

# Supporting Information for: Insight into Two-Dimensional Borophene: Five-Center Bond and Phonon-Mediated Superconductivity

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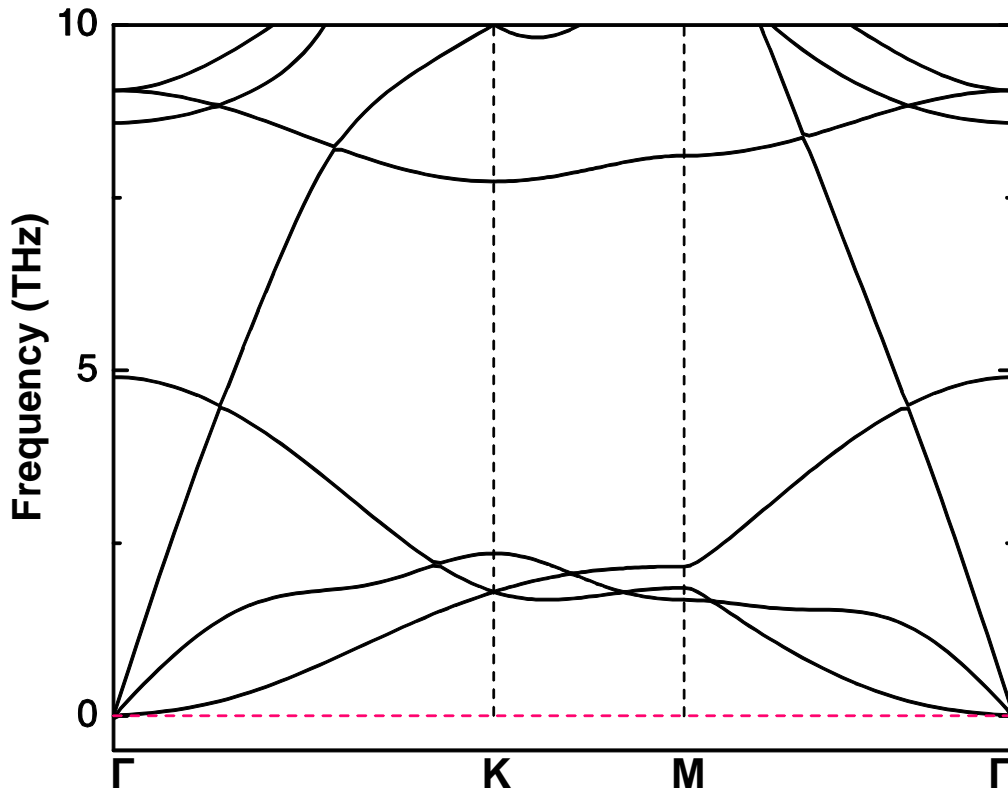


Figure S1: Amplification of phonon dispersion of super-B below 10 THz. Around the  $\Gamma$  point, there are two linear LA and TA acoustic phonon branches, and a parabolic ZA mode. All frequencies are free from imaginary, confirming the dynamical stability of super-B.

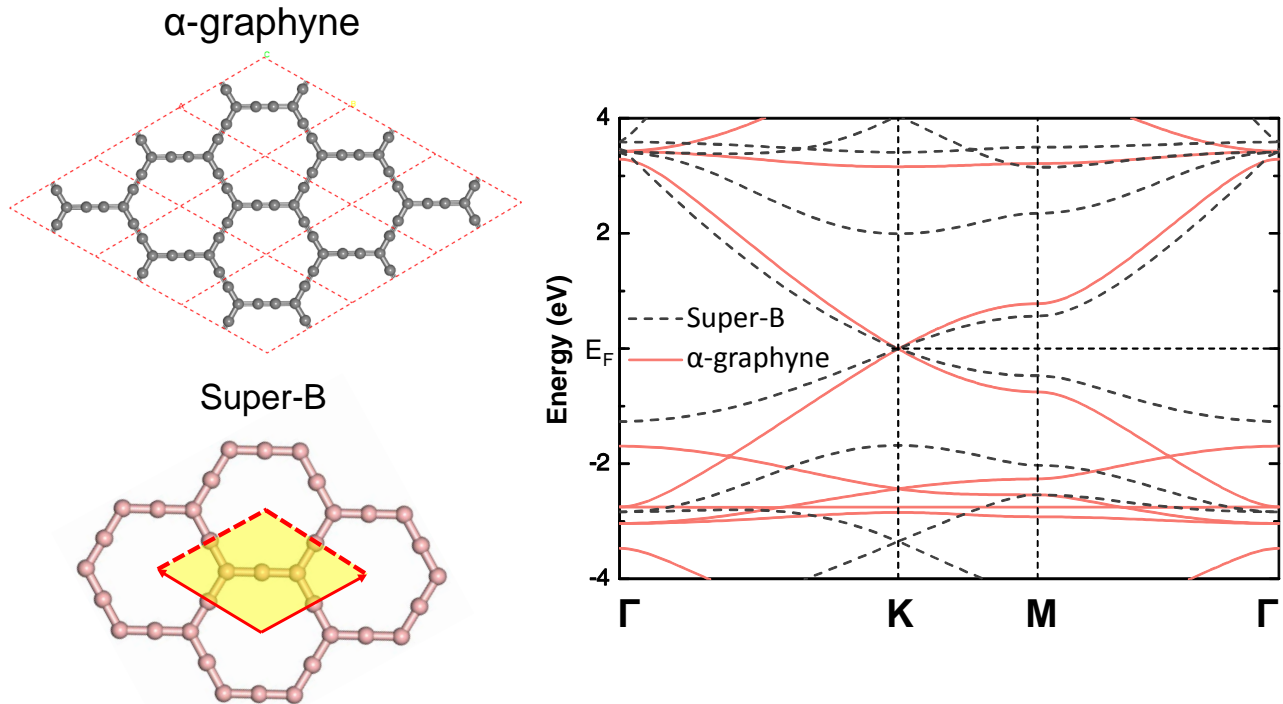


Figure S2: Crystal structure of  $\alpha$ -graphyne and super-B. Electronic band structures of pristine  $\alpha$ -graphyne and super-B under  $-0.2 e/B$  doping. Both are Dirac materials.

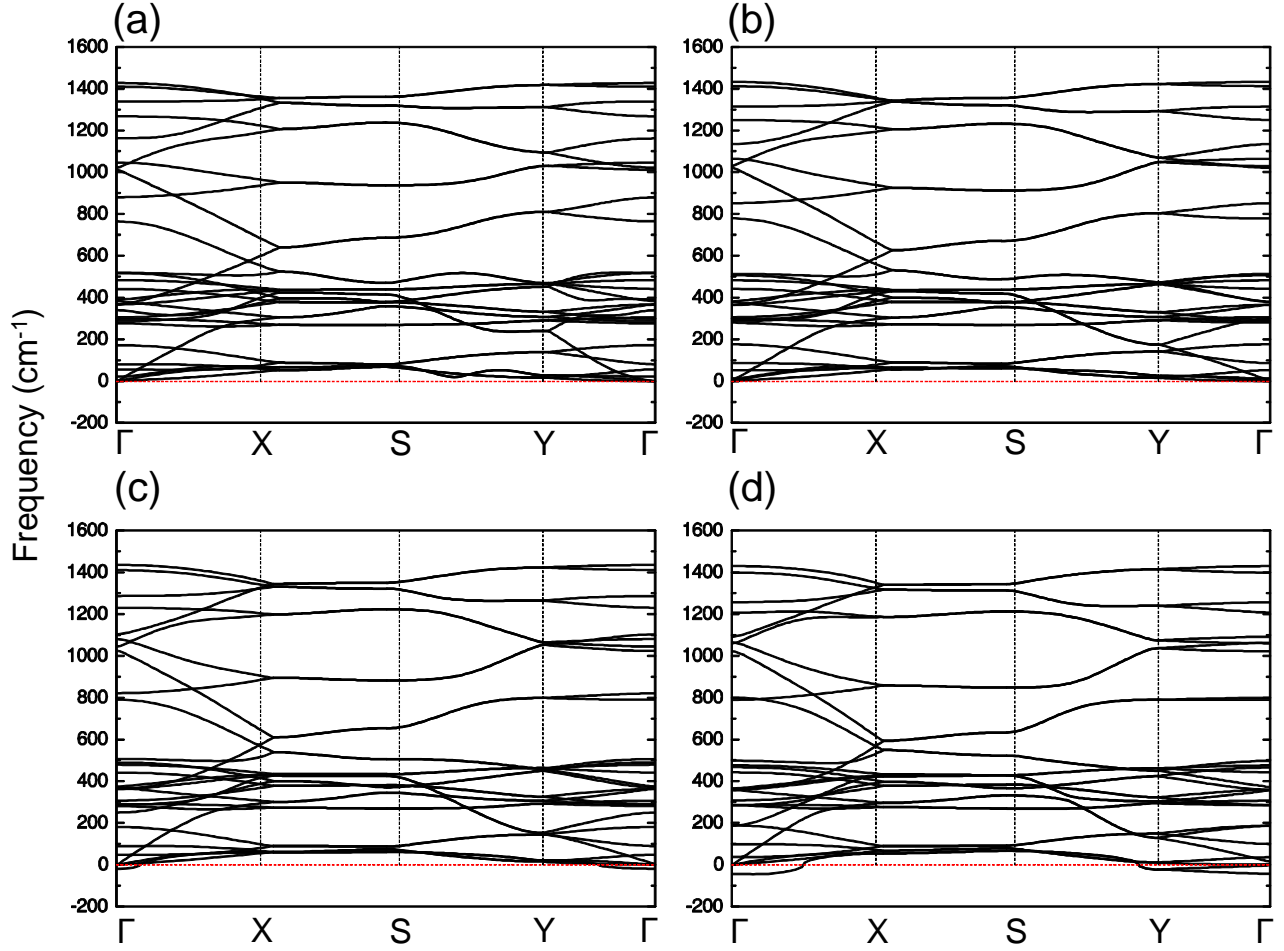


Figure S3: Phonon dispersions of super-B under uniaxial strain of (a)  $\varepsilon=6\%$ , (b)  $\varepsilon=8\%$ , (c)  $\varepsilon=10\%$ , (d)  $\varepsilon=12\%$ .

Table S1: Calculated properties of singled-walled borophene nanotubes (SWBNTs).  $N_{atom}$  is the number of atoms.  $E_g$  is the electronic band gap.  $E_c$  is the cohesive energy and  $D$  is the diameter of SWBNTs.

SWBNTs	$N_{atom}$	$E_g$ (eV)	$E_c$ (eV/atom)	$D$ (Å)
(4,0)	40	0, metal	5.256	7.07
(8,0)	40	0, metal	5.537	13.91
(4,4)	80	0, metal	5.284	11.93
(8,8)	80	0, metal	5.543	23.99

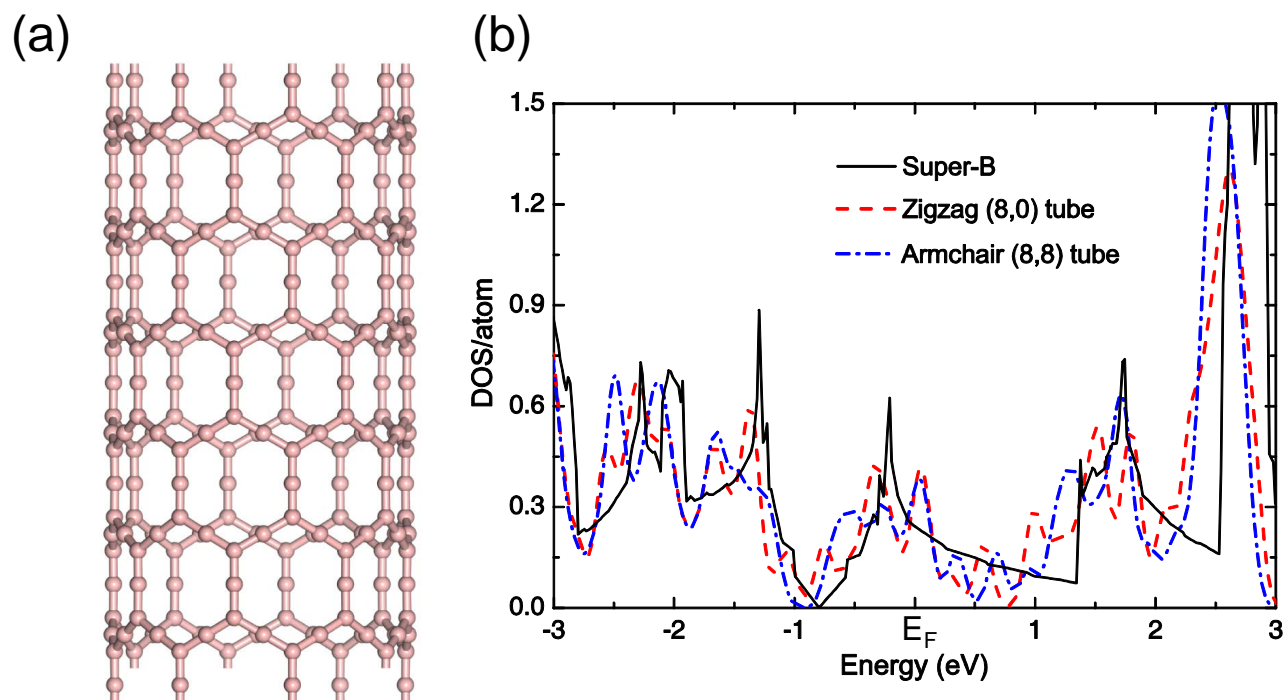


Figure S4: (a) Optimized super-borophene nanotubes of zigzag (8,0) as an example. All single-walled borophene nanotubes (SWBNTs) are cylindrical without any buckling or collapse in our study. (b) Electronic density of states of planar super-borophene, zigzag (8,0) and armchair (8,8) nanotubes, indicating the metallic property of SWBNTs.

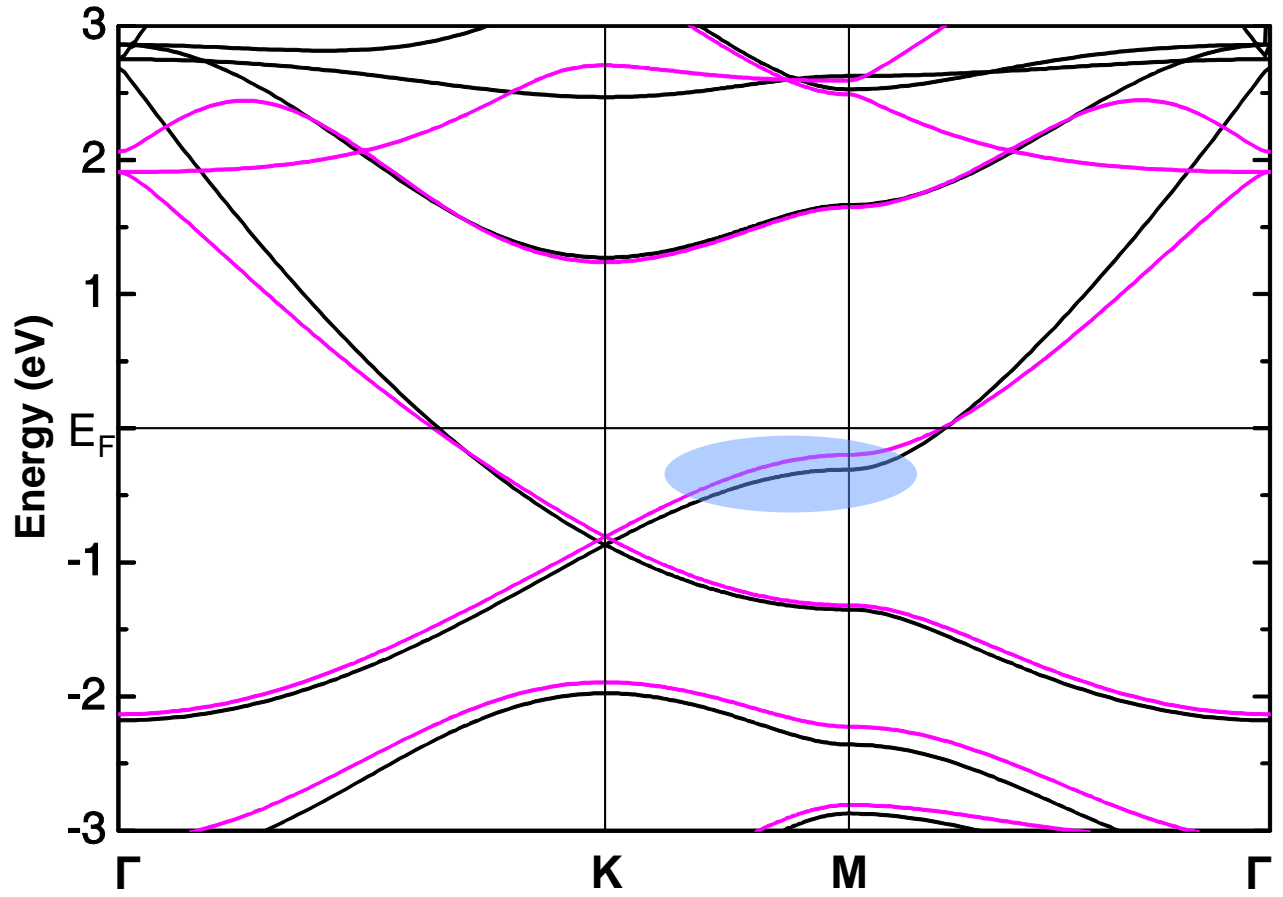


Figure S5: Band structure of the undistorted (black lines) and distorted structures (pink lines) in super-B by the  $O_z$  phonon mode ( $u_B \approx 0.4 \text{ \AA}$ ) in super-B.