



Cite this: *Phys. Chem. Chem. Phys.*, 2020, 22, 16796

# Comparative investigation of the thermal transport properties of Janus SnSSe and SnS<sub>2</sub> monolayers

Gang Liu,<sup>a</sup> Hui Wang,<sup>a</sup> Zhibin Gao<sup>b</sup> and Guo-Ling Li<sup>c</sup>

Recently, Janus two-dimensional (2D) materials as a new member of 2D derivatives have been receiving much attention due to their novel properties. In this work, the lattice thermal conductivity  $\kappa_L$  of the Janus SnSSe monolayer is investigated based on first-principles calculations, while that of the SnS<sub>2</sub> monolayer is studied for comparison. It is found that the  $\kappa_L$  values of SnSSe and SnS<sub>2</sub> are 13.3 and 11.0 W m<sup>-1</sup> K<sup>-1</sup> at room temperature, and acoustic branches dominate their thermal transport. Weaker phonon anharmonicity in SnSSe leads to a slightly higher  $\kappa_L$ , though it has weaker phonon harmonicity. The smaller Grüneisen parameters of TA and LA phonons lower than 1 THz in SnSSe indicate weaker phonon anharmonicity, resulting in a higher  $\kappa_L$ . Finally, the size effect and boundary effect are also investigated, exhibiting that the  $\kappa_L$  can further decrease at the nanoscale. Our work suggests that Janus SnSSe and SnS<sub>2</sub> have a much lower  $\kappa_L$  compared with conventional transition metal dichalcogenides (TMDs) and are potential competitors in the thermoelectric field.

Received 10th April 2020,  
Accepted 23rd June 2020

DOI: 10.1039/d0cp01939a

rs.li/pccp

## Introduction

The successful exfoliation of graphene has opened up new fields in the study of two-dimensional (2D) materials since 2004.<sup>1</sup> Stimulated by graphene, many other 2D materials have been synthesized experimentally or predicted theoretically, such as hexagonal boron nitride,<sup>2</sup> transition metal chalcogenides (TMDs),<sup>3–6</sup> group-V 2D materials,<sup>7–16</sup> and group-VI 2D materials.<sup>17–22</sup> Among these 2D materials, TMDs attract remarkable attention due to their distinctive physical and chemical properties, such as finite direct band gaps, high on/off ratios (as high as 10<sup>3</sup>–10<sup>8</sup>), high carrier mobilities and strong optoelectronic responses, as well as their various potential applications.<sup>5,23–27</sup>

In ancient Roman mythology, Janus was the god of gates, time, duality, and doorways, who is characterized by two faces. Recently, as a new member of 2D derivatives, Janus 2D materials have been receiving much attention, since the Janus monolayer MoSSe is synthesized by well-controlled sulfurization of the MoSe<sub>2</sub> monolayer, in which the top Se layer is substituted by vaporized sulfur.<sup>28,29</sup> Compared to perfect 2D materials, Janus monolayers with a broken reflection symmetry allow

out-of-plane intrinsic electric polarization. Thus, Janus monolayers display many novel properties, such as large Rashba effect, chiral effect, and spatial isolation of charge carriers.<sup>30–35</sup> Furthermore, theoretical investigations show that the thermal transport properties of Janus monolayers are also significantly affected. For instance, the thermal conductivities of MoSSe and PtSSe are suppressed much more compared to those of MoS<sub>2</sub> and PtS<sub>2</sub>.<sup>36,37</sup> The thermoelectric performance is measured by using the figure of merit  $ZT$ , which is expressed as  $ZT = S^2\sigma T / (\kappa_e + \kappa_L)$ . Here,  $S^2\sigma$  means the power factor, while  $\kappa_e$  and  $\kappa_L$  are the electrical and lattice thermal conductivities. For a semiconductor,  $\kappa_e$  is much smaller than  $\kappa_L$ , and it is concluded that low thermal conductivity leads to high thermoelectric efficiency.

In this work, we systemically investigate the thermal transport properties of Janus SnSSe monolayers, which are constructed based on the synthesized 1T structure of SnS<sub>2</sub>/SnSe<sub>2</sub>.<sup>38,39</sup> The thermal transport properties of the SnS<sub>2</sub> monolayer are also studied, to explore the effect of the Janus structure on thermal transport. Based on first-principles calculations, the lattice thermal conductivity  $\kappa_L$  is obtained by solving the linearized phonon transport Boltzmann equation (BTE). We found that they are 13.3 and 11.0 W m<sup>-1</sup> K<sup>-1</sup> at room temperature, while acoustic branches dominate the thermal transport of both the monolayers. Different from other Janus monolayers,<sup>36,37</sup> the two monolayers have  $\kappa_L$  close to each other, showing that the Janus structure does not have a remarkable effect on thermal transport. The harmonic properties, such as phonon spectra, and mechanical properties, Debye temperature, and phonon group velocities, are exhibited.

<sup>a</sup> School of Physics and Engineering, Henan University of Science and Technology, Luoyang 471023, People's Republic of China. E-mail: liugang8105@gmail.com

<sup>b</sup> Department of Physics, National University of Singapore, Singapore 117551, Republic of Singapore. E-mail: zhibin.gao@nus.edu.sg

<sup>c</sup> Chemistry and Chemical Engineering Guangdong Laboratory, Shantou 515063, People's Republic of China

To explore the underlying physical mechanisms of the approximately identical  $\kappa_L$  of the two monolayers, anharmonic properties are also investigated, such as relaxation times, the total phase space for three-phonon processes, and Grüneisen parameters. It is found the smaller Grüneisen parameters of TA and LA phonons with low frequency in SnSSe result in a slightly higher  $\kappa_L$  in SnSSe, though it exhibits weaker harmonic properties. Comprehensively, the weaker anharmonic properties enhance the thermal transport in Janus SnSSe, making its  $\kappa_L$  close to that of SnS<sub>2</sub>. To study the size and the boundary effect, the cumulative and size-dependent  $\kappa_L$  are also exhibited.

## Computational methods

Based on density functional theory (DFT), all the first-principles calculations are performed by using the VASP package.<sup>40–42</sup> Generalized gradient approximations parameterized by Perdew, Burke, and Ernzerhof (PBE) are chosen for exchange–correlation functional.<sup>43</sup> A plane-wave basis set with a kinetic energy cutoff of 500 eV is used. During the structural relaxation, a Monkhorst–Pack<sup>44</sup>  $k$ -mesh of  $15 \times 15 \times 1$  is used to sample the Brillouin zone (BZ), while the energy and the Hellman–Feynman force convergence thresholds are  $10^{-6}$  eV and  $10^{-4}$  eV Å<sup>-1</sup>, respectively. A vacuum space of at least 20 Å is maintained along the  $z$  direction, which is enough to eliminate the interactions between the adjacent layers.

Due to the isotropic in-plane structure of the SnSSe monolayer, the in-plane  $\kappa_L$  is also isotropic and can be calculated as:

$$\kappa_L = \frac{1}{V} \sum_{\lambda} C_{\lambda} v_{\lambda\alpha}^2 \tau_{\lambda\alpha}, \quad (1)$$

where  $V$  is the cell volume and  $\lambda$  is the phonon mode which comprises both the wave vector index  $\mathbf{q}$  and the phonon branch index  $j$ . Furthermore,  $C_{\lambda}$  is the heat capacity in each mode;  $v_{\lambda\alpha}$  is the group velocity of the phonon along the  $\alpha$  direction, with the mode index  $\lambda$ ; and  $\tau_{\lambda\alpha}$  is the relaxation time of the phonon with  $\lambda$  mode along the same direction. Based on eqn (1),  $\kappa_L$  is determined based on both harmonic and anharmonic properties. The harmonic interatomic force constants (IFCs) were

calculated using a  $6 \times 6 \times 1$  supercell and a  $2 \times 2 \times 1$   $k$ -mesh within a finite displacement scheme, as implemented in the open-source software package PHONOPY.<sup>45</sup> Then the phonon dispersion relation can be obtained using the harmonic IFCs. The anharmonic IFCs were calculated using ShengBTE code,<sup>46</sup> considering up to the ninth-nearest neighbor. After careful parameter testing, the converged  $\kappa_L$  was obtained with a  $\mathbf{q}$ -mesh of  $201 \times 201 \times 1$ , and a scale broadening parameter of 0.1 was used for Gaussian smearing. Note that an effective thickness should be defined to calculate the thermal properties for 2D materials. For SnSSe, the thickness of 6.78 Å was considered as the summation of the buckling height  $h$  and the van der Waals radii of the S and Se atoms.<sup>47–49</sup> And for SnS<sub>2</sub> the thickness was 6.55 Å under the same definition.

## Results and discussion

The optimized structure of the Janus SnSSe monolayer is shown in Fig. 1(a), while that of the SnS<sub>2</sub> monolayer is exhibited in Fig. 1(b). It is found that they share a similar structure; nevertheless, in SnSSe the Sn atom layer is sandwiched between the S and Se atom layers, with a broken reflection symmetry along the out-of-plane direction. Thus, its structure belongs to the  $P3m1$  (156) symmetry group, whose symmetry is lower than  $P\bar{3}m1$  (164) for SnS<sub>2</sub>. Note that they belong to the same trigonal crystal system but with different subgroups due to the broken reflection symmetry, which could induce piezoelectric properties in Janus materials, such as SnSSe. The lattice constant  $a$  and the buckling height  $h$  are 3.78 and 3.08 Å for SnSSe, while the corresponding values are 3.70 and 2.96 Å for SnS<sub>2</sub>. These results are in good agreement with those in previous researches.<sup>50,51</sup> In general, a larger lattice constant implies weaker interatomic bonding in SnSSe.

Usually, we can estimate  $\kappa_L$  based on the Slack model:<sup>52</sup>

$$\kappa_L \sim \frac{a^4 \rho \omega_D^3}{\gamma^2 T}, \quad (2)$$

where  $a^3$ ,  $\rho$ ,  $\omega_D$  and  $T$  are the average volume occupied by one atom of the crystal, the density, the Debye frequency, and the

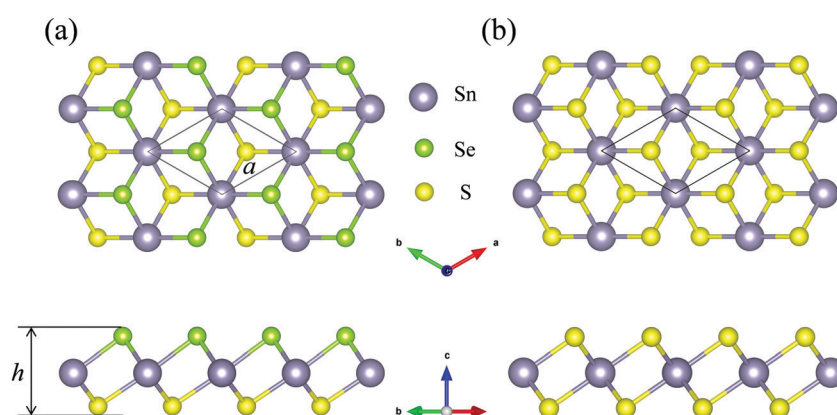


Fig. 1 (a) Structure of the Janus SnSSe monolayer and (b) the structure of the SnS<sub>2</sub> monolayer. Both top and side views are exhibited. The primitive cells are marked in solid lines.

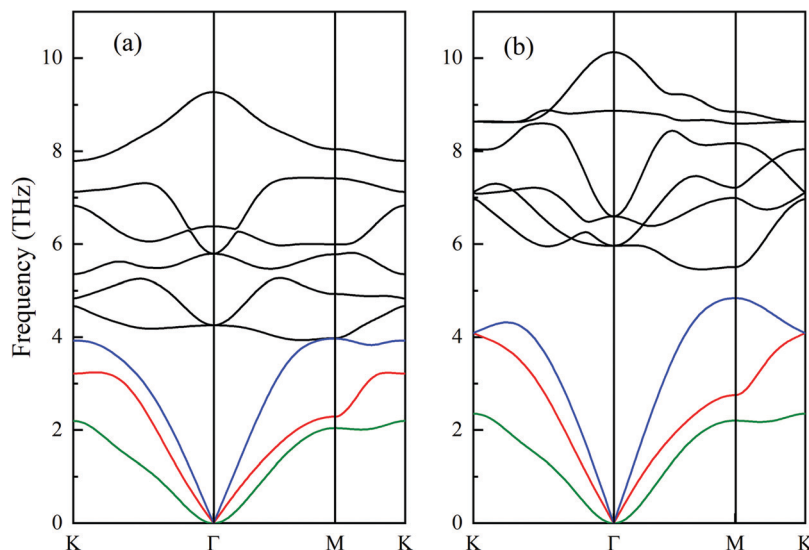


Fig. 2 Phonon dispersions for SnSSe (a) and SnS<sub>2</sub> (b) monolayers. Three acoustic phonon branches, which correspond to an out-of-plane (ZA) mode, an in-plane transverse (TA) mode, and an in-plane longitudinal (LA) mode, are marked in green, red and blue colors.

absolute temperature. The Grüneisen parameter  $\gamma$  is expressed as  $\gamma = -\frac{d \ln \omega}{d \ln V}$ , exhibiting phonon anharmonicity. This indicates that both stronger harmonicity and weaker anharmonicity lead to a higher  $\kappa_L$ . The phonon dispersions for the monolayers SnSSe and SnS<sub>2</sub> are displayed in Fig. 2, which show the phonon harmonicity of the materials. There is no imaginary frequency indicating the dynamic stability of the two structures. For both the monolayers, there are 9 branches as each primitive cell possesses 3 atoms. On the whole, the phonon dispersions are very similar to each other. However, the phonon frequencies for each branch are lower in SnSSe, resulting from the heavier average atomic mass  $M$ , as listed in Table 1. In general, the average phonon frequency is inversely proportional to the average atomic mass, the same as the maximum vibrational frequencies. Furthermore, there is no phonon gap in Janus SnSSe, whereas it appears in the phonon dispersion of SnS<sub>2</sub>. It should be noted that the phonon gap generally can suppress phonon scattering, and hence enhance thermal transport.<sup>53</sup>

The 2D elastic constants and Young's moduli are calculated, as shown in Table 1. It should be noted that the calculated elastic constants satisfy the Born criteria of mechanical stability.<sup>54</sup> The 2D Young's modulus  $E$  is calculated based on elastic constants with the following expression:  $E = (C_{11}^2 - C_{12}^2)/C_{11}$ .<sup>55</sup> It is found that the 2D elastic constants and Young's moduli for SnSSe are slightly smaller than those for SnS<sub>2</sub>, due to the larger lattice constant and weaker interatomic bonding in SnSSe. Their  $E$

are close to those of  $\alpha$ -selenene and  $\beta$ -arsenene,<sup>56</sup> but smaller than those of blue phosphorene, the MoS<sub>2</sub> monolayer, and graphene.<sup>56–58</sup> Furthermore, our results are in good agreement with those in previous work.<sup>50</sup>

The group velocity is denoted as  $\vec{v} = d\omega/d\vec{q}$ , while the Debye temperature  $\theta_D$  is denoted as  $\theta_D = \hbar\omega_D/k_B$ , where  $\omega_D$  can be considered as the maximum acoustic phonon frequency.<sup>21,48,59</sup> The group velocities of the acoustic phonons around the  $\Gamma$  point and Debye temperature  $\theta_D$  for SnSSe and SnS<sub>2</sub> are also listed in Table 1. The phonon group velocities of TA and LA modes for SnSSe are smaller than that for SnS<sub>2</sub>, whereas the phonon group velocity of ZA phonons is larger in SnSSe.  $\theta_D$  is smaller in SnSSe than in SnS<sub>2</sub>, to the benefit of lower  $\kappa_L$  in SnSSe based on eqn (2).

The intrinsic  $\kappa_L$  of the monolayers SnSSe and SnS<sub>2</sub> are calculated by ShengBTE with an iterative scheme,<sup>46</sup> as displayed in Fig. 3. The  $\kappa_L$  of the monolayer SnSSe is higher than that of SnS<sub>2</sub> in the whole temperature range. For instance, the values are 13.3 and 11.0 W m<sup>-1</sup> K<sup>-1</sup> at 300 K, which are close to each other. The intrinsic  $\kappa_L$  for both the monolayers show an inverse dependence on temperature  $T$ , implying the dominant Umklapp process of phonon–phonon scattering in the thermal transport. It is found that the  $\kappa_L$  of the monolayer SnS<sub>2</sub> is slightly lower than the in-plane  $\kappa_L$  of 12.1 W m<sup>-1</sup> K<sup>-1</sup> for bulk SnS<sub>2</sub>,<sup>60</sup> which does not follow the unique trend of 2D SnS<sub>2</sub> that  $\kappa_L$  decreases with decreasing thickness.<sup>61</sup> The reason for a slightly higher  $\kappa_L$  of the SnSSe monolayer which has lower harmonic properties than SnS<sub>2</sub> will be discussed later. The values are much smaller than that of MoS<sub>2</sub> with 131 W m<sup>-1</sup> K<sup>-1</sup>,<sup>62</sup> implying potential competitors in the thermoelectric field. For instance, previous work shows an excellent power factor of about 65  $\mu$ W cm<sup>-1</sup> K<sup>-2</sup> with a doping level of 0.0248 at 700 K in the SnSSe monolayer.<sup>50</sup> Considering that the lattice thermal conductivity is 5.0 W m<sup>-1</sup> K<sup>-1</sup> at the same temperature, SnSSe possesses a high  $ZT$  of about 0.9.

Table 1 2D elastic constants and Young's moduli (in N m<sup>-1</sup>), Debye temperature (in K), average atomic mass  $M$  (in amu), and group velocities of the three acoustic phonons (in km s<sup>-1</sup>) around the  $\Gamma$  point

	$C_{11}$	$C_{12}$	$C_{66}$	$E$	$v_{ZA}$	$v_{TA}$	$v_{LA}$	$M$	$\theta_D$
SnSSe	63.8	15.9	23.9	59.8	0.263	2.521	3.992	76.6	190
SnS <sub>2</sub>	69.7	17.0	26.3	65.6	0.139	3.052	4.788	60.9	233

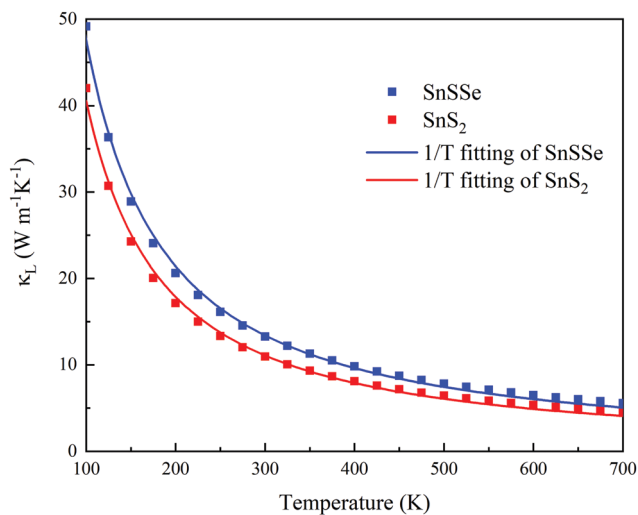


Fig. 3 Temperature-dependent  $\kappa_L$  of the monolayers SnSSe and SnS<sub>2</sub>. 1/T fittings are shown in solid lines.

Furthermore, we also use thermal sheet conductance (“2D thermal conductivity”) with the unit  $\text{W K}^{-1}$  as it is more meaningful and physical for 2D materials.<sup>63,64</sup> Then we obtain values of 8.99 and 7.17  $\text{nW K}^{-1}$  for the SnSSe and SnS<sub>2</sub> monolayers at 300 K, respectively. For comparison, it was reported that the thermal sheet conductances are 57.04, 34.25, and 28.44  $\text{nW K}^{-1}$  for the MoS<sub>2</sub>, MoSSe, and MoSe<sub>2</sub> monolayers,

respectively.<sup>36</sup> It can be seen that Janus SnSSe possesses much lower thermal sheet conductance than Janus MoSSe.

It is found that the acoustic phonons contribute most to the total  $\kappa_L$ . For SnSSe, we found that ZA, TA and LA modes contribute 27.1%, 35.7% and 35.3% to the total  $\kappa_L$  at room temperature, while all the optical branches contribute 1.9% only. For SnS<sub>2</sub>, the normalized contributions of ZA, TA, and LA modes are 33.5%, 30.7%, and 31.3%, respectively, while the one of all the optical modes is 4.5%. It is found that the contribution of ZA mode is lower in SnSSe than in SnS<sub>2</sub>. Note that the contribution of the ZA mode is much lower than that in graphene (about 75%), and it is believed that the domination comes from the unique symmetry of flat graphene along its *c*-axis.<sup>65,66</sup> There is a symmetry selection rule in flat graphene that only an even number of ZA modes can be involved in scattering processes. This rule originates from the reflection symmetry about the *c*-axis in the structure. The thermal resistance originates from the anharmonic phonon scattering. Due to the selection rule, the ZA mode contributes mainly to the total thermal conductivity in graphene. However, the lattice does not have a reflection symmetry along the *c*-axis in Janus SnSSe and SnS<sub>2</sub>. As a result, the selection rule is broken and the contribution of the ZA mode in the thermal transport of the two materials is much lower than that in graphene.

To further understand the underlying physical mechanisms of  $\kappa_L$  in these two monolayers, we investigate the phonon group velocity and the relaxation time, as shown in Fig. 4. On the

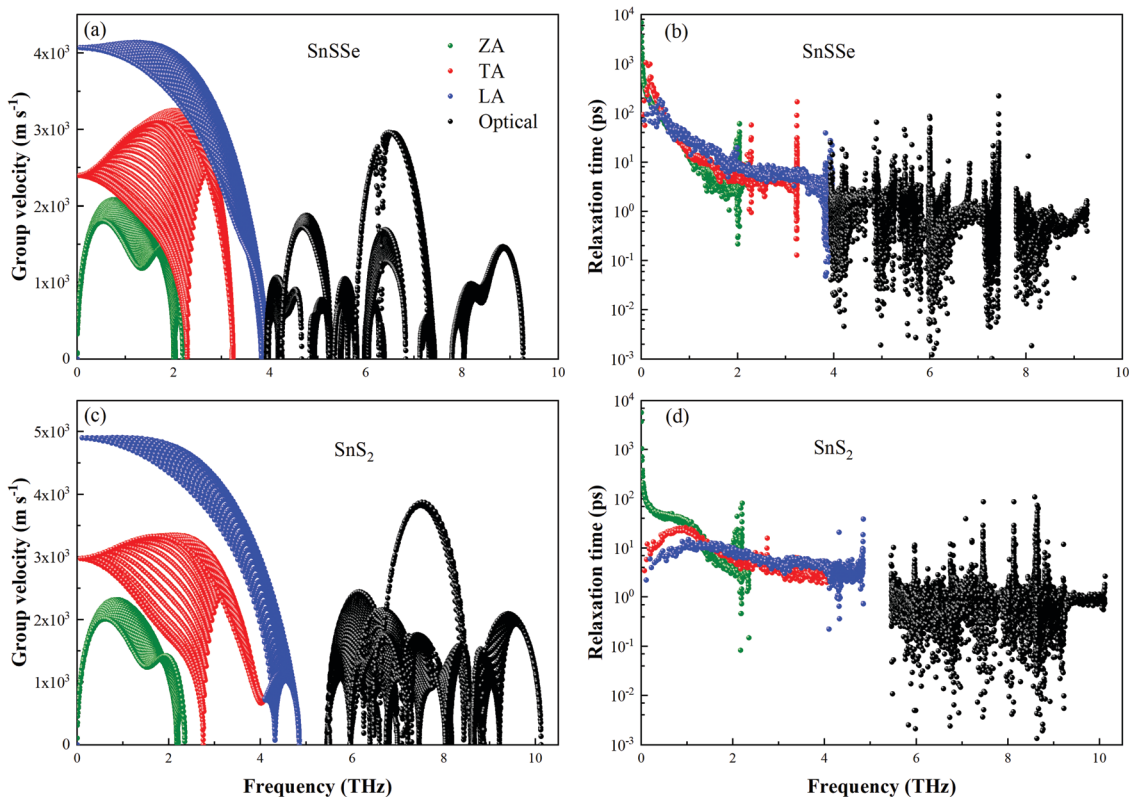


Fig. 4 Phonon group velocities and relaxation times of the two monolayers at room temperature; (a) and (b) display the group velocity and relaxation time of SnSSe, while (c) and (d) show the group velocity and relaxation time of SnS<sub>2</sub>.

whole, the phonon group velocities of the two monolayers are similar, whereas those of SnSSe are lower. The range of group velocity is from 0 to 4000 m s<sup>-1</sup> for SnSSe, while it is from 0 to 5000 m s<sup>-1</sup> for SnS<sub>2</sub>. Furthermore, compared to Janus SnSSe, the phonon group velocity of phonons with a low frequency is as high as 5500 m s<sup>-1</sup> in the MoSSe monolayer, leading to a higher thermal conductivity in MoSSe.<sup>36</sup> This also confirms that heavier *M* leads to weaker phonon harmonicity in SnSSe, as mentioned previously. The phonon group velocities of acoustic modes are higher than those of optical modes because of the relative flatness of optical modes.

The relaxation time is inversely related to the strength of anharmonic interaction, which is in the range of 10<sup>-3</sup> to 10<sup>4</sup> ps for both the monolayers as displayed in Fig. 4(b) and (d). However, there are remarkable differences between TA and LA phonons with a low frequency between the two monolayers. The relaxation times of TA and LA phonons below 1 THz for SnSSe are one order higher than those for SnS<sub>2</sub>. Based on eqn (1), the κ<sub>L</sub> is mainly determined based on the group velocity and the relaxation time. It is mentioned above that TA and LA modes contribute more than 60% to the κ<sub>L</sub> in both the monolayers. Therefore, the much smaller relaxation time of TA and LA phonons below 1 THz determines the smaller κ<sub>L</sub> in SnS<sub>2</sub>, though SnS<sub>2</sub> possesses stronger phonon harmonic properties. Furthermore, the relaxation times of many phonons show a large decrease near 4 THz in SnSSe, which is the cross-region of

acoustic and optical branches. However, there is no such situation near the acoustic-optical gap (5 THz) in SnS<sub>2</sub>, confirming the effect of enhancing the thermal transport for the acoustic-optical gap.<sup>53</sup>

The intrinsic phonon scattering rate 1/τ<sub>λ</sub><sup>0</sup> (inversion of the relaxation time) determined by three-phonon transition probabilities can be expressed in the following equations:

$$\frac{1}{\tau_{\lambda}^0} = \frac{1}{N} \left( \sum_{\lambda'\lambda''} \Gamma_{\lambda\lambda'\lambda''}^+ + \sum_{\lambda'\lambda''} \frac{1}{2} \Gamma_{\lambda\lambda'\lambda''}^- \right), \quad (3)$$

$$\Gamma_{\lambda\lambda'\lambda''}^+ = \frac{\hbar\pi (f_0' - f_0'')}{4 \omega_{\lambda}\omega_{\lambda'}\omega_{\lambda''}} |V_{\lambda\lambda'\lambda''}^+|^2 \delta(\omega_{\lambda} + \omega_{\lambda'} - \omega_{\lambda''}), \quad (4)$$

$$\Gamma_{\lambda\lambda'\lambda''}^- = \frac{\hbar\pi (f_0' + f_0'' + 1)}{4 \omega_{\lambda}\omega_{\lambda'}\omega_{\lambda''}} |V_{\lambda\lambda'\lambda''}^-|^2 \delta(\omega_{\lambda} - \omega_{\lambda'} - \omega_{\lambda''}), \quad (5)$$

where *f*<sub>0</sub> means Bose–Einstein statistics of the phonon mode λ, Γ<sub>λλ'λ''</sub><sup>+</sup> and Γ<sub>λλ'λ''</sub><sup>-</sup> stand for the absorption and emission processes, and *N* is the number of *q* points in BZ.<sup>46</sup> Furthermore, *V*<sub>λλ'λ''</sub><sup>±</sup> means the scattering matrix elements, which are proportional to anharmonic IFCs.<sup>46,48</sup> As mentioned previously, the Grüneisen parameter γ indicates the anharmonicity of the materials, thus γ is proportional to *V*<sub>λλ'λ''</sub><sup>±</sup> and the scattering rate. It is also in agreement with the Slack model in eqn (2), which implies that κ<sub>L</sub> is inversely proportional to γ. Based on

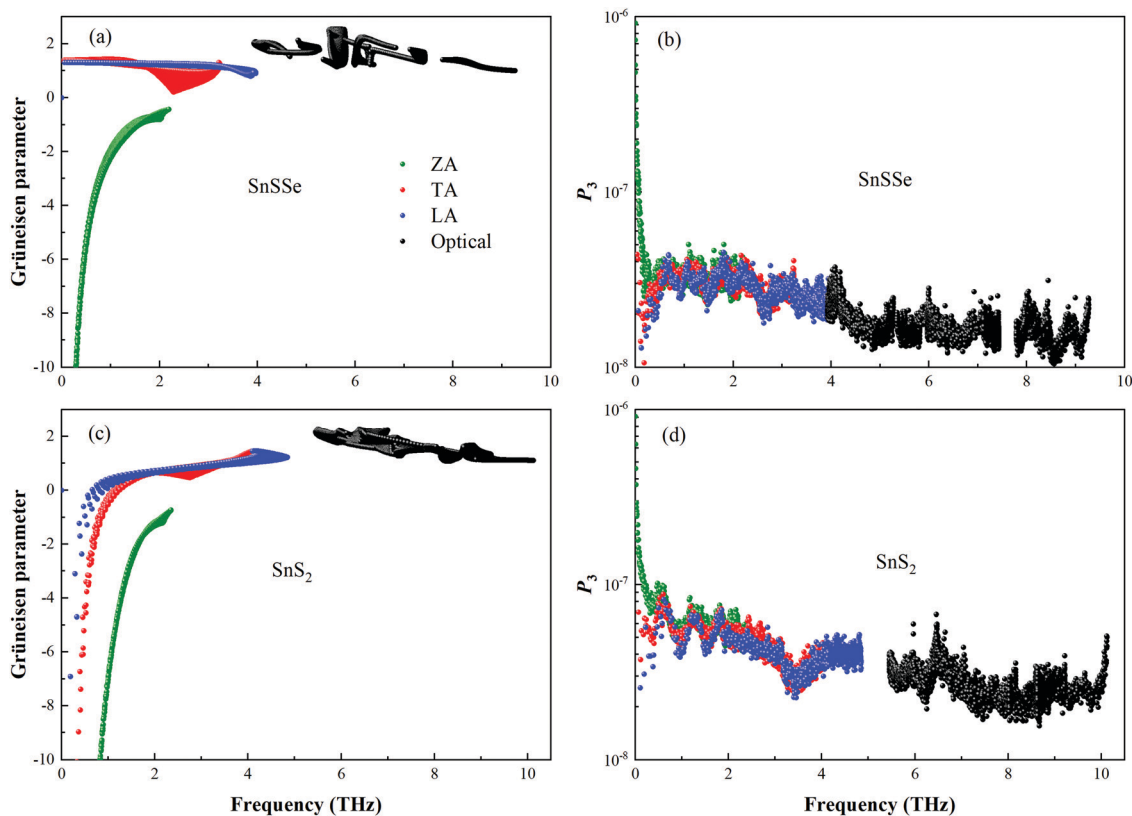


Fig. 5 Grüneisen parameter γ and *P*<sub>3</sub> for the monolayers SnSSe and SnS<sub>2</sub>; (a) and (b) show γ and *P*<sub>3</sub> of SnSSe, while (c) and (d) display those quantities of SnS<sub>2</sub>.

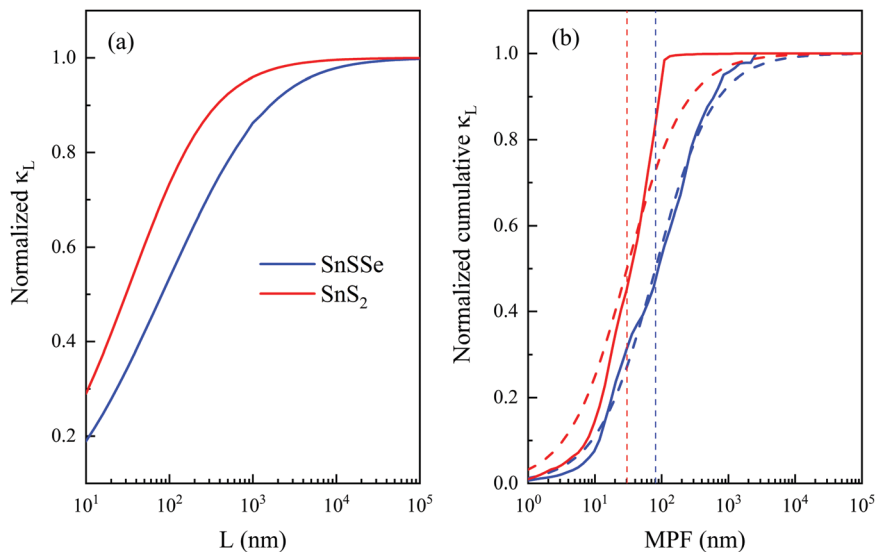


Fig. 6 (a) Normalized  $\kappa_L$  as a function of the sample size  $L$  at 300 K. (b) Normalized cumulative  $\kappa_L$  as a function of the phonon MPF of the monolayers SnSSe and SnS<sub>2</sub> at 300 K. The dashed lines in (b) indicate the fitting data. The vertical lines indicate the position of  $l_0$  for the two monolayers.

eqn (3)–(5), it is also found that the scattering rate is proportional to the number of Dirac delta distributions, which can be denoted by the volume of the scattering phase space  $P_3$  for three-phonon processes.<sup>46</sup> We have calculated  $\gamma$  and  $P_3$ , as exhibited in Fig. 5. For  $P_3$ , a significant increase near 4 THz in SnSSe can be seen, while there is a decrease near 5 THz in SnS<sub>2</sub>. This indicates the suppression effect on scattering for the acoustic-optical gap, thus the acoustic-optical gap can enhance the relaxation time as displayed in Fig. 4. However, it cannot lead to lower  $\kappa_L$  in Janus SnSSe, as most of the contributions to  $\kappa_L$  come from phonons with a low frequency. We found that there are obvious distinctions for  $\gamma$  of TA and LA phonons with low frequency. Specifically,  $\gamma$  is around 1.6 for TA and LA phonons with a frequency lower than 1 THz in SnSSe, while it shows negative values with a very large absolute value in SnS<sub>2</sub>. Therefore,  $\gamma$  leads to a discrepancy of the relaxation time of these low-frequency phonons in two monolayers, and finally suppresses the  $\kappa_L$  of SnS<sub>2</sub>, though it possesses higher phonon harmonicity than SnSSe, such as group velocity, Young's modulus, and Debye temperature. In conclusion, the much weaker phonon anharmonicity in SnSSe compensates the weaker harmonicity, and even leads to a slightly higher  $\kappa_L$ .

In practical applications, all materials have a finite size which can suppress  $\kappa_L$  significantly through boundary scattering of different sample sizes, especially at the nanoscale. Here, an empirical formula is used to describe the boundary scattering, expressed as:  $\frac{1}{\tau_\lambda^b} = \frac{v_\lambda}{L}$ , where  $L$  means the size of the material.<sup>67,68</sup> The calculated results are shown in Fig. 6(a). The  $\kappa_L$  of the two monolayers reduces following an exponential function of increasing  $L$  due to the strong boundary effect, which has been experimentally verified in suspended graphene.<sup>69</sup> It is found that the  $\kappa_L$  of the Janus SnSSe monolayer decreases more quickly than that of the SnS<sub>2</sub> monolayer with diminishing size. For instance, the normalized  $\kappa_L$  of the SnSSe monolayer is 0.53 at

a size of 100 nm, while that of the SnS<sub>2</sub> monolayer is 0.73. When the  $L$  is 1000 nm, the data are 0.86 and 0.96, respectively.

To estimate the size effect, we also evaluate the normalized cumulative  $\kappa_L$  with respect to the phonon mean free paths (MFPs) for both the monolayers, as shown in Fig. 6(b). The phonon MFPs which contribute mainly to  $\kappa_L$  span from 1 to 1000 nm for SnSSe, whereas the range is from 1 to 100 nm for SnS<sub>2</sub>, much narrower than the former. This indicates that phonons with a low frequency contribute more to  $\kappa_L$  in SnS<sub>2</sub> than in SnSSe. In order to obtain the characteristic length, we introduce a single parametric function:<sup>46</sup>

$$\kappa_L(l \leq l_{\max}) = \frac{\kappa_{\max}}{1 + l_0/l_{\max}}, \quad (6)$$

where  $l_{\max}$  and  $\kappa_{\max}$  are the maximum MFP and the ultimate cumulative lattice thermal conductivity.  $l_0$  is the only parameter to be determined, and can be regarded as the representative MFP. It is found that  $l_0$  values are 80.9 and 30.2 nm for the SnSSe and SnS<sub>2</sub> monolayers, respectively, corresponding to the positions of 50% of the total  $\kappa_L$ . This is in good agreement with the curves shown in Fig. 6(a), indicating a much weaker size effect in the phonon transport of the nanoscale SnSSe than SnS<sub>2</sub>. It can be expected that the  $\kappa_L$  will significantly decrease when the size is of the order of 100 nm. This information is very useful for the thermal management design of micro-/nano-electronic devices based on these monolayers.

## Conclusion

In summary, the lattice thermal conductivities  $\kappa_L$  of Janus SnSSe and SnS<sub>2</sub> monolayers are investigated based on first-principles calculations. The  $\kappa_L$  values of SnSSe and SnS<sub>2</sub> are 13.3 and 11.0 W m<sup>-1</sup> K<sup>-1</sup> at room temperature, which are close to each other. Acoustic branches dominate the thermal transport of the two monolayers. The harmonic and anharmonic

phonon properties together determine the  $\kappa_L$  of the materials, thus they are further investigated. It is found that the SnS<sub>2</sub> monolayer possesses stronger harmonic properties than the Janus SnSSe monolayer, such as higher elastic constants, Young's modulus, phonon group velocity and  $\theta_D$ . However, the SnSSe monolayer has a slightly higher  $\kappa_L$  than SnS<sub>2</sub> due to the weaker anharmonic scattering than the former. Smaller Grüneisen parameters of LA and TA phonons within 1 THz are found in SnSSe, exhibiting lower anharmonicity of these phonons. And this finally leads to higher relaxation times and  $\kappa_L$  in the Janus SnSSe monolayer. At last, the size and boundary effects are studied by cumulative  $\kappa_L$  and size-dependent  $\kappa_L$ , respectively. This provides important information for the future design of micro-/nano-devices. It can be expected that our work may contribute to the understanding of the thermal transport of 2D materials, as well as the practical applications of SnSSe and SnS<sub>2</sub> monolayers.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

This work was supported by the National Natural Science Foundation of China (No. 11974100). Z. Gao acknowledges financial support from MOE Tier 1 funding of Singapore (Grant No. R-144-000-402-114).

## References

- 1 K. S. Novoselov, A. K. Geim, S. V. Morozov, D. Jiang, Y. Zhang, S. V. Dubonos, I. V. Grigorieva and A. A. Firsov, *Science*, 2004, **306**, 666.
- 2 S. Hu, M. Lozada-Hidalgo, F. C. Wang, A. Mishchenko, F. Schedin, R. R. Nair, E. W. Hill, D. W. Boukhvalov, M. I. Katsnelson and R. A. Dryfe, *et al.*, *Nature*, 2014, **516**, 227.
- 3 C. Ataca, H. Şahin and S. Ciraci, *J. Phys. Chem. C*, 2012, **116**, 8983.
- 4 J. N. Coleman, M. Lotya, A. O'Neill, S. D. Bergin, P. J. King, U. Khan, K. Young, A. Gaucher, S. De and R. J. Smith, *et al.*, *Science*, 2011, **331**, 568.
- 5 K. F. Mak, C. Lee, J. Hone, J. Shan and T. F. Heinz, *Phys. Rev. Lett.*, 2010, **105**, 136805.
- 6 Y. Zhan, Z. Liu, S. Najmaei, P. M. Ajayan and J. J. S. Lou, *Small*, 2012, **8**, 966.
- 7 Z. Zhu and D. Tomanek, *Phys. Rev. Lett.*, 2014, **112**, 176802.
- 8 S. Zhang, Z. Yan, Y. Li, Z. Chen and H. Zeng, *Angew. Chem., Int. Ed.*, 2015, **54**, 3112.
- 9 G. Wang, R. Pandey and S. P. Karna, *ACS Appl. Mater. Interfaces*, 2015, **7**, 11490.
- 10 Z. Zhu, J. Guan and D. Tománek, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2015, **91**, 161404.
- 11 C. Kamal and M. Ezawa, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2015, **91**, 085423.
- 12 O. Ü. Aktürk, V. O. Özçelik and S. Ciraci, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2015, **91**, 235446.
- 13 S. Zhang, M. Xie, F. Li, Z. Yan, Y. Li, E. Kan, W. Liu, Z. Chen and H. Zeng, *Angew. Chem., Int. Ed.*, 2016, **55**, 1666.
- 14 H. Liu, A. T. Neal, Z. Zhu, Z. Luo, X. Xu, D. Tomanek and P. D. Ye, *ACS Nano*, 2014, **8**, 4033.
- 15 V. Tran, R. Soklaski, Y. Liang and L. Yang, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2014, **89**, 235319.
- 16 L. Li, Y. Yu, G. J. Ye, Q. Ge, X. Ou, H. Wu, D. Feng, X. H. Chen and Y. Zhang, *Nat. Nanotechnol.*, 2014, **9**, 372.
- 17 Z. Zhu, X. Cai, S. Yi, J. Chen, Y. Dai, C. Niu, Z. Guo, M. Xie, F. Liu and J. H. Cho, *et al.*, *Phys. Rev. Lett.*, 2017, **119**, 106101.
- 18 J. Chen, Y. Dai, Y. Ma, X. Dai, W. Ho and M. Xie, *Nanoscale*, 2017, **9**, 15945.
- 19 J. Qin, G. Qiu, J. Jian, H. Zhou, L. Yang, A. Charnas, D. Y. Zemlyanov, C. Y. Xu, X. Xu and W. Wu, *et al.*, *ACS Nano*, 2017, **11**, 10222.
- 20 G. Liu, Z. Gao and J. Ren, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2019, **99**, 195436.
- 21 Z. Gao, G. Liu and J. Ren, *ACS Appl. Mater. Interfaces*, 2018, **10**, 40702.
- 22 S. Sharma, N. Singh and U. Schwingenschlögl, *ACS Appl. Mater. Interfaces*, 2018, **1**, 1950.
- 23 B. Radisavljevic, A. Radenovic, J. Brivio, V. Giacometti and A. Kis, *Nat. Nanotechnol.*, 2011, **6**, 147.
- 24 S.-W. Min, H. S. Lee, H. J. Choi, M. K. Park, T. Nam, H. Kim, S. Ryu and S. Im, *Nanoscale*, 2013, **5**, 548.
- 25 M. Bernardi, M. Palummo and J. C. Grossman, *Nano Lett.*, 2013, **13**, 3664.
- 26 W. Zhang, Z. Huang, W. Zhang and Y. J. N. R. Li, *Nano Res.*, 2014, **7**, 1731.
- 27 Z. Hui, W. Xu, X. Li, P. Guo, Y. Zhang and J. Liu, *Nanoscale*, 2019, **11**, 6045.
- 28 A.-Y. Lu, H. Zhu, J. Xiao, C.-P. Chuu, Y. Han, M.-H. Chiu, C.-C. Cheng, C.-W. Yang, K.-H. Wei and Y. Yang, *et al.*, *Nat. Nanotechnol.*, 2017, **12**, 744.
- 29 J. Zhang, S. Jia, I. Kholmanov, L. Dong, D. Er, W. Chen, H. Guo, Z. Jin, V. B. Shenoy and L. Shi, *et al.*, *ACS Nano*, 2017, **11**, 8192.
- 30 Q.-F. Yao, J. Cai, W.-Y. Tong, S.-J. Gong, J.-Q. Wang, X. Wan, C.-G. Duan and J. H. Chu, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2017, **95**, 165401.
- 31 F. Li, W. Wei, P. Zhao, B. Huang and Y. Dai, *J. Phys. Chem. Lett.*, 2017, **8**, 5959.
- 32 W.-J. Yin, B. Wen, G.-Z. Nie, X.-L. Wei and L.-M. Liu, *J. Mater. Chem. C*, 2018, **6**, 1693.
- 33 T. Hu, F. Jia, G. Zhao, J. Wu, A. Stroppa and W. Ren, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2018, **97**, 235404.
- 34 J. Liang, W. Wang, H. Du, A. Hallal, K. Garcia, M. Chshiev, A. Fert and H. Yang, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2020, **101**, 184401.
- 35 G. Radvosky, R. Popovitz-Biro and R. Tenne, *Chem. Mater.*, 2012, **24**, 3004.
- 36 S. D. Guo, *Phys. Chem. Chem. Phys.*, 2018, **20**, 7236.
- 37 W.-L. Tao, Y. Mu, C.-E. Hu, Y. Cheng and G.-F. Ji, *Philos. Mag.*, 2019, **99**, 1025.

- 38 X. Zhou, Q. Zhang, L. Gan, H. Li and T. Zhai, *Adv. Funct. Mater.*, 2016, **26**, 4405.
- 39 X. Zhou, L. Gan, W. Tian, Q. Zhang, S. Jin, H. Li, Y. Bando, D. Golberg and T. Zhai, *Adv. Mater.*, 2015, **27**, 8035.
- 40 G. Kresse and J. Hafner, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1993, **47**, 558.
- 41 G. Kresse and J. Furthmüller, *Comput. Mater. Sci.*, 1996, **6**, 15.
- 42 G. Kresse and J. Furthmüller, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1996, **54**, 11169.
- 43 J. P. Perdew, K. Burke and M. Ernzerhof, *Phys. Rev. Lett.*, 1996, **77**, 3865.
- 44 H. J. Monkhorst and J. D. Pack, *Phys. Rev. B: Solid State*, 1976, **13**, 5188.
- 45 A. Togo, F. Oba and I. Tanaka, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2008, **78**, 134106.
- 46 W. Li, J. Carrete, N. A. Katcho and N. Mingo, *Comput. Phys. Commun.*, 2014, **185**, 1747.
- 47 M. Hu, X. Zhang and D. Poulidakos, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2013, **87**, 195417.
- 48 Z. Gao, Z. Zhang, G. Liu and J. S. Wang, *Phys. Chem. Chem. Phys.*, 2019, **21**, 26033.
- 49 G. Liu, H. Wang, Y. Gao, J. Zhou and H. Wang, *Phys. Chem. Chem. Phys.*, 2017, **19**, 2843.
- 50 S. D. Guo, X. S. Guo, R. Y. Han and Y. Deng, *Phys. Chem. Chem. Phys.*, 2019, **21**, 24620.
- 51 A. Shafique, A. Samad and Y. H. Shin, *Phys. Chem. Chem. Phys.*, 2017, **19**, 20677.
- 52 G. A. Slack, *J. Phys. Chem. Solids*, 1973, **34**, 321.
- 53 L. Lindsay, D. A. Broido and T. L. Reinecke, *Phys. Rev. Lett.*, 2013, **111**, 025901.
- 54 R. C. Andrew, R. E. Mapasha, A. M. Ukpong and N. Chetty, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2012, **85**, 125428.
- 55 Q. Wei and X. Peng, *Appl. Phys. Lett.*, 2014, **104**, 251915.
- 56 G. Liu, Z. Gao and J. Zhou, *Phys. E*, 2019, **112**, 59.
- 57 F. Liu, P. Ming and J. Li, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2007, **76**, 064120.
- 58 T. Li, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2012, **85**, 235407.
- 59 L.-D. Zhao, S.-H. Lo, Y. Zhang, H. Sun, G. Tan, C. Uher, C. Wolverton, V. P. Dravid and M. G. Kanatzidis, *Nature*, 2014, **508**, 373.
- 60 H. Wang, Y. Gao and G. Liu, *RSC Adv.*, 2017, **7**, 8098.
- 61 M. J. Lee, J. H. Ahn, J. H. Sung, H. Heo, S. G. Jeon, W. Lee, J. Y. Song, K. H. Hong, B. Choi and S. H. Lee, *et al.*, *Nat. Commun.*, 2016, **7**, 12011.
- 62 A. N. Gandi and U. Schwingenschlögl, *EPL*, 2016, **113**, 36002.
- 63 X. Wu, V. Varshney, J. Lee, Y. Pang, A. K. Roy and T. Luo, *Chem. Phys. Lett.*, 2017, **669**, 233.
- 64 Z. Gao, F. Tao and J. Ren, *Nanoscale*, 2018, **10**, 12997.
- 65 L. Lindsay, D. A. Broido and N. Mingo, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2010, **82**, 115427.
- 66 L. Lindsay, W. Li, J. Carrete, N. Mingo, D. A. Broido and T. L. Reinecke, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2014, **89**, 155426.
- 67 A. A. Balandin, S. Ghosh, W. Bao, I. Calizo, D. Teweldebrhan, F. Miao and C. N. Lau, *Nano Lett.*, 2008, **8**, 902.
- 68 D. L. Nika, E. P. Pokatilov, A. S. Askerov and A. A. Balandin, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2009, **79**, 155413.
- 69 X. Xu, L. F. C. Pereira, Y. Wang, J. Wu, K. Zhang, X. Zhao, S. Bae, C. Tinh Bui, R. Xie and J. T. L. Thong, *et al.*, *Nat. Commun.*, 2014, **5**, 3689.