dependent behavior of the square group velocity at 300 K for α-Te. All optical phonon branches are in purple. (b) Phonon relaxation time of ZA, TA, LA, and optical phonon branches as a function of frequency at room temperature. (c) Mode-Grüneisen parameter and (d) phase-space volume P_3 for three-phonon scattering processes.
where, $L$ is the size of the material. This formula represents the situation for a completely diffusive boundary scattering of phonons. Cumulative $\kappa_{L}(\langle\Lambda<\Lambda_{\text{max}}\rangle)$ can also be used to study the size effect, whose definition has been defined elsewhere.\textsuperscript{31} Figure 3e shows the size dependence of $\kappa_{L}$ for $\alpha$-Te with completely diffusive boundary scattering at room temperature and the cumulative $\kappa_{L}$ is displayed in Figure 3f. As shown in Figure 3e, $\kappa_{L}$ becomes lower while the sample size becomes smaller, as the boundary scattering becomes larger. For a specific example, when the sample size is 1 $\mu$m, $\kappa_{L}$ can be suppressed to 7.56 W/(m K), about 78\% of value for the infinitely large system. When the sample size is 10 $\mu$m, $\kappa_{L}$ reaches 91\% of the infinitely large system. This implies that the size effect always maintains until about 10 $\mu$m, such as 2D WTe\textsubscript{2}.\textsuperscript{65}

The size effect can also be estimated from the cumulative $\kappa_{L}$ as a function of MFP shown in Figure 3f. We can find that the MFP range of phonons that contribute significantly to $\kappa_{L}$ is about 10 nm to 10 $\mu$m, which is consistent with our previous result in Figure 3e. To obtain the representative MFP, we fit cumulative $\kappa_{L}$ using a single parametric function: $\kappa(\Lambda=L_{\text{max}}) = \kappa_{\text{max}}/(1+\Lambda_{0}/\Lambda_{\text{max}})$, where $\kappa_{\text{max}}$ is $\kappa_{L}$ of infinite size and $\Lambda_{\text{max}}$ is the maximal MFP. The fitting parameter $\Lambda_{0}$ can be interpreted as the typical MFP with which the phonons contribute significantly to $\kappa_{L}$. The fitted curve is shown in Figure 3f by a dashed line. The parameter $\Lambda_{0}$ is 94 nm, which could be interpreted as the representative MFP of $\alpha$-Te. This implies that the $\kappa_{L}$ of $\alpha$-Te may decline sharply with the sample size of hundreds of nm. This property is propitious to the electronic and thermoelectric materials based on $\alpha$-Te in the nanoscale.\textsuperscript{10}

Group velocity of phonon has great effects on thermal transport of materials, as it is proportional to $v^{3}$ based on eq 3. The calculated $v$ with different frequencies are shown in Figure 4a. The LA branch possesses the highest $v$ among the three acoustic branches, specifically more than two times of that for ZA and TA phonons. The optical phonons around 3.7 THz has the largest $v$, but they only contribute 10\% to total $\kappa_{L}$. Here, $v$ is also displayed in Figure 4b. $\tau$ around $\Gamma$ point has the magnitude of $10^{7}$–$10^{8}$ ps but $\tau$ of most phonons with a frequency of more than 5 THz is about 0.1–10 ps. This is the reason why phonons with very low frequency dominate the thermal transport in $\alpha$-Te (Figure 3d). Furthermore, $\tau$ of the TA branch is the largest of all, about $10^{9}$ ps around the $\Gamma$ point.

This is the reason why the TA mode contributes most to $\kappa_{L}$ even more than LA phonons (Figure 3c). It can also explain that optical phonons contribute little to $\kappa_{L}$ since most of them have ultralow $\tau$ of only 1–10 ps.

The Grünerisen parameter provides crucial information on the anharmonic interactions of phonons. $\gamma$ in $\alpha$-Te for the whole frequency spectrum is displayed in Figure 4c. $\gamma$ of TA and LA modes are in the range of 0–2, whereas those of optical modes are 1–6. Comparing with $\beta$-Te, $\gamma$ of $\alpha$-Te are smaller, indicating a lower anharmonicity and a higher $\kappa_{L}$. Interestingly, it can be found that $\gamma$ of acoustic and optical phonon modes have suddenly dropped around 2–2.5 THz. Since there is no acoustic-optical phonon gap, the large acoustic-optical phonon scattering would lead to a giant $\gamma$ and is also the source of ultralow $\kappa_{L}$ in $\beta$-Te.\textsuperscript{14} In the three-phonon scattering process, all phonon modes must satisfy the conservation of energy and momentum simultaneously.\textsuperscript{36} The quantitative probability of all available three-phonon scattering in $\alpha$-Te are shown in Figure 4d. This $P_{3}$ phase space is 1 order smaller than that of $\beta$-Te, indicating a weaker anharmonicity of $\alpha$-Te compared with $\beta$-Te.\textsuperscript{12}

On the basis of the above results, intrinsic figure of merit $ZT$ can be evaluated and is exhibited in Figure 5. The climax $ZT$ at 700 K are 0.57 and 0.83 for electron and hole doping $\alpha$-Te, which is as high as $\beta$-Te\textsuperscript{16} and has the same order of bulk Te.\textsuperscript{17} Room temperature $ZT$ of $\alpha$-Te is 0.54. Our calculation suggests that monolayer $\alpha$-Te is a promising thermoelectric material. Furthermore, it can be promoted further via suppressing $\kappa_{L}$ such as the grain boundary, isotope effect, and vacancy.\textsuperscript{10}

4. CONCLUSIONS

In summary, we have systematically studied the extraordinarily high thermoelectric performance of monolayer $\alpha$-Te by the ab initio calculations. To explain the high $ZT$, we consider the electronic and thermal transport properties. A large and asymmetric electronic density of states induce relatively flat bands, leading to a large Seebeck coefficient $S$. A small effective carrier mass $m^{*}$ of CBM (VBM) will result in a larger electronic conductivity $\sigma$. Combining both, the PF in $\alpha$-Te (12 mW/(m K\textsuperscript{2})) exhibits 10 times as large as that in bulk tellurium (1.3 mW/(m K\textsuperscript{2}))\textsuperscript{17} at the similar conditions. For lattice thermal conductivity $\kappa_{L}$, $\alpha$-Te consists of heavy atomic mass, which breeds low harmonic properties, such as low group velocities. For anharmonicity, strong phonon anharmonic scattering rates including acoustic-optical phonon scattering bring about the same order of magnitude $\kappa_{L}$ of $\alpha$-Te.
Te compared with the bulk Te and $\beta$-Te. The superior electronic properties and suitable $\kappa_s$ combine together leading to the ultrahigh $ZT$ in $\alpha$-Te. A maximum $ZT$ of 0.83 is achieved with a reasonable hole concentration at 700 K. Our results indicate that monolayer $\alpha$-Te is a promising thermoelectric material. We hope that $\alpha$-Te, more stable than $\beta$-Te, would be experimentally observed with high $ZT$ in the near future.

**ASSOCIATED CONTENT**

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Electronic band structure and effective mass around conduction band minimum and valence band maximum of two-dimensional tellurium (PDF)

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**Notes**

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