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# On the Second Explosion Limits of Hydrogen, Methane, Ethane, and Propane

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**ABSTRACT:** In this work, we have first investigated the explosion limit behaviors from hydrogen to propane through numerical simulations and validated with the available experimental data. The shape of the explosion limit curves and the possible turning points  $(P_{1-2}, T_{1-2})$ , first to second limit transition, and  $(P_{2-3}, T_{2-3})$ , second to third limit transition that bound the second explosion limit as a function of the fuel carbon number, have been examined. Results show that with an increase of methane mole fraction in the hydrogen/methane system, the upper turning point  $(P_{1-2}, T_{1-2})$  remains almost unchanged and the lower transition point  $(P_{2-3}, T_{2-3})$ rotates counterclockwise around  $(P_{1-2}, T_{1-2})$ . With a further increase of carbon number,  $(P_{1-2}, T_{1-2})$  moves to the lower-pressure and -temperature region and  $(P_{2-3}, T_{2-3})$  gradually moves to the lower-pressure and higher-temperature region. The slope of the second explosion limit is inversely proportional to the carbon number,  $k_{\rm PT} = 0.0069 - 0.005/(X_{\rm c} - 0.7)$ , approximately. Second, a sensitivity



analysis has been conducted to study the elementary reaction on the second explosion limits. The results show that the chain branching and termination reactions governing the explosion limit of hydrogen have a little effect on the second explosion limit of methane. The  $C_2H_5O_2H$  decomposition to form OH radicals is dominant in controlling the nonmonotonic behavior of the second explosion limit of  $C_2H_6$ . The second explosion limit behavior of propane is governed by three sets of reactions in the low-temperature oxidation process.

# 1. INTRODUCTION

Flammable gases widely exist in petroleum, coal, chemical, metallurgy, textile, medicine, and other industries. Under certain conditions, the combustible mixture will explode in the processes of transportation, storage, mining, and utilization, resulting in a huge loss of life and property. Therefore, the phenomenon of explosion has always been concerned by researchers owing to the explosion characteristics,<sup>1</sup> minimum ignition energy,<sup>2</sup> and flammability characteristics.<sup>3</sup> The explosion limits of a homogeneous fuel/oxidizer mixture that separates the explosive and nonexplosive regions are dominated by the competition of the radical producing and removing reactions, the result of which is pressure- and temperature-dependent.<sup>4</sup> As such, the explosion limit is typically characterized in the pressure-temperature parameter space and can be described by the pressure as a complex function of the system temperature. As a prominent example, the explosion limit of the  $H_2-O_2$  mixture presents a Z-shaped curve, which consists of two turning points. The nonexplosion to explosion transition boundary divides the pressure vs temperature curve into the first, second, and third explosion limits under the low-, medium-, and high-pressure conditions, respectively.5 The first and third explosion limits are controlled by the competitive mechanism of the chain branching reactions and the diffusion mechanism of active radicals to

the wall (chain termination step), while the second limit relies primarily on the competition between chain termination and branching reactions.<sup>4</sup> Semenov et al. studied the first explosion limit and found that the elimination of H radicals is more important than that of O and OH radicals when determining this limit.<sup>6</sup> However, Glassman pointed out that at low pressures, the elimination of OH and H radicals was equally critical to the first explosion limit.<sup>7</sup> When the pressure is sufficiently high, the reaction between HO<sub>2</sub> and H<sub>2</sub> produces  $H_2O_2$ , which subsequently decomposes to two OH radicals and increases system reactivity. When this lumped channel overtakes the wall destruction mechanism of HO<sub>2</sub>, explosion happens again, and this critical pressure is the so-called third explosion limit.8 Recently, Sánchez observed that the third explosion limit can be well predicted by five HO2- and H2O2involving reactions."

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The second explosion limit presents a significantly different characteristic compared with the first and third explosion limits. The appearance of the second explosion limit makes the explosion limit curve change from monotonic to nonmonotonic.<sup>10</sup> In particular, the second explosion limit of hydrogen is peculiar in that as the pressure is further increased inside the peninsular of the explosion regime, the mixture becomes nonexplosive. The second limit is the control limit of purified chemical kinetics, i.e., the free radical formation reaction competes with the termination reaction of the free radicals.<sup>11</sup> Moreover, as the three-body termination reaction H  $+ O_2 + M = HO_2 + M$  is pressure-sensitive, it will override the most effective chain branching reaction to generate the second explosion limit when the  $H_2/O_2$  system moves from a lower pressure to a higher pressure under a constant temperature. The appearance of the second explosion limit of hydrogen then demonstrates that the reactivity of the system in the mediumpressure region is reduced.

Plenty of studies on H<sub>2</sub>/O<sub>2</sub> systems have clearly recognized the three explosion limits and the corresponding controlling mechanisms for each limit. For explosion limits of larger molecules, however, only limited investigations have been conducted. Specifically, Liang et al. have investigated the hydrogen addition effect on the explosion limits of  $CO/O_2$ mixtures and showed that the explosion curve changed from a C-shape to Z-shape with minute quantities of hydrogen addition, and the most severe change appeared in the second explosion limit region.<sup>12</sup> Subsequently, they investigated the  $CH_4/O_2$  system and showed that the addition of 5% of H<sub>2</sub> also changed the monotonic explosion curve to the nonmonotonic Z-shaped one.<sup>13</sup> The presence of inert gas in the system did not affect the shape of the explosion limit curve but only shifted the explosion limit curve to higher temperatures.<sup>1</sup> Because propane occupies the position between lower and higher hydrocarbons, at very early times, Newitt and Thornes<sup>15</sup> experimentally measured the ignition temperature of propane/oxygen in a closed homogeneous reactor with varying pressures. They showed that at lower and higher pressures, the ignition temperature decreased with increasing pressure, while at intermediate pressures, the ignition temperature increased with increasing pressure, which was consistent with the widely recognized negative temperature coefficient (NTC) behavior caused by the formation of cool flame. At the same time, low-temperature combustion is accompanied by a cool flame, which not only affects the safety of the engine but also plays an important role in the combustion technology of the advanced engine.<sup>16</sup> Furthermore, the typical negative temperature coefficient (NTC) behavior was reported for larger alkanes.<sup>17</sup> Recently, Yu et al. first investigated the effect of equivalence ratio and N2 addition on the explosion limit of propane.<sup>18</sup> After that, Liu et al. investigated the effect of  $O_3$ addition on the cool flame region of the explosion limit of propane.19

The objectives of the present work are the following. Because only Newitt and Thornes reported the experimentally measured explosion temperature as a function of system pressure though that was decades ago and only propane was investigated. As such, our first objective is to use several wellrecognized kinetic mechanisms that have been widely used in the combustion chemistry community to numerically investigate the explosion limit behaviors from hydrogen to propane with gradually increasing the carbon number in the system. The shape of the explosion limit curve and the possible turning point shift as a function of the fuel carbon number will be examined. We note that the classic Z-shaped explosion limit curve has been widely recognized for the hydrogen/oxygen system, while fewer investigations for larger molecules have been reported. We also note that the second explosion limit depends on the competition between the chain branching and termination reactions, which may be complex and demands more investigations. As such, we will emphasize on the second explosion limit. Second, because the detailed mechanisms contain hundreds of chain branching and termination reactions, a sensitivity analysis will be conducted to find out the most important elementary reactions that control the second explosion limits of all of the C0-C3 alkane/oxygen systems. This can be realized by tuning the rate constant of each elementary reaction and accessing the response of the explosion limit curve, and by doing this, the sensitive reactions that affect the second explosion limit behaviors will be selected. These sensitive reactions will be subsequently removed individually from the mechanism, and the predictions from the mechanism without including these reactions will be compared with the original one to identify the controlling elementary reactions for the second explosion limit behaviors. In the following, we will specify our numerical method and the criterion of the explosion limit. Then, we will show our numerically calculated explosion limit curves using the validated kinetic mechanisms, followed by the effect of the dominant elementary reactions on the nonmonotonic second explosion limit curves.

## 2. NUMERICAL APPROACH METHOD

The explosion limits of C0–C3 alkanes are calculated using the SENKIN code.<sup>20</sup> An explosion is identified if the system temperature increases by 50 K compared with the initial temperature within 10 s under certain pressure conditions, as recommended in ref 5. The initial calculated pressure is ranged from 3.5 to  $3.2 \times 10^7$  Pa, which covers the working range of the common combustion devices, and the explosion temperature searching range is 350–2500 K. Other criteria like an average pressure increase rate of 3%/ms can be found for the determination of the cool flame ignition.<sup>21</sup>

Three different detailed chemical kinetic models are used in this study, which are the comprehensive *iso*-octane combustion model (KAUST),<sup>22</sup> Aramco 2.0 model,<sup>23</sup> and methane/ propane oxidation model<sup>24</sup> from the National University of Ireland Galway (NUIG). As the KAUST and Aramco 2.0 models include larger hydrocarbon molecules, only the C3 subset species and related reactions are used in this study. Diffusion of the carriers to the chamber wall is assumed to be much faster than wall absorption since only a small amount of the carriers that reach the wall are absorbed.<sup>5</sup> Moreover, concentrations of the carriers at the wall are assumed to be the same as those in the gas phase such that a zero-dimensional reactive system with a volume V and surface area S is assured.

The carriers are destroyed at the wall according to the reactions,

H, O, OH, HO<sub>2</sub>, H<sub>2</sub>O<sub>2</sub>, HCO  $\xrightarrow{k_{\text{H}}, k_{\text{O}}, k_{\text{HO}2}, k_{\text{HO}2}, k_{\text{HO}2}, k_{\text{HCO}}}$  wall destruction, with the corresponding reaction rate per unit volume  $k_{\text{H}}, k_{\text{O}}, k_{\text{OH}}, k_{\text{HO}}, k_{\text{HO}}, and k_{\text{HCO}}$  given by

$$k = \frac{1}{2}\varepsilon\overline{\nu}\frac{S}{V} \tag{1}$$



Figure 1. Comparison of the calculation and experimental explosion limits of hydrogen (a) and propane (b); the experiment data of the  $H_2$  are taken from ref 4, and the experiment data of  $C_3H_8$  are taken from ref 15.

where  $\overline{\nu} = (8k_{\rm B}T/\pi m)^{1/2}$  is the average velocity of the thermal motion of the carriers at temperature *T*, *m* is the molar mass, and  $k_{\rm B}$  is the Boltzmann constant. The sticking coefficient  $\varepsilon$  measures the destruction efficiency in the collision with the wall, and usually,  $\varepsilon \approx 10^{-5}$  to  $10^{-2}$  is selected for quartz.<sup>5</sup> As the reaction vessel used in the Newitt and Thornes experiment is made of transparent silica, the sticking coefficient is taken as  $10^{-3}$  in this study.

#### 3. RESULTS AND DISCUSSION

3.1. Kinetic Model Validation and the Boundary of the Second Explosion Limit. To begin with, the simulation results of the explosion limits for hydrogen and propane with different kinetic mechanisms are presented in Figure 1. Experimental data from Lewis and von Elbe for the hydrogen/oxygen system<sup>4</sup> and from Newitt and Thornes for the propane/oxygen system<sup>15</sup> are also used to validate these kinetic models. For stoichiometric hydrogen/oxygen, as shown in Figure 1a, all of the kinetic models reproduce the experimentally observed "Z-shaped" explosion limit curve in the pressure and temperature parameter space. The second explosion limit is bounded by two turning points,  $(P_{1-2}, T_{1-2})$ and  $(P_{2-3}, T_{2-3})$ . The turning point  $(P_{1-2}, T_{1-2})$  indicates the thermodynamic state that separates the first and second limits, and the point  $(P_{2-3}, T_{2-3})$  indicates the turning from the second limit to the third limit. On the first and the third explosion limit curves, the pressure decreases with an increase of temperature, indicating that at higher temperatures, explosion can be triggered with lower reactant concentrations. On the second explosion limit curve, the pressure increases with an increase of temperature, indicating that the explosion will be triggered with higher reactant concentrations. Additionally, all of the three kinetic models show excellent agreement with the experimental measurement from Lewis, including the prediction of the position and the two turning points that bound the second explosion limit.

The explosion limits for equimolecular propane/oxygen mixture are shown in Figure 1b, and experiments from Newitt and Thornes show that the curve is "S-shaped". All of the three models qualitatively captured the explosion limit curve, although the turning point predictions deviate slightly from the measurements. Compared with the kinetic models of Aramco 2.0 and KAUST, the methane/propane model shows better agreement between the predicted and measured turning points. Additionally, similar to that of hydrogen, on both the first and third explosion limit curves, the explosion pressure increases at lower temperatures, and on the second explosion limit curve, pressure increases at higher temperatures. However, the turning point pressure from the first to the second explosion limit  $P_{1-2}$  is higher than that from the second to the third explosion limit  $P_{2-3}$ , and the turning point temperature  $T_{1-2}$  is higher than  $T_{2-3}$ , which is different from the hydrogen/oxygen system shown in Figure 1a. This phenomenon is consistent with the negative temperature coefficient (NTC) characteristics for typical hydrocarbons. Because of its good performance for the explosion limit curve prediction, the methane/propane model (C1/C3)<sup>24</sup> is then selected for the following calculations of the C0–C3 alkane/ oxygen system.

To further verify the prediction ability of the methane/ propane mechanism, the comparison between the calculated and experimental explosion limits of methane and ethane are shown in Figure 2. It can be seen that the overall trend of the



**Figure 2.** Comparison of the calculated and experimental explosion limits of methane and ethane; the experimental data are taken from ref 25.

calculated results and the experimental results is in good agreement, and the position of the second explosion limit is also very close.

**3.2. Second Explosion Limit Dependence on Carbon Number.** Since both the first and third explosion limits have been well-recognized and reasonably interpreted by previous investigations,<sup>6-9</sup> we will then focus on the second explosion limit and see how it changes the Z-curve explosion limit behavior of the hydrogen/oxygen system to the S-curve behavior of the propane/oxygen system by gradually increasing the carbon number of the fuel. In each calculation, a stoichiometric fuel/ $O_2$  mixture is used.

3.2.1. From C0 to C1. Figure 3 shows the explosion limit curves of the  $H_2/CH_4/O_2$  system with increasing methane



Figure 3. Effect of methane addition on the second explosion limit of hydrogen.

substitution ( $X_{Cl}$ , the mole fraction of methane in the H<sub>2</sub>/ methane fuel blends). As can be seen that the upper turning point  $(P_{2-3} = 0.86 \text{ bar}, T_{2-3} = 825.8 \text{ K})$  remains almost unchanged with an increase of CH<sub>4</sub> substitution, indicating that increasing the carbon number has a weak influence on the second to the third explosion limit transition. However, with an increase of  $X_{Cl}$ , the transition point for the first to the second explosion limit  $(P_{1-2}, T_{1-2})$  gradually moves to the higher-pressure and -temperature region, i.e., (0.012 bar, 712.9 K), (0.014 bar, 753.2 K), and (0.017 bar, 794 K), respectively, for  $X_{C1} = 20, 40$ , and 60%. As such, the second limit rotates counterclockwise around the upper turning point and the explosion region is narrowed. In addition, with an increase of  $X_{Cl}$ , the positive slope of the second explosion limit curve significantly increases to an infinitely large value at  $X_{C1} \approx 20\%$ . Then, the slope ( $k_{\text{PT}}$ , defined in Section 3.3) transits to a negative value and the magnitude of the slope decreases with further increasing  $X_{C1}$ . As a consequence, the explosion curve transits from nonmonotonic (pure H<sub>2</sub>) to monotonic (pure  $CH_4$ ), and the turning point that separates the three explosion limits cannot be determined clearly such that the second explosion limit vanishes. In this case, we define a pseudo- $(P_{1-2}, P_{1-2})$  $T_{1-2}$ ) for a higher  $X_{C1}$  (>0.8) system by extrapolating the welldefined turning point  $(P_{1-2}, T_{1-2})$  for a lower  $X_{C1}$  (0-0.6) system to higher  $X_{C1}$  cases. In this way, we can clearly see the trend of the second limit behavior, which can be quantified by the value of  $k_{\rm PT}$ .

3.2.2. From C1 to C2. Figure 4 shows the explosion limit curves of the CH<sub>4</sub>/C<sub>2</sub>H<sub>6</sub>/O<sub>2</sub> system with increasing ethane substitution ( $X_{C2}$ , the mole fraction of methane in the CH<sub>4</sub>/C<sub>2</sub>H<sub>6</sub> fuel blends). For the methane/oxygen system, the explosion pressure exhibits a monotonic decrease with an increase of temperature in the whole examined region. For  $X_{C2}$  < 10%, no obvious turning points show up on the whole explosion pressure for temperatures higher than 700 K does not change much, while for lower temperatures, the explosion pressure decreases. For  $X_{C2}$  > 10%, the increased carbon number results in the presence of two turning points and bound a period of an almost horizontal line. As such, the



Figure 4. Effect of ethane addition on the second explosion limit of methane.

second explosion limit is retrieved. On the second explosion limit curve, the pressures for different  $X_{C2}$  systems all show weak dependence on temperature. However, the turning point for the first to the second limit  $(P_{1-2}, T_{1-2})$  gradually moves to higher temperatures, while the turning point for the second to the third limit transition  $(P_{2-3}, T_{2-3})$  moves to a lowertemperature region, resulting in an expanded second limit region. Because for  $X_{C2}$  larger than 10% the two turning points can be well defined, we also extrapolate the bound pressure and temperature on the second explosion limit to lower  $X_{C2}$ cases such that we also get two pseudoturning points for lower  $X_{C2}$  cases. It is noted that for the pure CH<sub>4</sub>/O<sub>2</sub> system ( $X_{C1}$  = 1 for  $H_2/CH_4$  or  $X_{C2} = 0$  for  $CH_4/C_2H_6$  fuel blends), there is no second explosion limit. As such, the pseudoturning points obtained by extrapolating  $X_{C2}$  from 1 to 0 in CH<sub>4</sub>/C<sub>2</sub>H<sub>6</sub> in Figure 4 do not show the pseudoturning points in Figure 3, which is obtained by extrapolating  $X_{C1}$  from 0 to 1. It seems that the second limit curve also rotates counterclockwise with an increase of carbon number  $X_{C2}$ .

3.2.3. From C2 to C3. Figure 5 shows the explosion limit curves of the  $C_2H_6/C_3H_8/O_2$  system with increasing propane



**Figure 5.** Effect of propane addition on the second explosion limit of ethane.

substitution ( $X_{C3}$ , the mole fraction of propane in the C<sub>2</sub>H<sub>6</sub>/C<sub>3</sub>H<sub>8</sub> fuel blends). It is seen that for all different  $X_{C3}$  cases, the explosion limit curve is "S"-shaped, and with an increase of  $X_{C3}$ , nonmonotonic S-shaped behavior of the curve becomes more severe and the second explosion limit shifts to lower pressures. In addition, the transition point temperature  $T_{1-2}$ 

gradually moves to a higher-temperature region, while the transition point temperature for the second to the third explosion limit  $T_{2-3}$  gradually moves to a lower-temperature region, indicating an extended second explosion limit. Furthermore, the reduction extent of  $P_{2-3}$  is comparable to that of  $P_{1-2}$  for small  $X_{C3}$  cases, and a more obvious decrease of  $P_{2-3}$  is observed when  $X_{C3}$  is larger than 0.1. From ethane to propane, it seems that the second limit curve again rotates counterclockwise with an increase of carbon number  $X_{C3}$ .

3.2.4. Overall Trend of the Second Limit Slope Versus Carbon Number. With an increase of carbon number, the second explosion limit curves all rotate counterclockwise, as shown in Figures 3–5. To more clearly present the effect of carbon number on the second explosion limit, the slope of the quasi-linear relationship between the logarithmic pressure and temperature is derived, as in eq 2.

$$k_{\rm PT} = (\lg(P_{1-2}/1 \text{ atom}) - \lg(P_{2-3}/1 \text{ atom})) /(T_{1-2} - T_{2-3})$$
(2)

where  $P_{1-2}$  and  $P_{2-3}$  are the pressures of the turning points and  $T_{1-2}$  and  $T_{2-3}$  are the temperatures of the turning points.

Figure 6 shows the  $k_{\text{PT}}$  as a function of the carbon number. Carbon number ranges of [0, 1], [1, 2], and [2, 3],



Figure 6. Trends of the slopes of the second explosion limit from  $C_0$  to  $C_3$ .

respectively, represent fuel mixtures of  $H_2/CH_4$  ( $0 \le X_{C1} \le 1.0$ ),  $CH_4/C_2H_6$  ( $0 \le X_{C2} \le 1.0$ ), and  $C_2H_6/C_3H_8$  ( $0 \le X_{C3} \le 1.0$ ).

It is seen that with an increase of carbon number, the slope variations can be divided into two regions. Pure hydrogen has a positive slope, further increasing  $X_{\rm C1}$  initially weakly and then significantly increasing the slope to an infinitely large value at  $X_{\rm C1} \approx 0.7$  (carbon number  $\approx 0.7$ ). Then, the slope just changes from positive infinity to negative infinity and the magnitude gradually decreases. As the carbon number further increases, the slope magnitude gradually decreases to zero at the carbon number only weakly increases the slope with a positive sign. The dependence of the slope of the second explosion limit on the carbon number can be expressed as the following function

$$k_{\rm PT} = 0.0069 - 0.005/(X_{\rm c} - 0.7) \tag{3}$$

It is shown from Figure 6 that the slope calculated by this fit function agrees well with the slope calculated from the

explosion limit curve. Therefore, the slope of the second explosion limit is inversely proportional to the carbon number.

3.3. Controlling Elementary Reactions for the Second **Explosion Limit.** We note that the second explosion limit is controlled by the competition between the chain branching and termination reactions.<sup>4,11</sup> For the carbon number lower than 0.70, chain termination reactions dominate the second explosion limit because the transition temperature  $T_{2-3}$  is larger than  $T_{1-2}$ , resulting in a nonexplosion peninsular, as shown in Figure 3. With an increase of carbon number,  $T_{1-2}$ gradually increases and approaches  $T_{2-3}$ . As such, the nonexplosive peninsular region gradually narrows, indicating that the chain termination reactions become weaker compared to the chain branching reactions. When the carbon number is increased to around 0.70,  $T_{1-2}$  equals  $T_{2-3}$ , the nonexplosive peninsular vanishes, and the roles of the chain termination reactions and the chain branching reactions are comparable. For the carbon number higher than 0.70,  $T_{1-2}$  is always larger than  $T_{2-3}$  indicating that the chain branching reactions become dominant in controlling the second explosion limit. Additionally, since the kinetics of different fuel systems inherently contain different chain termination and chain branching reactions, we will then examine further what are those elementary reactions (either chain branching or termination) that dominate the second explosion limit.

To realize this goal, a two-step approach is adopted. First, to find the key reactions controlling the second explosion limit behavior for C0-C3 alkane molecules, the sensitivity analysis is conducted by perturbing the rate constant of each elementary reaction and comparing the corresponding explosion limit curve with the original one. In each sensitivity calculation, the pre-exponential factor of the rate constant is reduced by 90% for each individual reaction. The explosion limit curve calculated by the modified mechanism will be compared with that calculated by the original mechanism. The reactions that have an obvious effect on the explosion curves will be retained in the reduced mechanism. As the key reactions related to the explosion limit of pure hydrogen have been studied extensively in previous research, the sensitivity analysis with respect to hydrogen is not performed in this study.<sup>12,14</sup> Instead, a nine-reaction mechanism is directly used as the reduced mechanism of hydrogen, where the reaction rate constants and the thermal parameters are all taken from the methane/propane model.<sup>24</sup>

The sensitivity analysis shows that a total number of 30 reactions should be retained to reproduce the explosion limit of methane calculated by the detailed mechanism. In addition, the explosion limit of  $C_2H_6$  can be well reproduced with 77 reactions based on the sensitivity analysis. Furthermore, to maintain the accuracy of the explosion limit calculations, a total number of 194 reactions are kept in the reduced mechanism for  $C_3H_8$ . The explosion limits of the stoichiometric hydrogen/oxygen, methane/oxygen, ethane/oxygen, and propane/oxygen mixtures calculated by the detailed and reduced mechanisms are compared in Figure 7. It is shown that the shape and position of the explosion limits calculated by the detailed mechanism with 9, 30, 77, and 194 reactions for hydrogen, methane, ethane, and propane, respectively.

Second, we remove the most sensitive elementary reactions in the reduced mechanism one at a time and compare the correspondingly calculated second explosion limit with the original reduced model. By doing this, the elementary reactions



Figure 7. Comparison of the calculation explosion limits of  $H_2$ ,  $CH_4$ ,  $C_2H_{6\prime}$  and  $C_3H_8$  with the detailed and reduced mechanism.

that affect the second explosion limit most will be found out. The criterion is to see whether the complete explosion limit curve will lose its nonmonotonic behavior for hydrogen, ethane, or propane. In the following, we apply these two steps toward hydrogen, methane, ethane, and propane systems, respectively.

3.3.1. Toward  $H_2$  and  $CH_4$ . We first compare the explosion limit curves calculated by the reduced mechanism (black solid line) and the mechanism with reducing the rate constant of H +  $O_2 \Leftrightarrow O$  + OH (red dash) and H +  $O_2$  + M  $\Leftrightarrow$  HO<sub>2</sub> + M (blue dot) by 90%, as shown in Figure 8a. Other elementary reactions that have much weaker effects are not shown. This comparison indicates that the third-body termination reaction H +  $O_2$  + M  $\Leftrightarrow$  HO<sub>2</sub> + M and the chain branching reaction H +  $O_2 \Leftrightarrow O$  + H are the most sensitive in determining the explosion limit for hydrogen. For methane, as shown in Figure 8b, the explosion limit curve is monotonic and these two reactions have almost no effect on the explosion limit curve.

For the second step, the explosion limits of hydrogen and methane are calculated without including the termination reaction  $(H + O_2 + M \Leftrightarrow HO_2 + M)$  or the branching reaction  $(H + O_2 \Leftrightarrow O + OH)$  in the reduced mechanisms, as shown in Figure 9. It is obvious that the explosion limit curve of hydrogen will lose its nonmonotonic characteristics when the termination reaction is excluded in the reduced mechanisms and the reactivity of the system is significantly improved, as shown in Figure 9a. In addition, when the branching reaction is not included in the reaction mechanism, the reactivity of the hydrogen/oxygen mixture reduces significantly as the explosion limit moves toward a high-temperature region. However, there is only a very small shift for the methane explosion limit without including the termination or branching reaction in the reduced mechanism, as shown in Figure 9b. So, the dominated chemical kinetics of these two fuels on the explosion limit is inconsistent.

The main reactions with larger sensitivity on the explosion limit of methane are given in Figure 10. The oxidation of methane is initiated by  $CH_4 + O_2 = CH_3 + HO_2$ , from which the methyl and OH radicals will be generated. After the radical pool is formed, the most sensitive methane-related reactions are  $CH_4 + OH \Leftrightarrow CH_3 + H_2O$  and  $CH_4 + HO_2 \Leftrightarrow CH_3 +$  $H_2O_2$ . The reaction of methyl (CH<sub>3</sub>) with hydroperoxyl (HO<sub>2</sub>) is important as the concentrations of both radicals are very high during the oxidation process of methane. The reaction path can be a chain-propagating reaction  $CH_3 + HO_2$ =  $CH_3O + OH$  or a termination reaction  $CH_3 + HO_2 = CH_4 +$  $O_2$ . The reaction of the formyl radical is considered important for flame speed predictions. For explosion limit calculations, the formyl decomposition reaction HCO + M = H + CO + Mand the reaction with molecular oxygen HCO +  $O_2 = CO +$ HO<sub>2</sub> are both important. The formyl radical is generated from CH<sub>2</sub>O reacted with OH and CH<sub>3</sub>. Also, CH<sub>2</sub>O radicals are produced from CH<sub>3</sub> and CH<sub>3</sub>O in their reaction with molecular oxygen. The reactions involving methyl, methoxy, and methylperoxy have a significant effect on the explosion limit of methane. This means that for the methane oxidation process the reactive free radicals are mainly generated through the C<sub>1</sub> subset reactions, which are very important in reproducing the correct kinetic behavior. As the explosion limit was no longer dominated by the chain termination reaction, the explosion limit has no nonmonotonic characteristics compared with the explosion limit of hydrogen.

3.3.2. Toward  $C_2H_6$ . By the same approach, we have first found the seven elementary reactions exhibiting the largest sensitivity with respect to the explosion limit of  $C_2H_6$ , as shown in Figure 11. Similar to the methane case, the branching reaction  $H + O_2 \Leftrightarrow O + H$  also has almost no effect on the explosion limit. However, the  $H_2O_2$  decomposition reaction obviously affects the first explosion limit. We note that after the radical pool is formed, ethane is mainly consumed through Habstraction by H or  $HO_2$ , instead of by  $O_2$ . The ethylperoxy radical  $C_2H_5O_2$  is largely produced by the addition of molecular oxygen to the ethyl radical due to the long lifetime of  $RO_2^{\bullet}$  radicals, which is the most important species for ethane oxidation.<sup>26</sup> The ethylperoxy radical can further abstract a hydrogen atom from ethane to generate  $C_2H_5O_2H$ . The cleavage



Figure 8. Sensitivities of the chain termination and branching reactions on the explosion limits of hydrogen (a) and methane (b).



Figure 9. Effect of the chain and termination reaction on the second explosion limits of hydrogen (a) and methane (b).



Figure 10. Main reactions with larger sensitivity on the explosion limit of methane.



Figure 11. Reactions exhibiting the largest sensitivities with respect to the explosion limit of  $C_2H_6$ .

of the weak O–O bond of  $C_2H_5O_2H$  leads to a chain branching reaction  $C_2H_5O_2H \Leftrightarrow C_2H_5O + OH.^{27}$  As the rate of the  $C_2H_5O_2H$  generation reaction reduces, the length of the second explosion limit reduces and  $P_{1-2}$  and  $P_{2-3}$  both increase. The reduction of the reaction rate of  $C_2H_5O_2H \Leftrightarrow$  $C_2H_5O + OH$  will shorten the length of the second explosion limit, while  $P_{1-2}$  is almost not changed. Under low-pressure conditions,  $C_2H_5O_2H$  is largely decomposed to  $C_2H_4 + HO_2$ . With the reduction of the rate of  $C_2H_5O_2H$  decomposition, both  $P_{1-2}$  and  $P_{2-3}$  are reduced obviously. For the ethane system, the hydroperoxyethyl species  $C_2H_4O_2H$  is unimportant for the explosion limit of ethane because only a negligibly small amount of  $C_2H_5O_2$  undergoes the isomerization process.<sup>26</sup> Figure 12 shows that when  $C_2H_5O_2H \Leftrightarrow C_2H_5O + OH$  is removed in the mechanism, the calculated explosion limit



Figure 12. Dominant reactions for the explosion limit behaviors of  $C_2H_6$ .

changes drastically and becomes monotonic. In addition, removing  $C_2H_6 + C_2H_5O_2 \Leftrightarrow C_2H_5 + C_2H_5O_2H$  will significantly shorten the length of the second explosion limit and the second limit is shifted to higher pressures. The  $C_2H_5O_2H$  decomposition to form the OH radical is dominant in controlling the nonmonotonic behavior of the second explosion limit of  $C_2H_6$ .

3.3.3. Toward  $C_3H_8$ . As the carbon number increases, more reaction channels become to affect the explosion limit curve,<sup>28</sup> and the determination of the dominant reaction for the second explosion limit of C3H8 is more complex since more fuelspecific reactions are affecting the explosion limit behavior. Figure 13 shows that the most sensitive reactions do not affect the general nonmonotonic explosion limit behavior but only shift the two turning points. H-abstraction from propane by OH and HO<sub>2</sub> produces two isomers. *n*-Propyl  $(n-C_3H_7)$  and iso-propyl  $(i-C_3H_7)$  are generated by OH,<sup>29</sup> and  $i-C_3H_7$  is produced through hydrogen abstraction by the HO<sub>2</sub> radical. Then, the addition of produced propyl radicals to molecular oxygen forms propylperoxyl radicals  $(C_3H_7O_2)$ , which then undergo the isomerization process to generate the propylhydroperoxyl radical C<sub>3</sub>H<sub>6</sub>OOH. The propylhydroperoxyl radical can decompose to  $C_3H_6 + HO_2$  or react with molecular oxygen to form  $C_3H_6OOHO_2$ . The formed  $C_3H_6OOHO_2$  will decompose to c3ket + OH. Thereafter, the decomposition of



Figure 13. Most sensitive reactions and their effect on the explosion limit behaviors of  $C_3H_8$  (a, b).

c3ket will generate a second OH radical. These reactions have also been recognized to be responsible for the NTC behavior of the larger hydrocarbons.<sup>30</sup>

Figure 14 further shows the comparison between the calculated explosion limits with removing the three types of



Figure 14. Dominant reactions for the second explosion limit of  $C_3H_8$ .

reaction groups and the calculations with the original mechanism. First, if the reaction path of the molecular oxygen addition to propylhydroperoxyl radical (the second O<sub>2</sub> addition) is cut off, which is used to block the formation of the twice OH radical generation in the chain branching path, the second explosion limit changes to almost a horizontal line instead of the nonmonotonic curve. Second, the second explosion limit still appears as a line with a small inclined angle when the second OH release reactions (the c3ket decomposition reactions) are deleted from the mechanism. This is because the first OH release reactions are still working. Third, when the reactions of the molecular oxygen addition and the decomposition of C<sub>3</sub>H<sub>6</sub>OOH are both excluded from the mechanism, a quasi-monotonic explosion limit curve is achieved. This means that C3H6OOH undergoes the decomposition reaction when the molecular oxygen addition reaction path is blocked, which will generate the  $C_3H_6$  radical. The C<sub>3</sub>H<sub>6</sub> subset reactions will give an explosion limit similar to that of C<sub>2</sub>H<sub>6</sub>. From the above analysis, it is concluded that the second explosion limit behavior of propane is governed by the three sets of reactions, as presented in Figure 14.

#### 4. CONCLUSIONS

In this study, the explosion limits of the typical  $C_0-C_3$  alkanes are analyzed computationally and theoretically. The critical path of the reaction influencing the second explosion limit is found. The key elementary reactions affecting the explosion limit of  $C_0-C_3$  alkanes are obtained.

The second explosion limit of pure hydrogen has a positive slope, further increasing  $X_{\rm C1}$  initially weakly then significantly increases the slope to an infinitely large value at  $X_{\rm C1} \approx 0.7$ . Then, the slope just changes from positive infinity to negative infinity and the magnitude gradually decreases. As the carbon number further increases, the slope magnitude gradually decreases to zero at the carbon number around 1.5. Further increasing the carbon number only weakly increases the slope with a positive sign. The dependence of the slope of the second explosion limit on the carbon number can be expressed using an inverse proportional function.

The termination reaction  $H + O_2 + M \Leftrightarrow HO_2 + M$  and the chain branching reaction  $H + O_2 \Leftrightarrow O + H$ , which are the key reactions in determining the explosion limit of  $C_0$ , have a very small effect on the explosion limit of C1-C3. The non-monotonic characteristic of the C2 explosion limit is controlled by the chain propagation reaction  $C_2H_5O_2H \Leftrightarrow C_2H_5O + OH$ . The NTC behavior in the explosion limit of C3 is governed by the low-temperature reactions of  $C_3H_8$ , which will generate two OH radicals and significantly improve the reactivity of the system.

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#### Notes

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